

# Event-by-event average $p_T$ fluctuations in $\sqrt{s_{NN}} = 200$ GeV Au+Au and p+p collisions in PHENIX: measurements and jet contribution simulations

M J Tannenbaum (for the PHENIX Collaboration)<sup>1</sup>

Physics Department, 510c, Brookhaven National Laboratory, Upton, NY 11973-5000, USA

Received 15 March 2004

Published 19 July 2004

Online at [stacks.iop.org/JPhysG/30/S1367](http://stacks.iop.org/JPhysG/30/S1367)

doi:10.1088/0954-3899/30/8/129

## Abstract

Small, but significant non-random fluctuations in event-by-event average  $p_T$  have been observed in Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV by the PHENIX Collaboration. These are consistent with being caused by correlations due to jets at large  $p_T$ , where the measured suppression must be included to reproduce the centrality dependence of the non-random fluctuations.

(Some figures in this article are in colour only in the electronic version)

## 1. The event-by-event average $p_T$ distribution is not a Gaussian, it is a Gamma distribution

The single-particle inclusive  $p_T$  distribution averaged over all particles in all events in a p–p experiment (inclusive) or in a given centrality class in an A+A experiment (semi-inclusive) is usually written in the form

$$\frac{d\sigma}{p_T dp_T} = b^2 e^{-bp_T} \quad \text{or} \quad \frac{d\sigma}{dp_T} = b^2 p_T e^{-bp_T}. \quad (1)$$

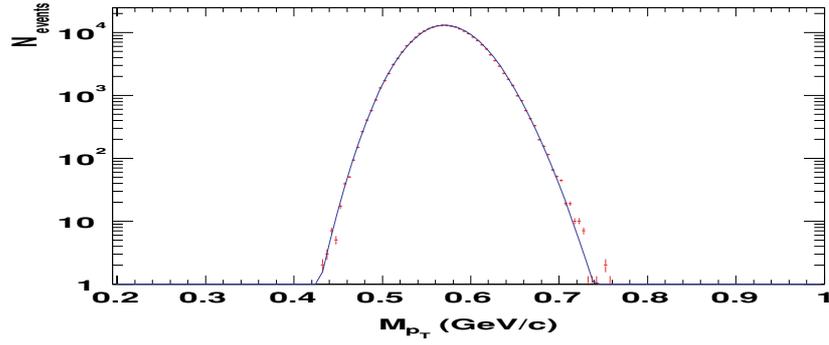
Equation (1) represents a Gamma distribution with  $p = 2$ , where  $\langle p_T \rangle = p/b$ ,  $\sigma_{p_T}/\langle p_T \rangle = 1/\sqrt{p}$  and typically  $b = 6$  (GeV/c)<sup>−1</sup> for p–p collisions. The ‘inverse slope parameter’  $T = 1/b$  is sometimes referred to as the ‘temperature parameter’.

For events with  $n$  detected charged particles with magnitudes of transverse momenta,  $p_{T_i}$ , the event-by-event average  $p_T$ , denoted by  $M_{p_T}$  is defined as

$$M_{p_T} = \overline{p_T} = \frac{1}{n} \sum_{i=1}^n p_{T_i} = \frac{1}{n} E_{Tc}. \quad (2)$$

For the case of statistical independent emission, where the fluctuations are purely random, an analytical formula for the distribution in  $M_{p_T}$  can be obtained assuming negative binomial

<sup>1</sup> For the full PHENIX Collaboration author list and acknowledgments, see appendix ‘Collaborations’ of this volume.



**Figure 1.** PHENIX mixed-event distribution for the 0–5% centrality class (data points) compared to equation (3) (curve).

(NBD) distributed event-by-event multiplicity, with Gamma distributed semi-inclusive  $p_T$  spectra [1]. The formula depends on the four semi-inclusive parameters  $\langle n \rangle$ ,  $1/k$ ,  $b$  and  $p$  which are derived from the means and standard deviations of the semi-inclusive  $p_T$  and multiplicity distributions,  $\langle n \rangle$ ,  $\sigma_n$ ,  $\langle p_T \rangle$  and  $\sigma_{p_T}$ :

$$f(y) = \sum_{n=n_{\min}}^{n_{\max}} f_{\text{NBD}}(n, 1/k, \langle n \rangle) f_{\Gamma}(y, np, nb), \quad (3)$$

where  $y = M_{p_T}$ . For fixed  $n$ , and purely random fluctuations, the mean and standard deviation of  $M_{p_T}$  follow the expected behaviour,  $\langle M_{p_T} \rangle = \langle p_T \rangle$ ,  $\sigma_{M_{p_T}} = \sigma_{p_T} / \sqrt{n}$ . In PHENIX, equation (3) is used to confirm the randomness of mixed events (figure 1).

## 2. Measurement of non-random fluctuations in PHENIX

Mixed events are used to define the baseline for random fluctuations of  $M_{p_T}$  in PHENIX [2, 3]. This has the advantage of effectively removing any residual detector-dependent effects. The event-by-event average distributions are very sensitive to the number of tracks in the event (denoted by  $n$  or  $N_{\text{tracks}}$ ), so the mixed-event sample is produced with the *identical*  $N_{\text{tracks}}$  distribution as the data. Additionally, no two tracks from the same data event are placed in the same mixed event in order to remove any intra-event correlations in  $p_T$ . Finally,  $\langle M_{p_T} \rangle$  must exactly match the semi-inclusive  $\langle p_T \rangle$ . As noted above, the randomness of  $M_{p_T}$  for the mixed-event sample is tested by comparison to equation (3). Figure 1 shows the excellent agreement between the calculation and the mixed-event  $M_{p_T}$  distributions for the 0–5% centrality class. The standard deviations,  $\sigma_{M_{p_T}}$ , differ by less than 0.04%. This represents the maximum error from any effects introduced by the event-mixing procedure.

The measured  $M_{p_T}$  distributions for the data in two centrality classes for  $\sqrt{s_{\text{NN}}} = 200$  GeV Au+Au collisions in PHENIX are shown in figure 2 (data points) compared to the mixed-event distributions (histograms). The non-Gaussian, Gamma distribution shape of the  $M_{p_T}$  distributions is evident. The difference between the data and the mixed-event random baseline distributions is barely visible to the naked eye. The non-random fluctuation is quantified by the per cent difference of the standard deviations of  $M_{p_T}$  for the data and the mixed-event (random) sample:

$$F_{p_T} \equiv \frac{\sigma_{M_{p_T}, \text{data}} - \sigma_{M_{p_T}, \text{mixed}}}{\sigma_{M_{p_T}, \text{mixed}}}. \quad (4)$$

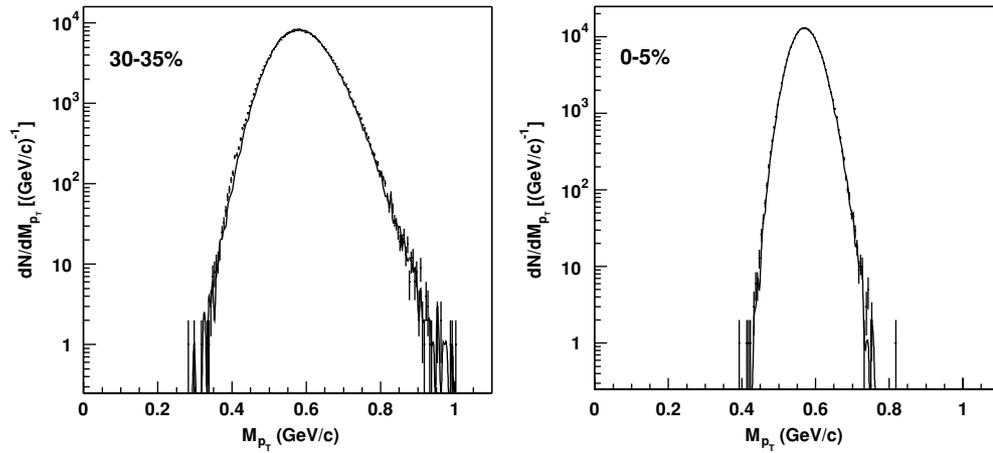


Figure 2.  $M_{p_T}$  for 30–35% and 0–5% centrality classes: data (points) mixed events (histogram).

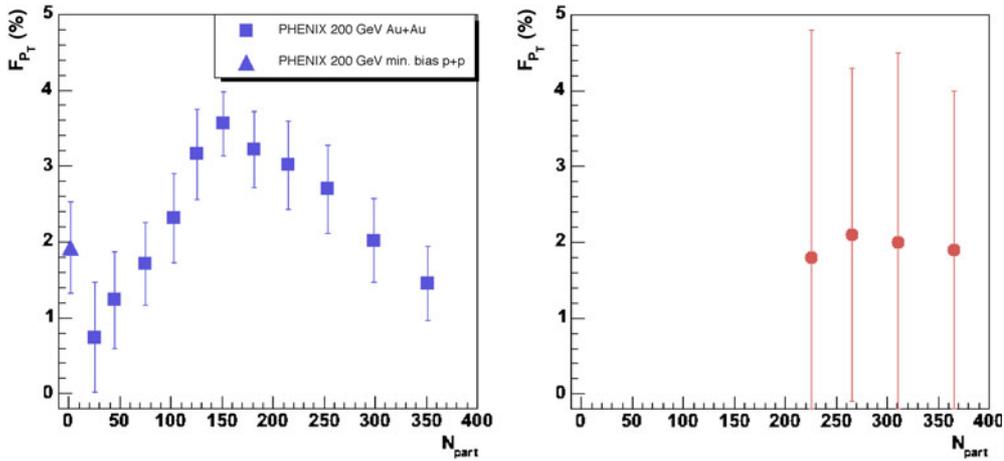


Figure 3.  $F_{p_T}$  in %: (left) Au+Au, p+p,  $\sqrt{s_{NN}} = 200$  GeV, (right) Au+Au 130 GeV.

The results are shown as a function of centrality represented by  $N_{\text{part}}$  in figure 3 compared to the previous PHENIX measurement at  $\sqrt{s_{NN}} = 130$  GeV [2]. The errors shown are systematic errors due to time-dependent detector variations. Comparatively, statistical errors are negligible. The systematic error is calculated from the rms variation of  $F_{p_T}$  from ten independent subsets of the data. The improvement over the  $\sqrt{s_{NN}} = 130$  GeV data is due to three times larger solid angle (larger  $N_{\text{tracks}}$ ), better tracking and more statistics [3].

The dependence of  $F_{p_T}$  on  $N_{\text{part}}$  is striking. To further understand this dependence and the source of these non-random fluctuations,  $F_{p_T}$  was measured over a varying  $p_T$  range,  $0.2 \text{ GeV}/c \leq p_T \leq p_T^{\text{max}}$  (figure 4), where  $p_T^{\text{max}} = 2.0 \text{ GeV}/c$  for the  $N_{\text{part}}$  dependence. The increase of  $F_{p_T}$  with  $p_T^{\text{max}}$  suggests elliptic flow or jet origin. This was investigated using a Monte Carlo simulation of correlations due to elliptic flow and jets in the PHENIX acceptance. The flow was significant only in the lowest centrality bin and negligible ( $F_{p_T} < 0.1\%$ ) at higher centralities. Jets were simulated by embedding (at a uniform rate per generated particle,  $S_{\text{prob}}(N_{\text{part}})$ ) p–p hard-scattering events from the PYTHIA event generator into simulated

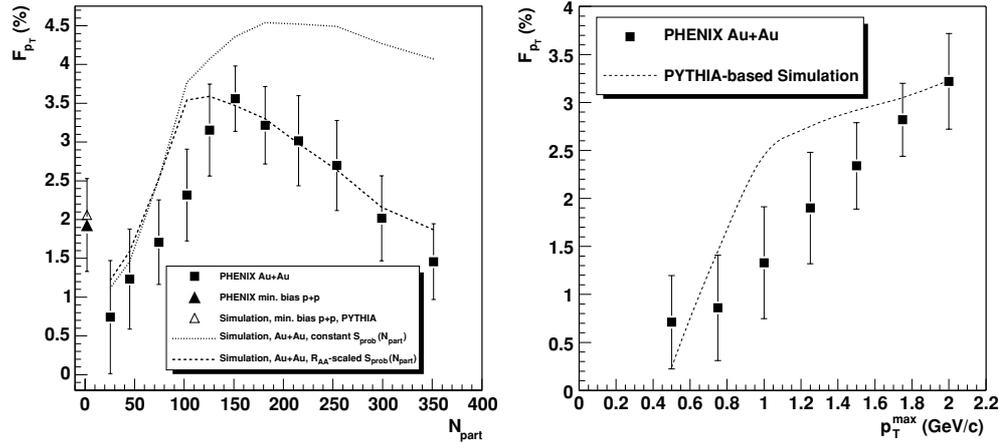


Figure 4.  $F_{p_T}$  versus centrality and  $p_T^{max}$  compared to simulations.

Au+Au events assembled at random according to the measured  $N_{tracks}$  and semi-inclusive  $p_T$  distributions. This changed  $\langle p_T \rangle$  and  $\sigma_{p_T}$  by less than 0.1%.  $S_{prob}(N_{part})$  was either constant for all centrality classes, or scaled by the measured hard-scattering suppression factor  $R_{AA}(N_{part})$  for  $p_T > 4.5$  GeV/c [4]. A value  $F_{p_T} = 2.06\%$  for p-p collisions was extracted from pure PYTHIA events in the PHENIX acceptance in agreement with the p-p measurement. The value of  $S_{prob}(N_{part})$  was chosen so that the simulation with  $S_{prob}(N_{part}) \times R_{AA}(N_{part})$  agreed with the data at  $N_{part} = 182$ . The centrality and  $p_T^{max}$  dependences of the measured  $F_{p_T}$  match the simulation very well, but only when the  $R_{AA}$  scaling is included.

A less experiment-dependent method to compare non-random fluctuations is to assume that the entire  $F_{p_T}$  is due to temperature fluctuations of the initial state, with rms variation  $\sigma_T/\langle T \rangle$  [5, 2]:

$$F_{p_T} = \frac{(\langle n \rangle - 1)}{2} \frac{\sigma_T^2 / \langle T \rangle^2}{\sigma_{p_T}^2 / \langle p_T \rangle^2} = \frac{p}{2} (\langle n \rangle - 1) \frac{\sigma_T^2}{\langle T \rangle^2}. \quad (5)$$

This yields  $\sigma_T/\langle T \rangle = 1.8\%$  for central collisions and 3.7% at the peak of  $F_{p_T}$ , which puts severely small limits on the critical fluctuations that were expected.

## References

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