

# *Space-time Evolution of Bulk QCD Matter at RHIC*

Chiho NONAKA  
*Nagoya University*

## **Contents**

- Introduction
  - Hydrodynamic models at RHIC
  - Freezeout process, finite state interactions
- 3D hydro+UrQMD
- Results
  - Single particle spectra, reaction dynamics, elliptic flow
- Summary

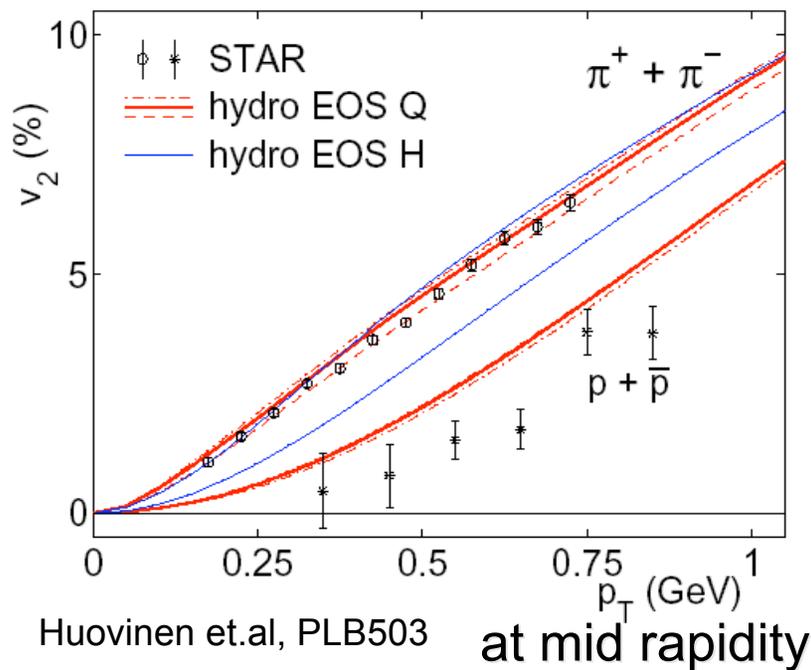
In collaboration with Steffen A. Bass (Duke University & RIKEN BNL)

June 7@RHIC AGS annual users' meeting

# Hydrodynamic Models at RHIC

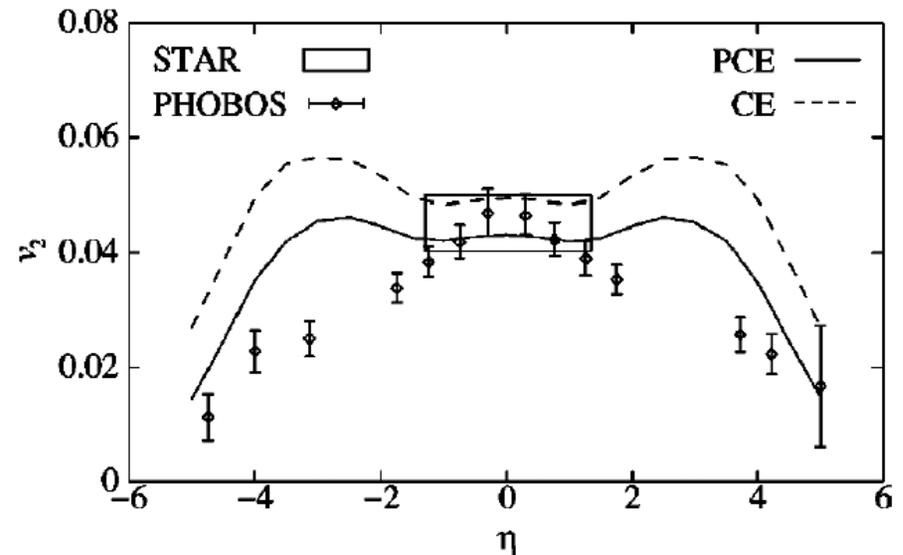
## Success of Perfect Hydrodynamic Models at RHIC

- Single particle spectra  
Huovinen, Kolb, Heinz, Hirano, Teaney, Shuryak, Hama, Morita, .....
- Strong elliptic flow  
Strong coupled (correlated) QGP



## However....

-Elliptic flow vs.  $\eta$



Hirano and Tsuda, PRC66

Discrepancy at large  $\eta$ :

- Insufficient thermalization?
- Viscosity effect?
- Simple freezeout process?

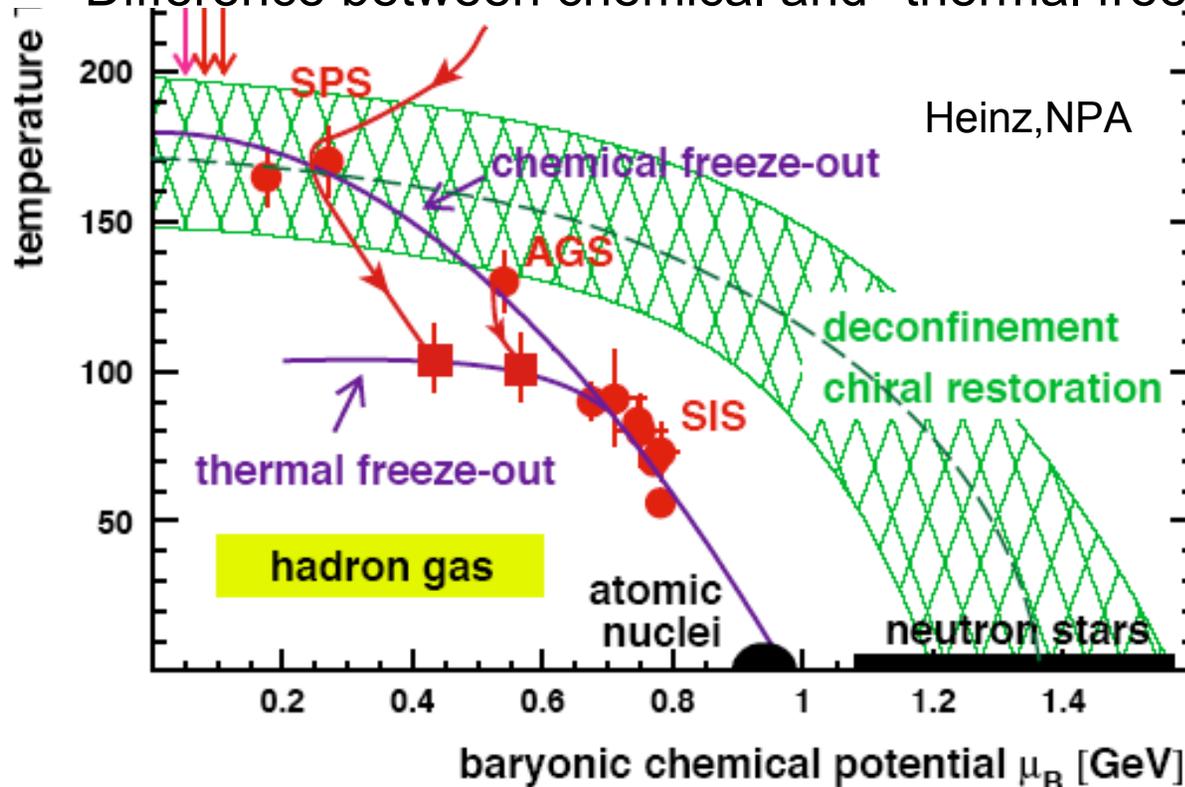
→ • *freezeout*  
• *viscosity*

RHIC & AGS annual users' meeting

# Freezeout process in Hydro

## 1. Single freezeout temperature?

– Difference between chemical and thermal freezeout



- chemical freezeout statistical model  
 $T_{\text{ch}} \sim 170$  MeV  
 hadron ratio
- thermal freezeout hydro  
 $T_f \sim 110\sim 140$  MeV

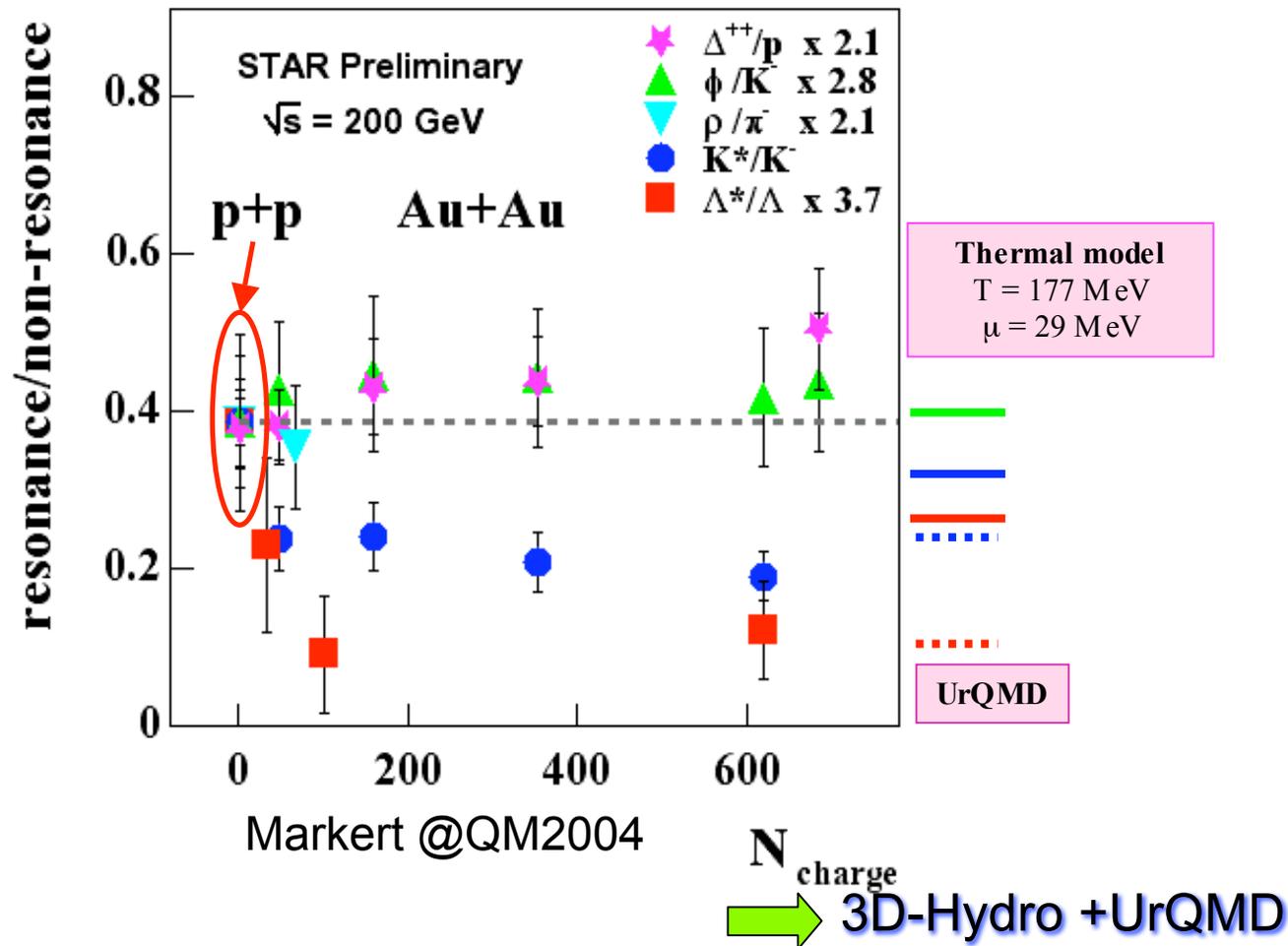
### Possible solutions:

- Partial chemical equilibrium (PCE)  
 Hirano, Kolb, Rapp
- Hydro + Micro Model

Bass, Dumitru, Teaney, Sushakov, [arXiv:1002.4885](#), AGS annual users' meeting

# Final State Interactions

2. In UrQMD final state interactions are included correctly.



# 3D-Hydro + UrQMD Model

Bass and Dumitru,  
PRC61,064909(2000)  
Teaney et al, nucl-th/0110037

## Key:

- Hadron phase: viscosity effect
- Freezeout process:
  - Chemical freezeout & thermal freezeout
  - Final state interactions
- 3D-Hydro + UrQMD
  - Treatment of freezeout is determined by mean free path.
  - Brake up thermalization: viscosity effect

## Full 3-d Hydrodynamics

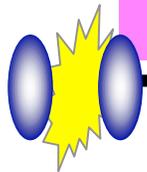
- EoS : 1st order phase transition  
QGP + excluded volume model

## Hadronization

Cooper-Frye  
formula  
Monte Carlo

## UrQMD

final state  
interactions



Chiho NONAKA

$T_C$ : critical temperature  $> T_{SW}$ : Hydro → UrQMD

RHIC & AGS annual users' meeting

# 3-D Hydrodynamic Model

- Relativistic hydrodynamic equation

$$\partial_\mu T^{\mu\nu} = 0 \quad T^{\mu\nu} : \text{energy momentum tensor}$$

- Baryon number conservation

$$\partial_\mu (n_B(T, \mu)) = 0$$

- Coordinates

$$(\tau, x, y, \eta) : \tau = \sqrt{t^2 - z^2}, \eta = \tanh^{-1} \left( \frac{z}{t} \right)$$

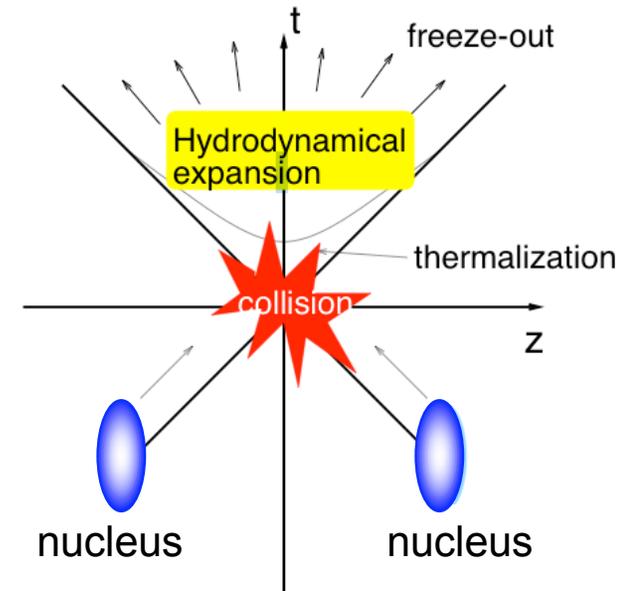
- Lagrangian hydrodynamics

- Tracing the adiabatic path of each volume element
- Effects of phase transition on observables
- Computational time
- Easy application to LHC

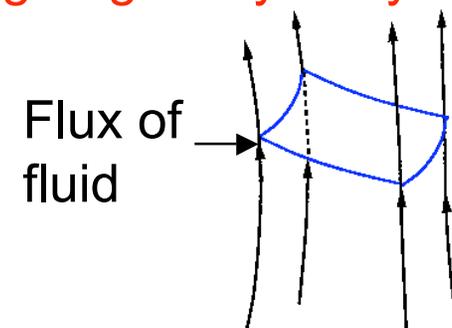
- Algorithm

- Focusing on the conservation law

$$\partial_\mu (s(T, \mu) u^\mu) = 0, \quad \partial_\mu (n_B(T, \mu) u^\mu) = 0$$



## Lagrangian hydrodynamics



# Parameters

## Initial Conditions

### – Energy density

$$\varepsilon(x, y, \eta) = \varepsilon_{\max} W(x, y; b) H(\eta)$$

### – Baryon number density

$$n_B(x, y, \eta) = n_{B\max} W(x, y; b) H(\eta)$$

### – Parameters

$$\left\{ \begin{array}{l} \tau_0 = 0.6 \text{ fm/c} \\ \varepsilon_{\max} = 40 \text{ GeV/fm}^3, n_{B\max} = 0.15 \text{ fm}^{-3} \\ \eta_0 = 0.5, \sigma_\eta = 1.5 \end{array} \right.$$

### – Flow

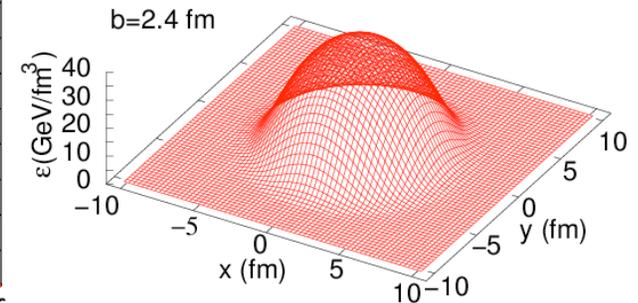
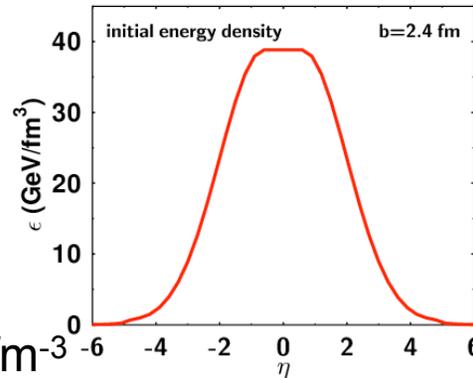
$$v_L = \eta \text{ (Bjorken's solution); } v_T = 0$$

## Switching temperature

$$T_{\text{SW}} = 150 \text{ [MeV]}$$

• longitudinal direction

• transverse plane

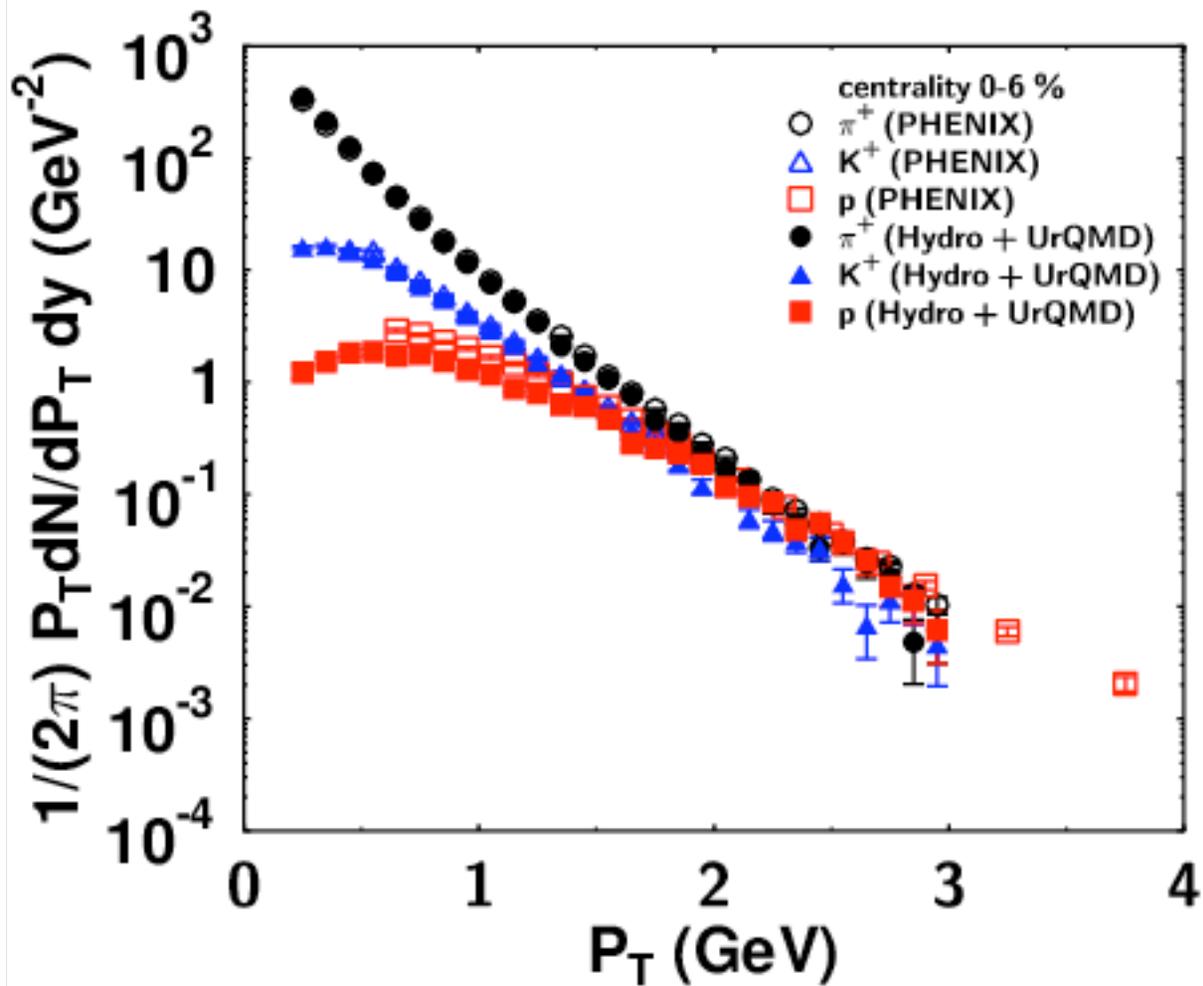


**Different from Pure Hydro !**

	hydro	Hydro+ UrQMD
$\tau_0$ (fm)	0.6	0.6
$\varepsilon_{\max}$ (GeV/fm <sup>3</sup> )	55	40
$n_{B\max}$ (fm <sup>-3</sup> )	0.15	0.15
$\eta_0, \sigma_\eta$	0.5, 1.5	0.5, 1.5

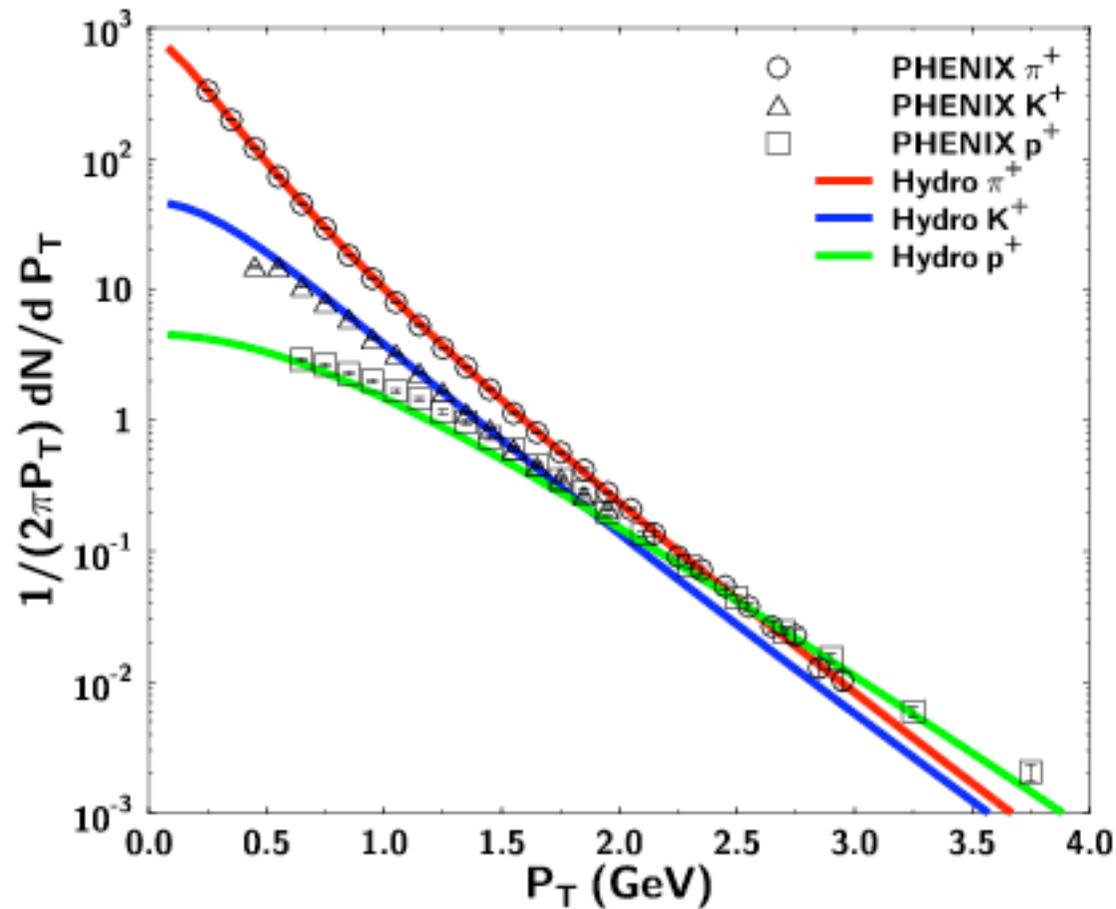
# $P_T$ spectra

- $P_T$  spectra at central collisions



# $P_T$ Spectra (Pure Hydro)

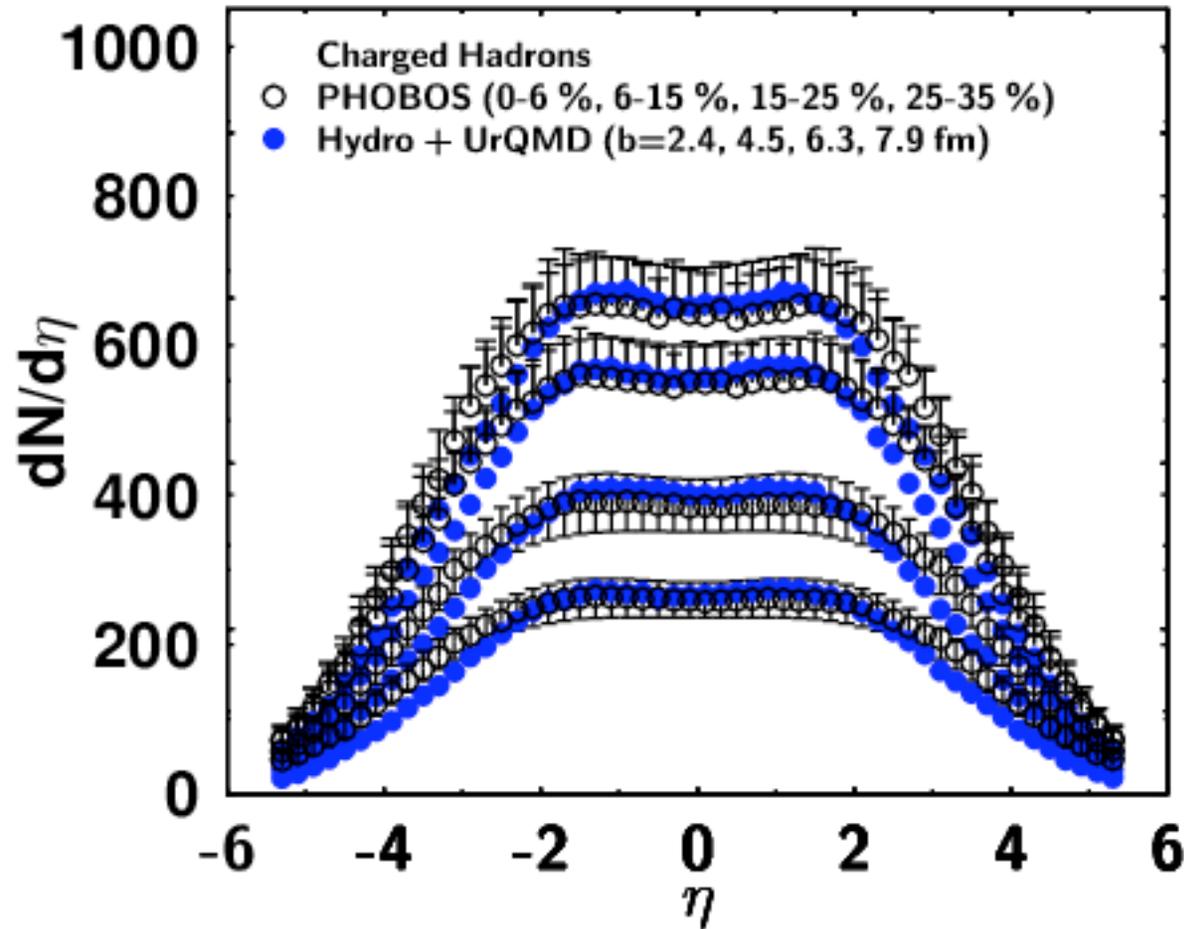
Au+Au, sqrt(s)=200 GeV



$T_f = 110$  MeV  
normalization of  $p$ :  
ratio at  $T_{\text{chem}}$   
Heinz and Kolb, hep-ph/0204061

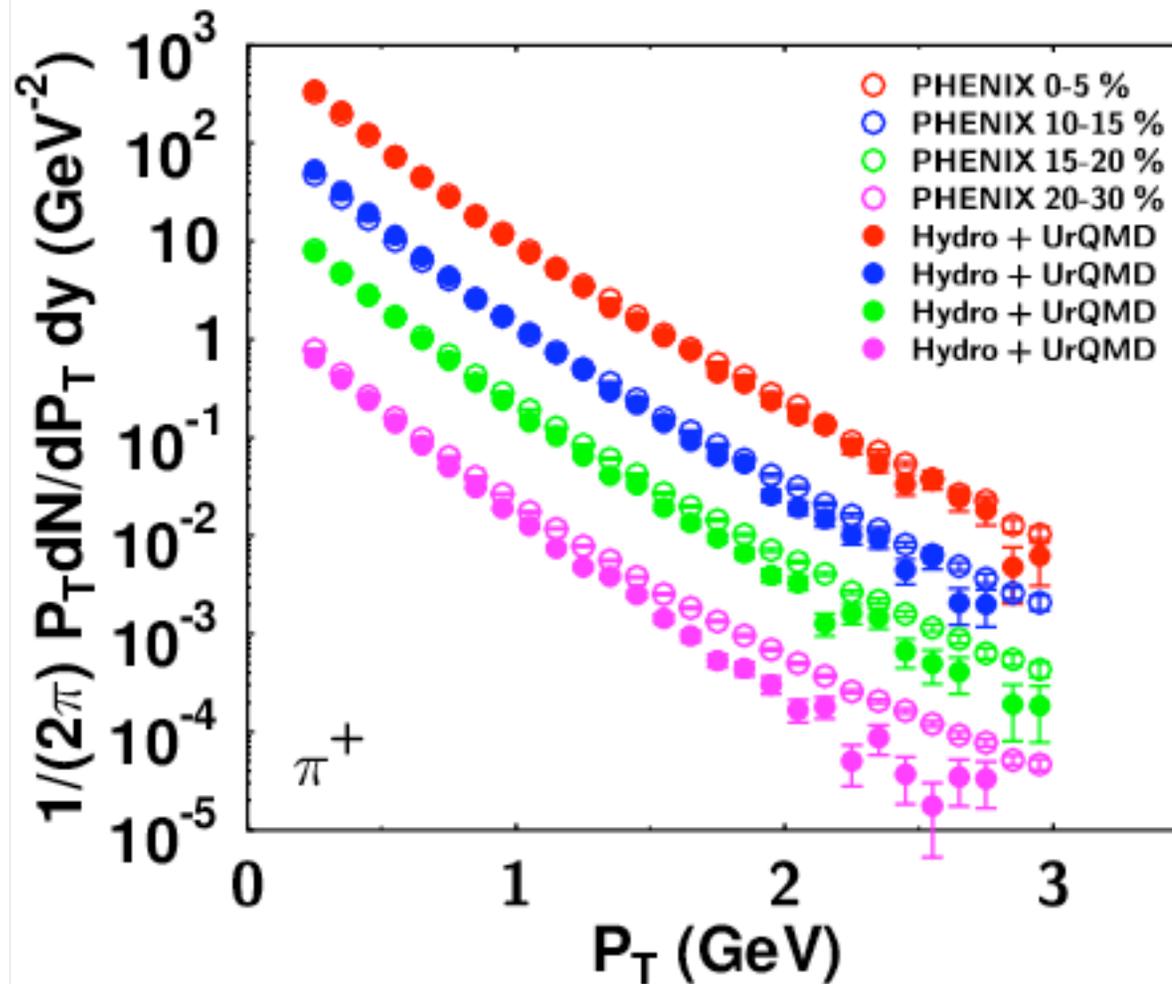
# Rapidity Distribution

- Impact parameter dependence of rapidity distributions



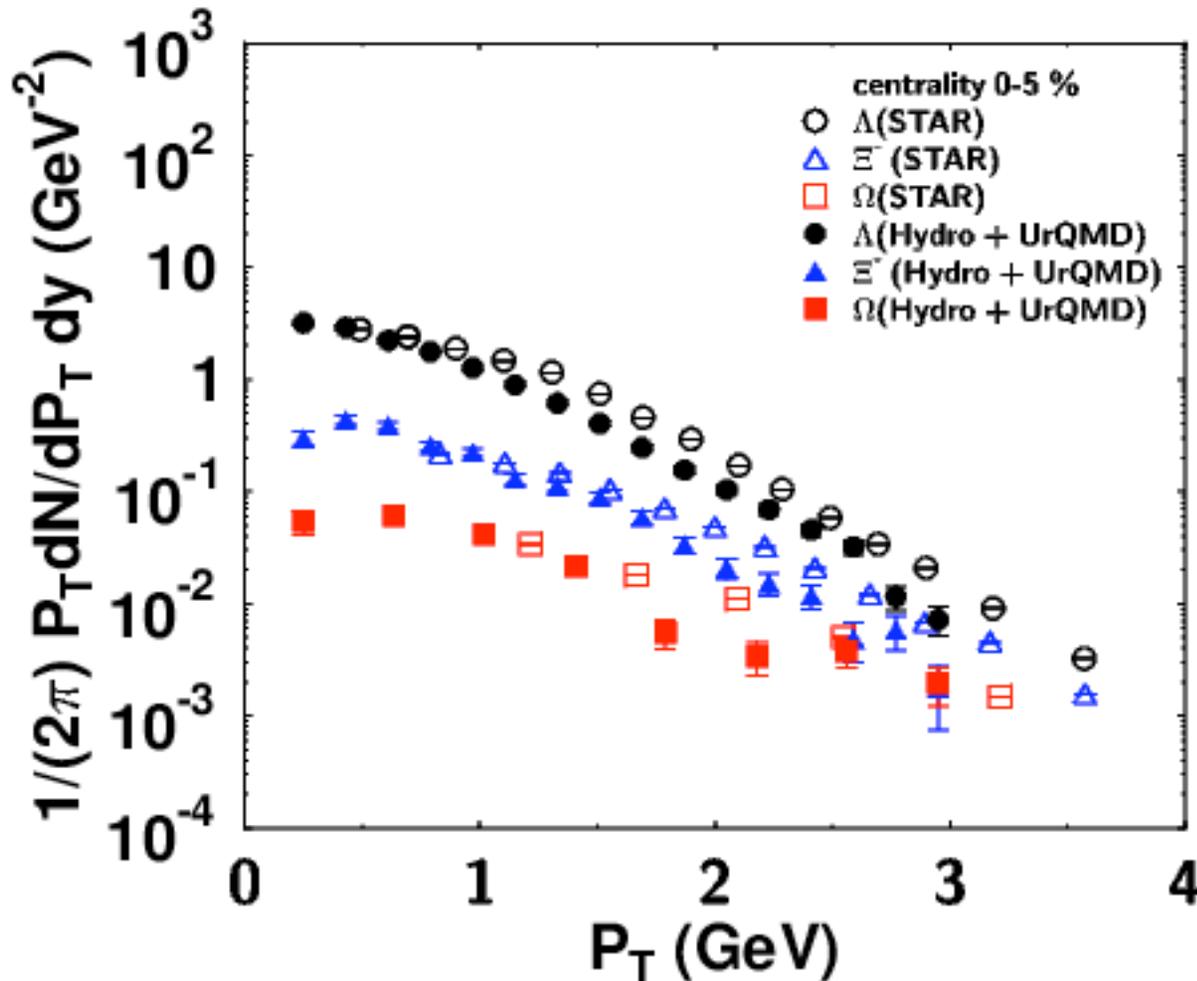
# Centrality Dependence

- Impact parameter dependence of  $P_T$



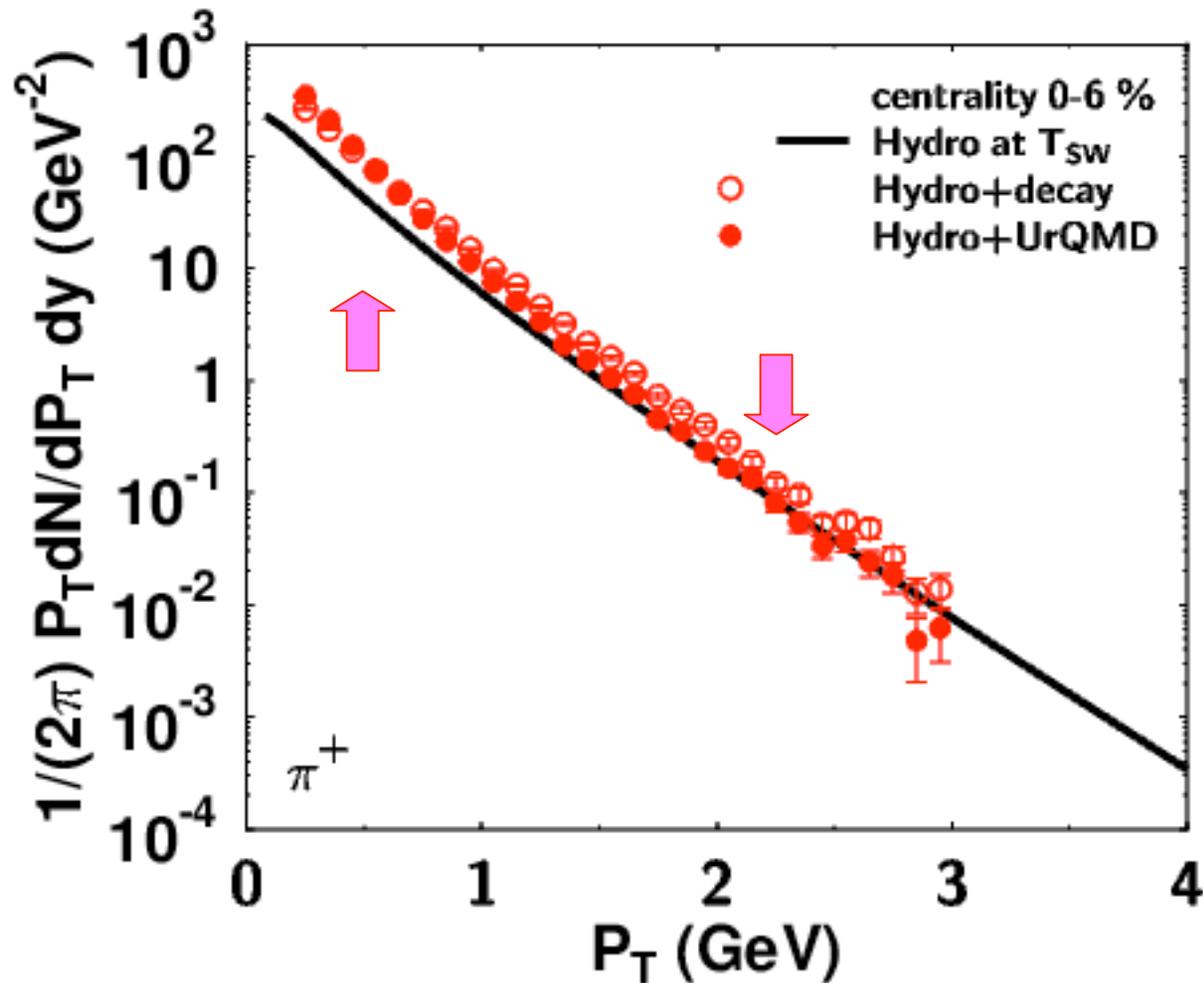
# $P_T$ Spectra for Strange Particles

Normalization is perfect!



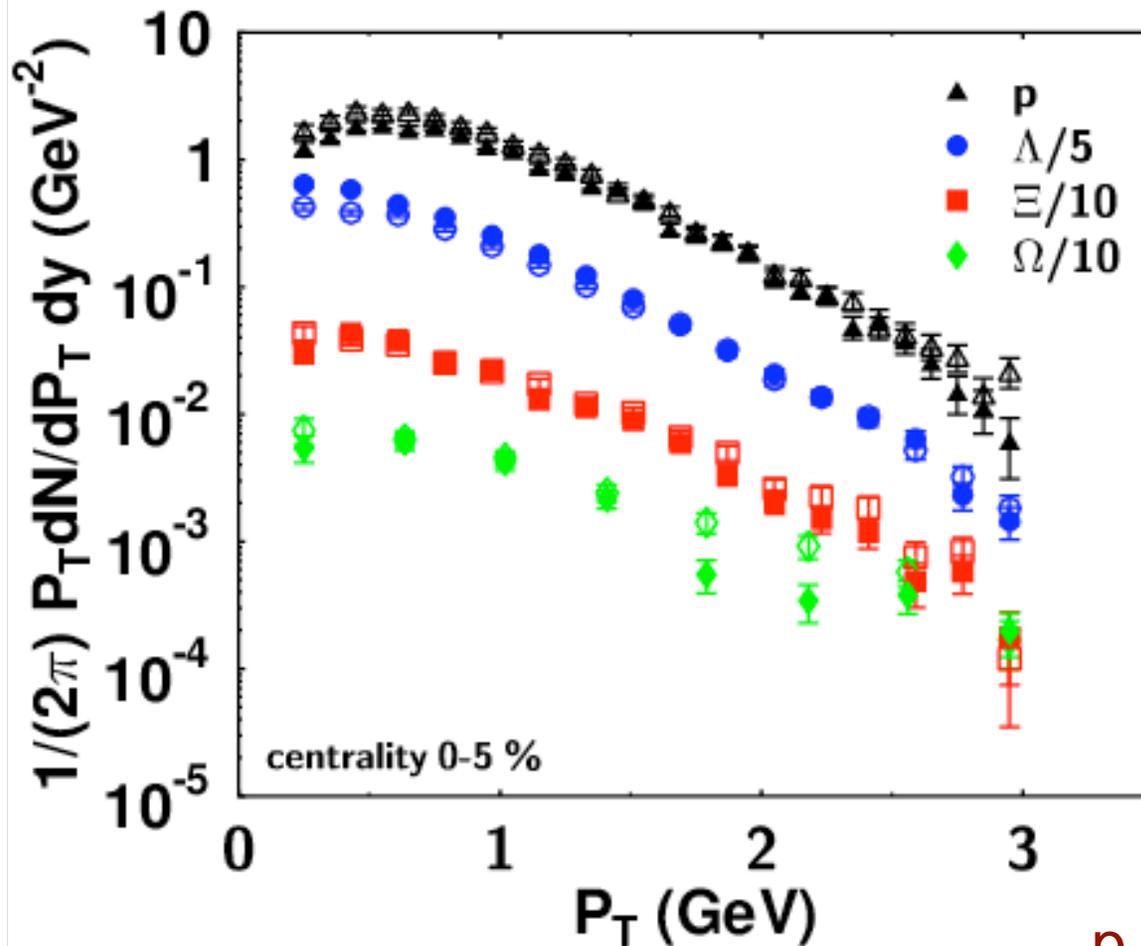
# Reaction Dynamics

- At mid rapidity



- Slope becomes steeper

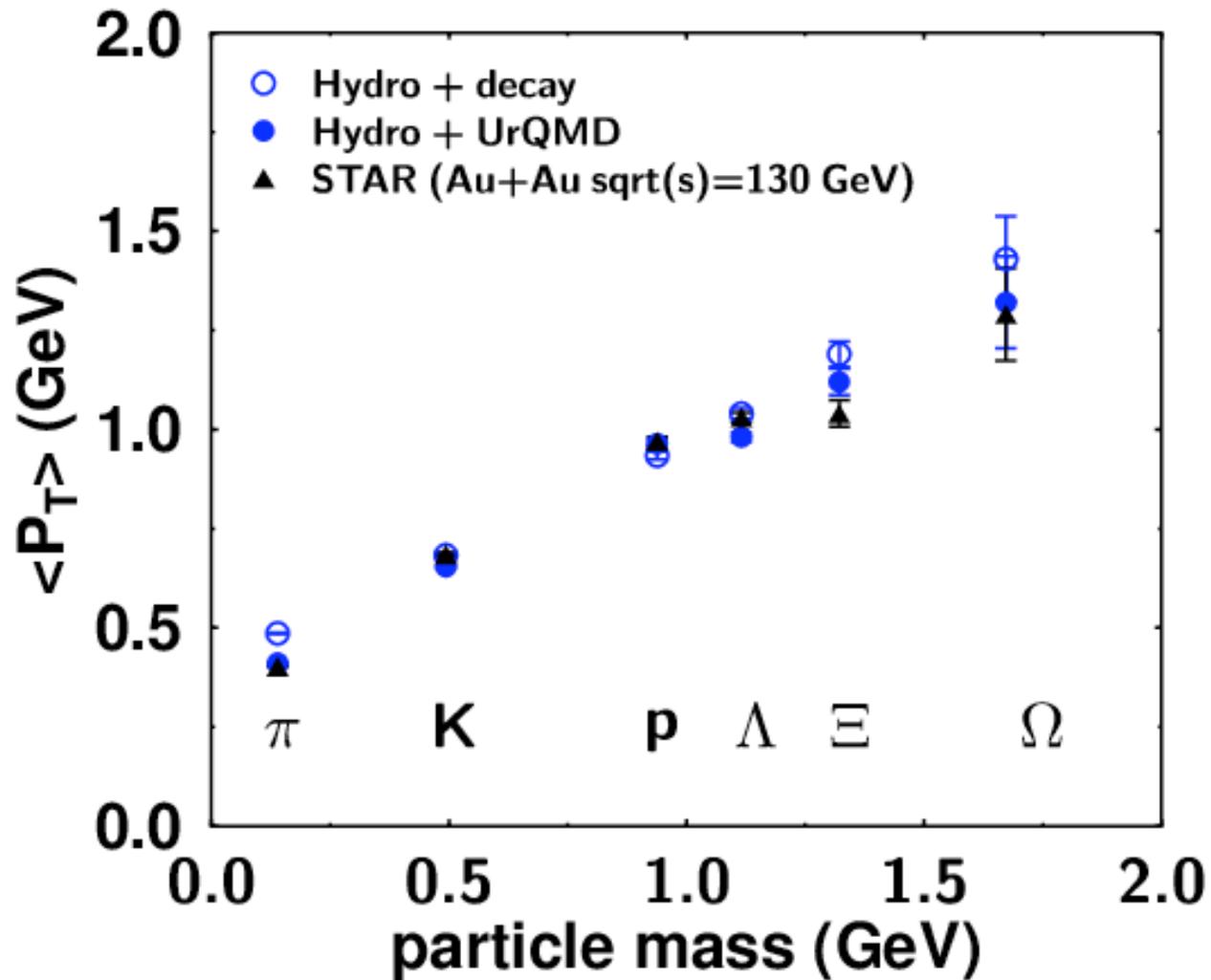
# Final State Interactions



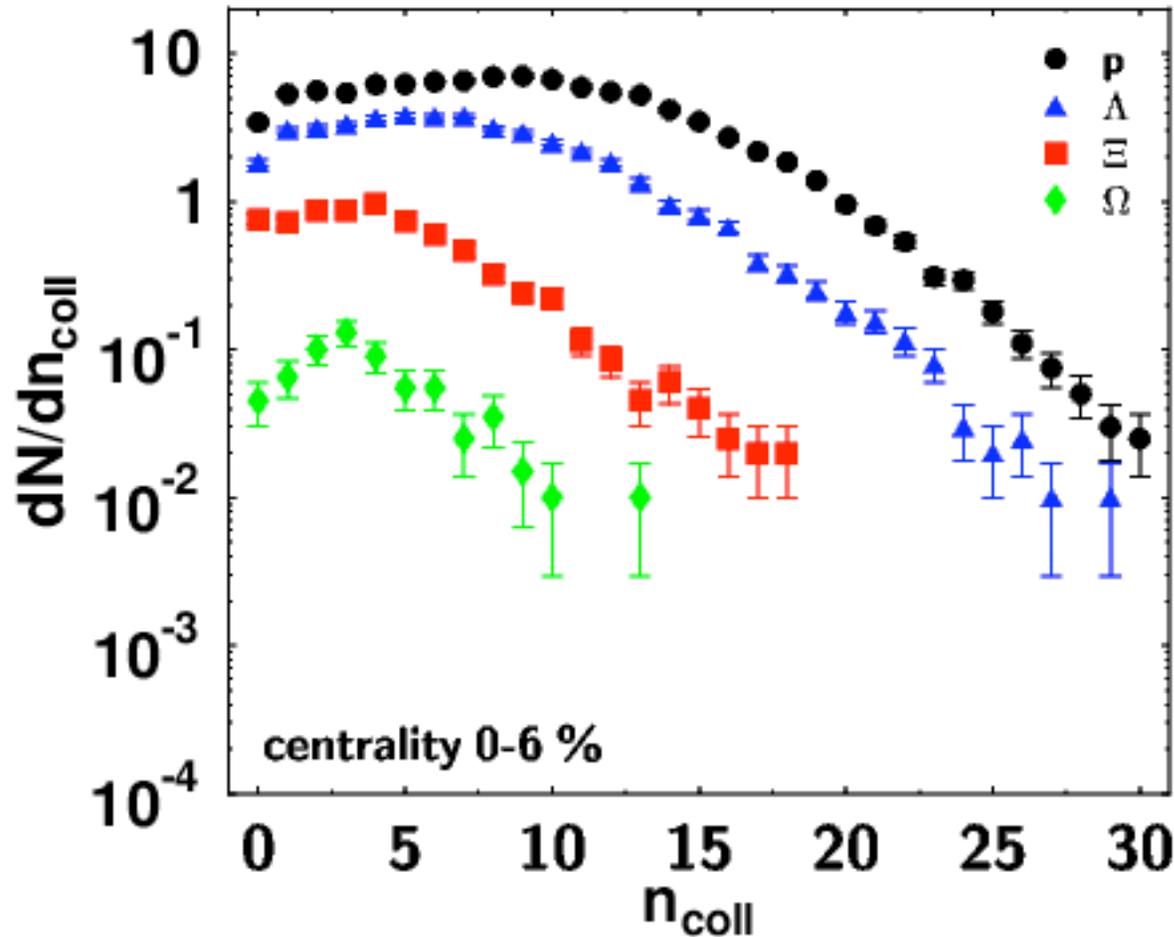
$p, \Lambda$  : flatter, pion wind  
 $\Xi, \Omega$ : small cross section

# $\langle P_T \rangle$ vs mass

- At mid rapidity

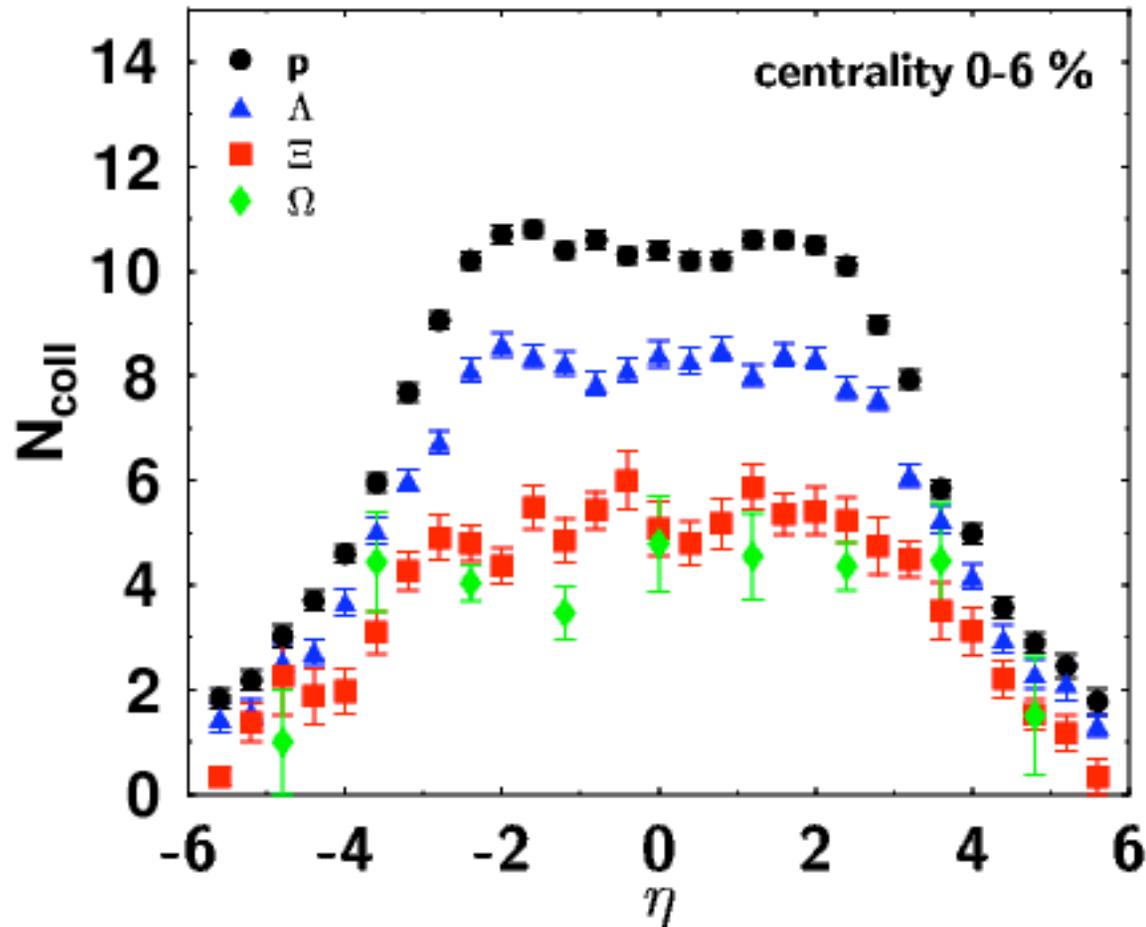


# Distribution of # of Collisions



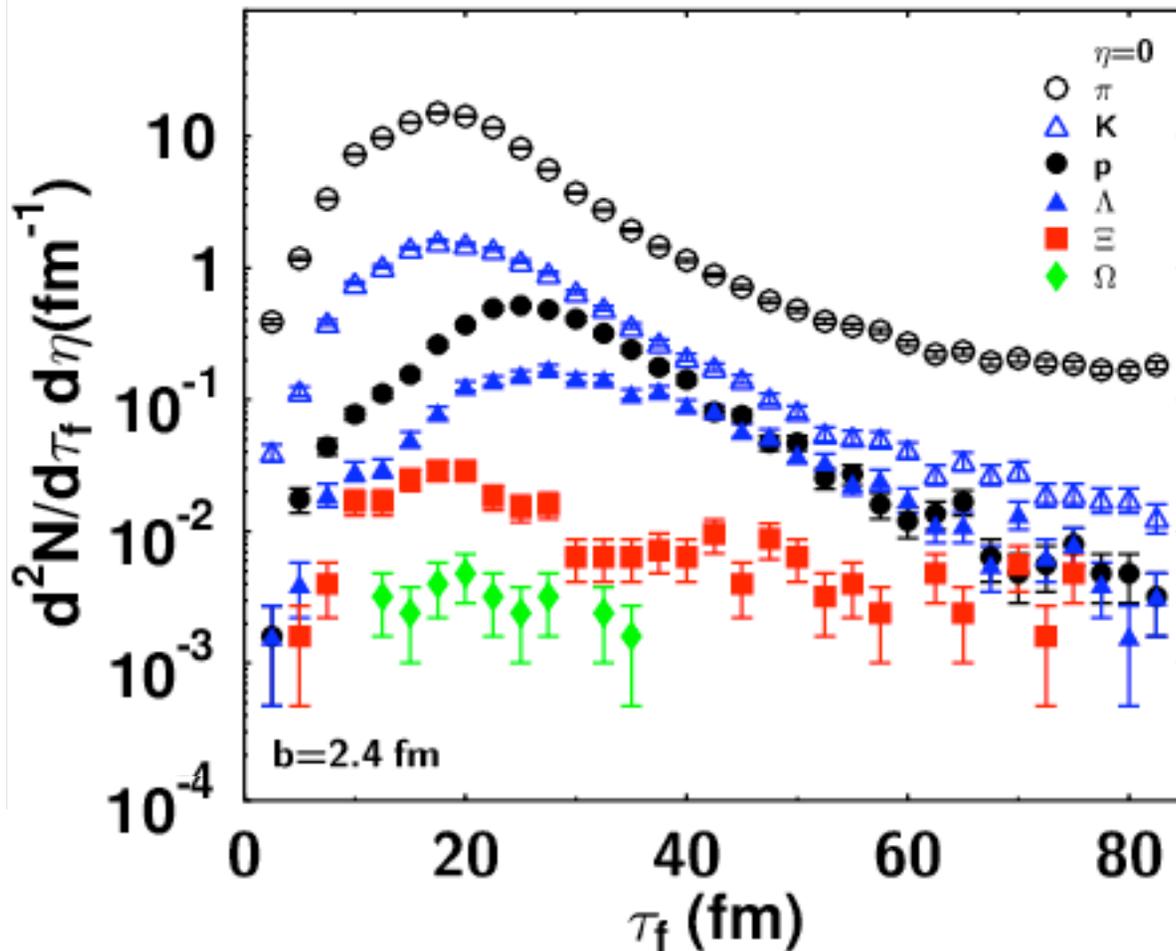
- $p, \Lambda$  broad  
 $p \sim 10$  times,  $\Lambda \sim 7$  times
- $\Xi, \Omega$  small cross section

# Distribution of # of Collisions



- plateau  
-3 <  $\eta$  < 3
- flavor difference

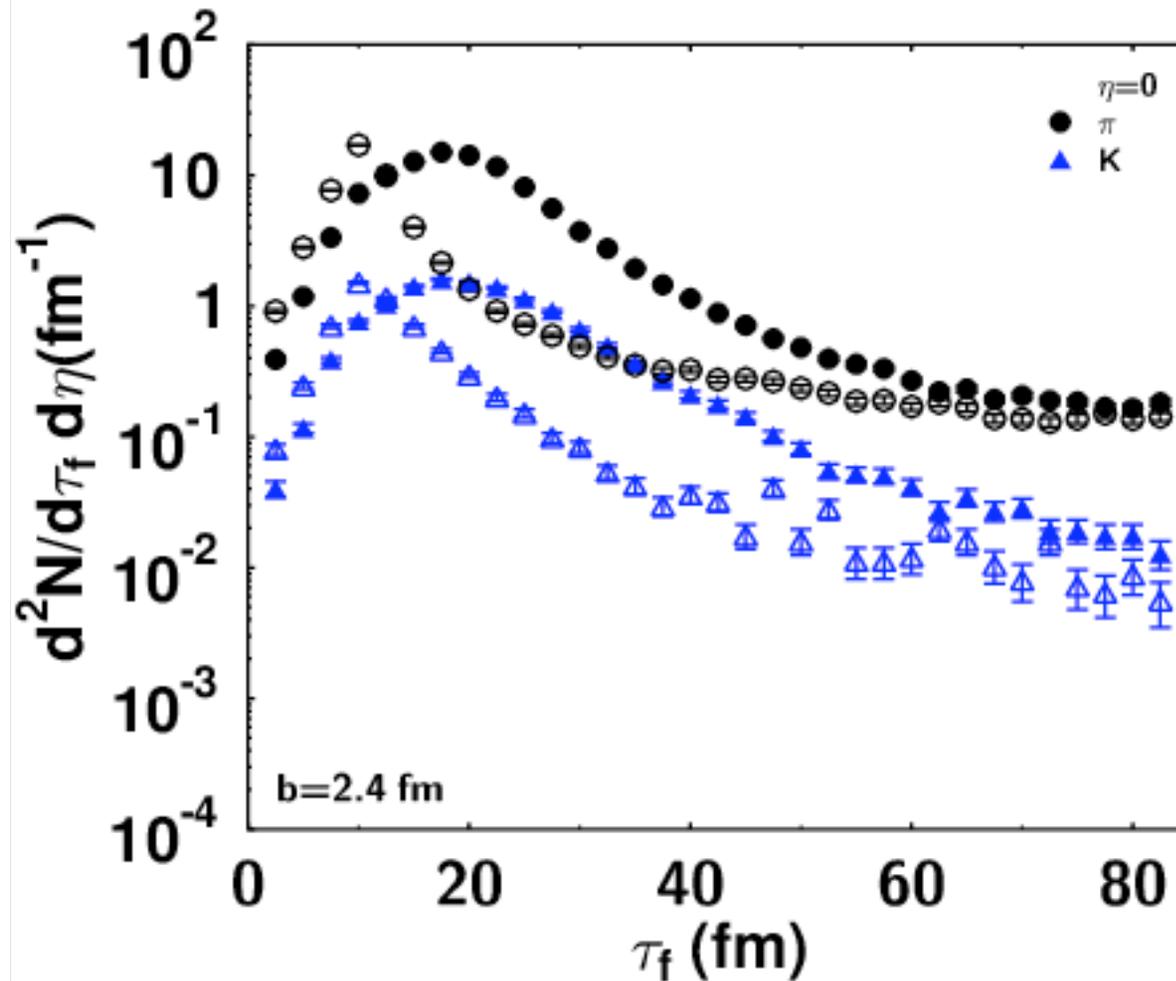
# $\tau_f$ Distribution



- $\pi$ , K: peak  $\sim 19$  fm
- p,  $\Lambda$ : peak  $\sim 22$  fm
- Multistrange particles small

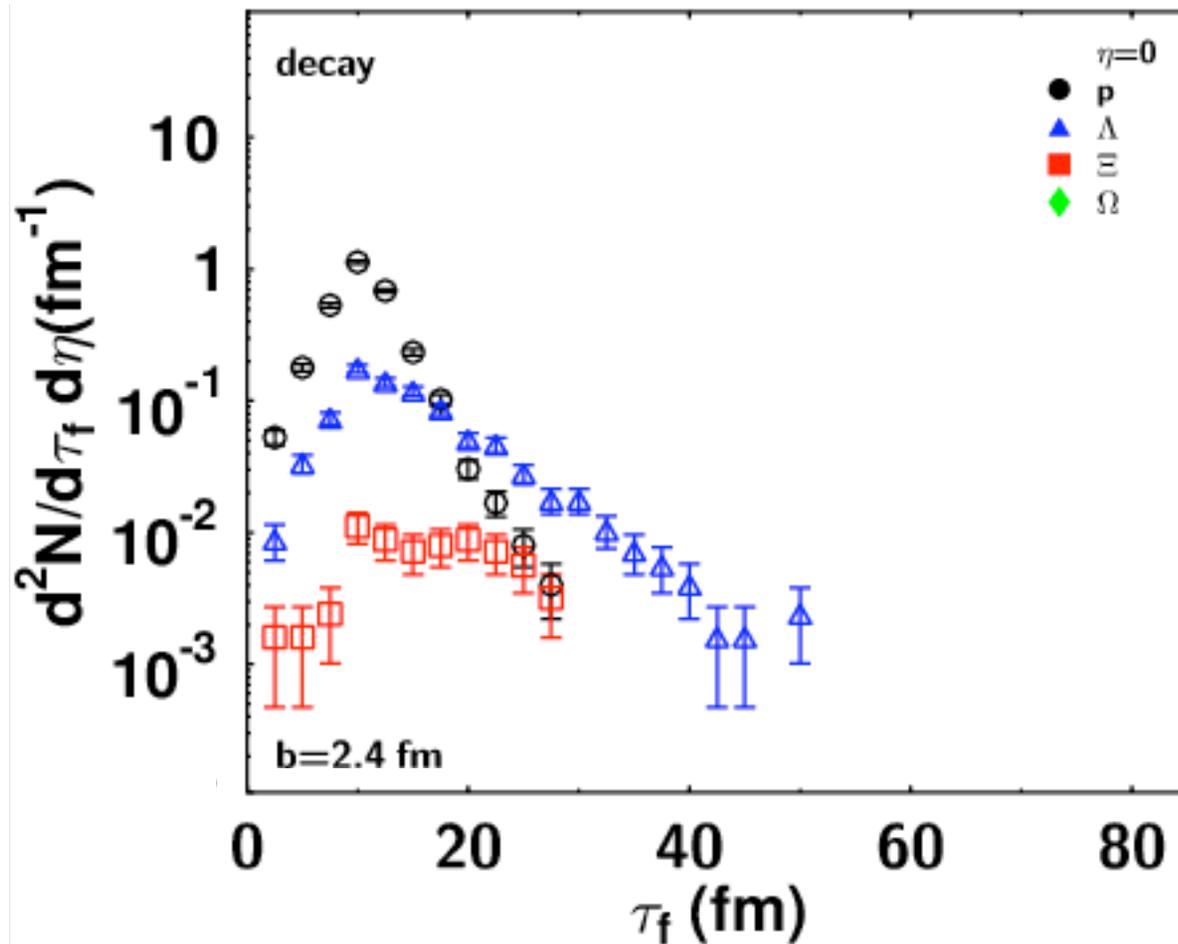
- Species dependence
- Broad distribution

# $\tau_f$ Distribution of $M$



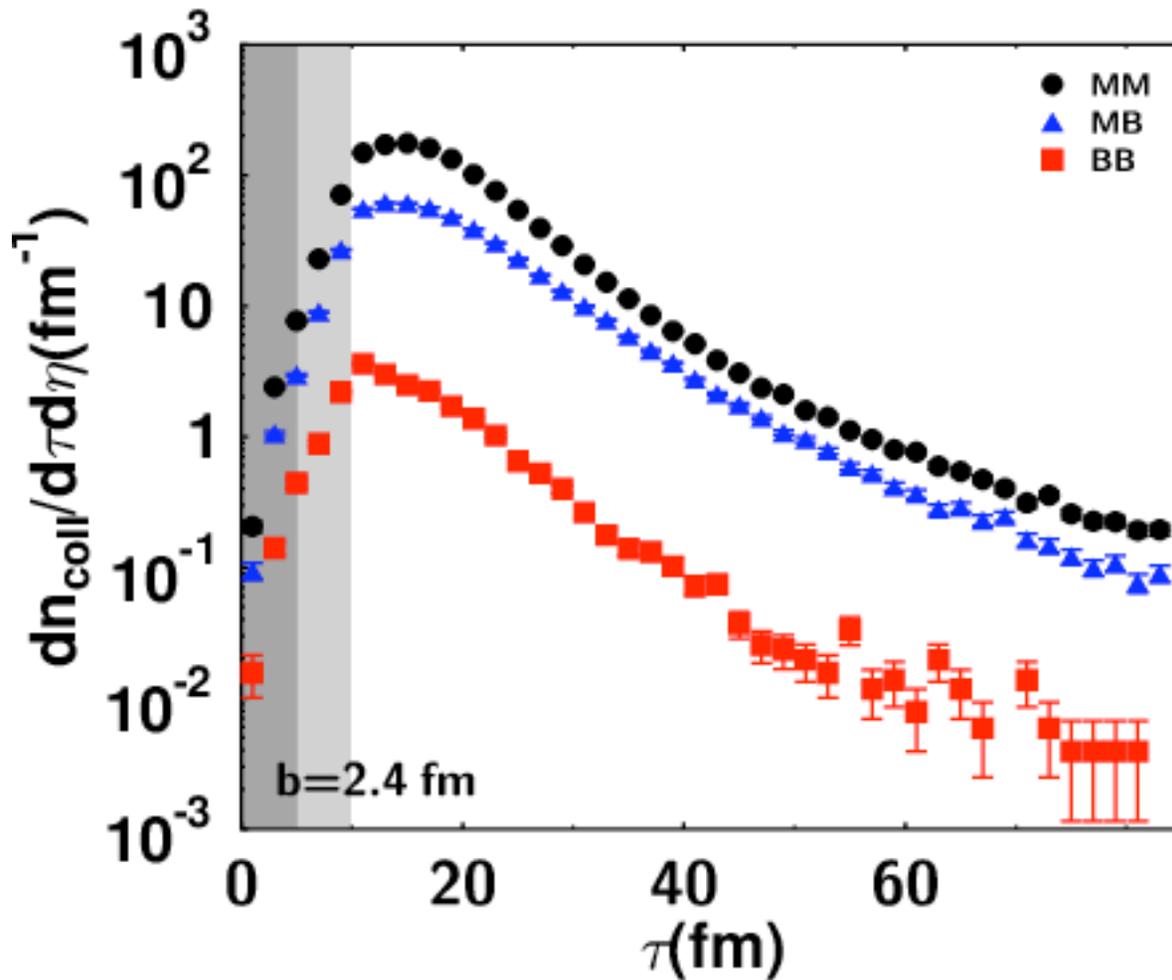
- Final state interactions  
↓  
Duration of freezeout process

# $\tau_f$ Distribution of $B$



- Final state interactions  
↓  
Duration of freezeout process

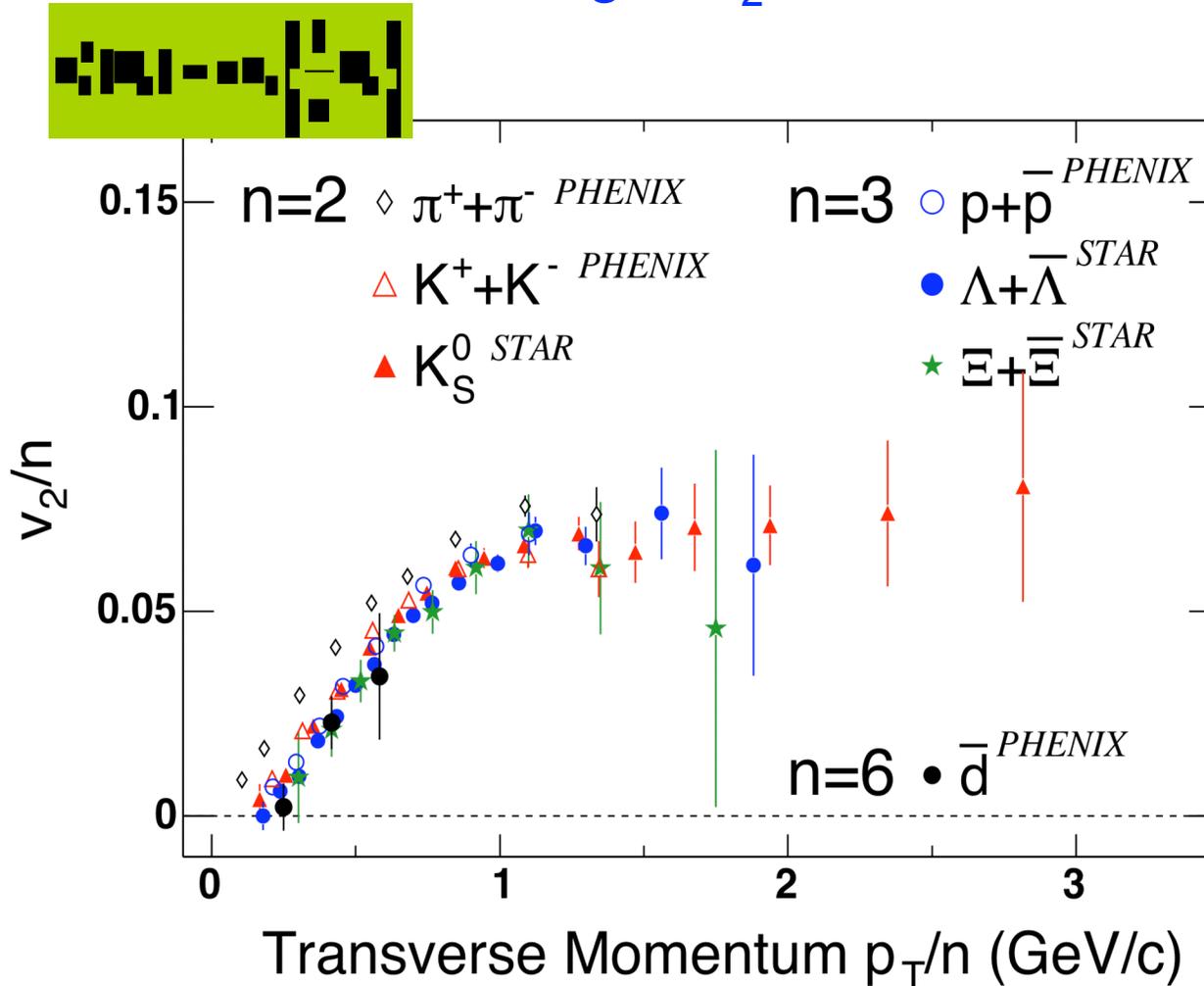
# Collision Rate



•MM is dominant.

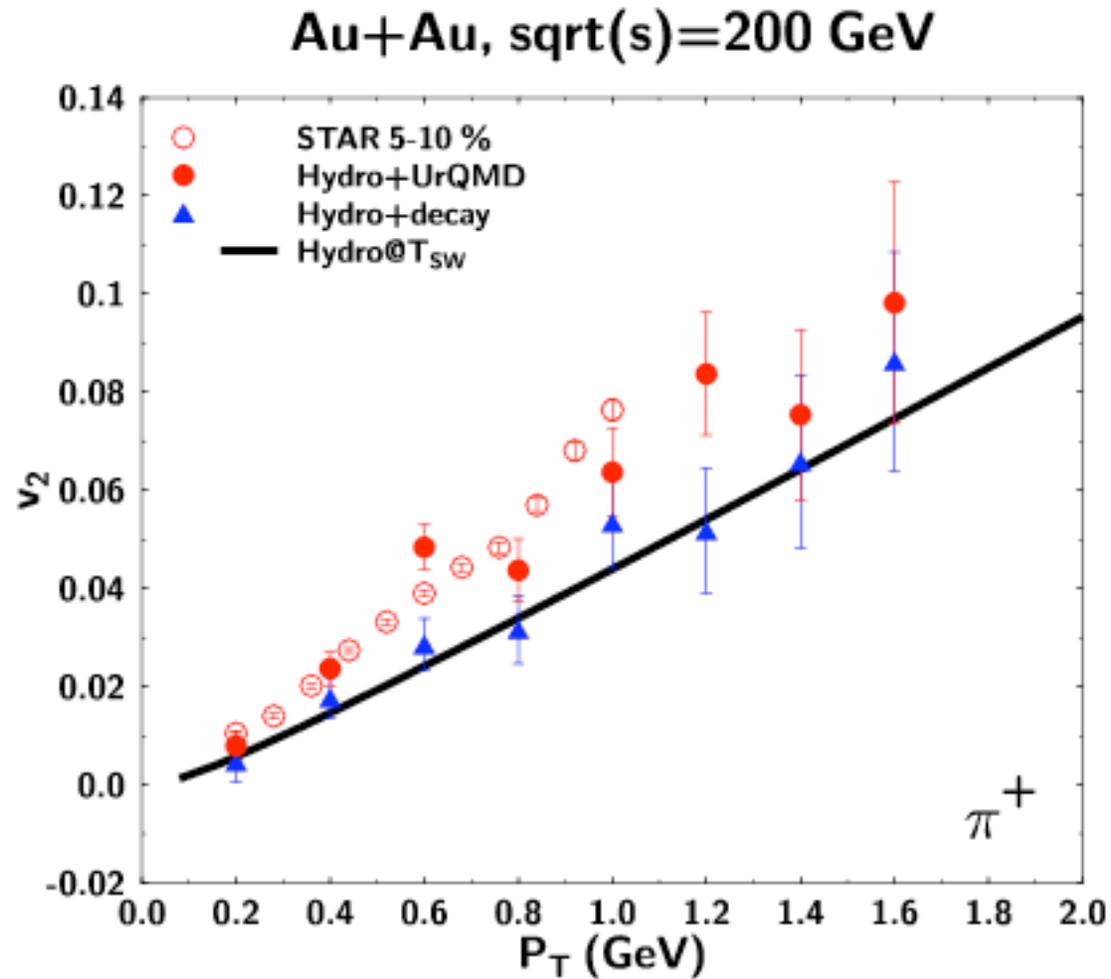
# $v_2$ in hadron phase ?

- Quark number scaling of  $v_2$



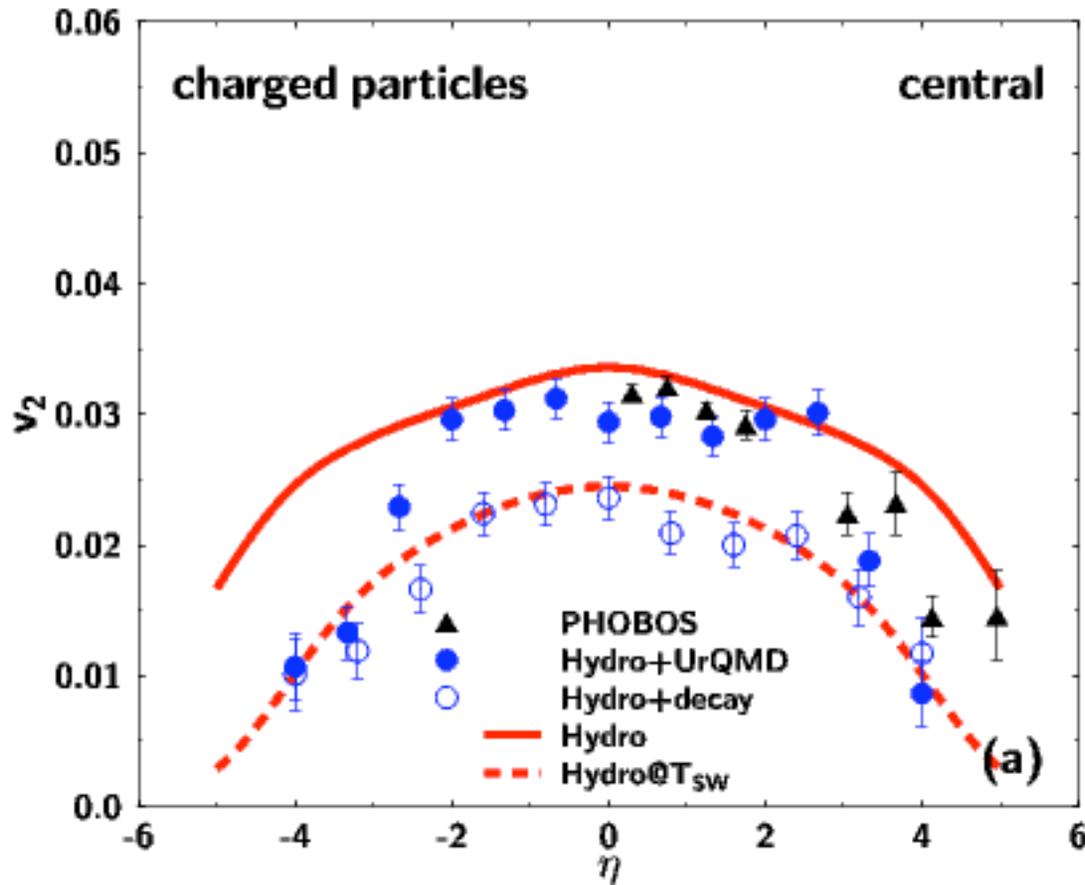
$v_2$ : early stage of expansion

# Reaction Dynamics in $v_2$ I



# Reaction Dynamics in $v_2$ II

Au+Au, sqrt(s)=200 GeV



- Hydro+decay  
~ Hydro@ $T_{sw}$
- $v_2$  grows in hadron phase a bit.
- $v_2$  builds up in QGP phase.

# Summary

- We present the 3-D hydrodynamic +cascade model
- 3-D Hydrodynamic Model
  - Single particle distribution
    - Centrality dependence
  - Elliptic flow
  - Low  $T_f$ : ✓single spectra, elliptic flow, ✗hadron ratios
    - Necessity of improvement of freezeout process in Hydro
- 3-D Hydro + UrQMD
  - Single particle distribution
    - Centrality dependence
  - Elliptic flow
  - Different initial conditions from pure Hydro
  - Hadron ratios ←Switching temperature from Hydro to UrQMD
  - Reaction dynamics in UrQMD
    - $\Xi, \Omega$ :small cross section,  $v_2$ :improvement at forward/backward  $\eta$
- Work in progress
  - EoS dependence: ex. lattice QCD
  - Switching temperature dependence