

Physics in Electron-Ion Collider Experiments

II: From Factors and Parton Distributions

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Huada School on QCD 2016: QCD in the EIC Era , May 23 – June 3, 2016

- Electron Scattering
- Elastic Scattering: From Factors
Surprise: G_E^p @ high Q^2 : proton shape, 2- γ exchange
Proton radius puzzle
- Deep-Inelastic Scattering:
Unpolarized Structure Functions \rightarrow Parton Distribution Functions
High-x physics
Sea asymmetry

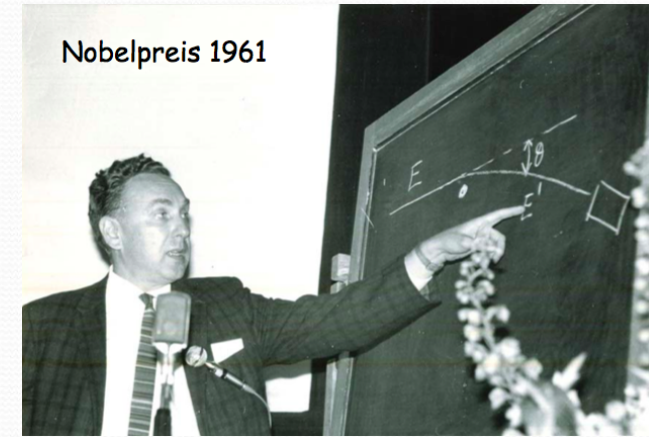
Electron Scattering

A Clean Probe To Study Nucleon Structure and QCD

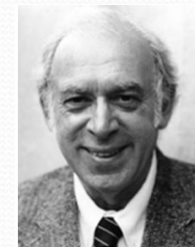
Electron Scattering and Nucleon Structure

- Clean probe to study nucleon structure
only electro-weak interaction, well understood
- Elastic Electron Scattering: Form Factors
→ 60s: established nucleon has structure (Nobel Prize)
electrical and magnetic distributions
- Resonance Excitations
→ internal structure, rich spectroscopy (new particle search)
constituent quark models
- Deep Inelastic Scattering
→ 70s: established quark-parton picture (Nobel Prize)
parton distribution functions (PDFs)
polarized PDFs : spin Structure
TMDs, GPDs: 3-d structure:

Factorization: observable $A \sim H \otimes S$



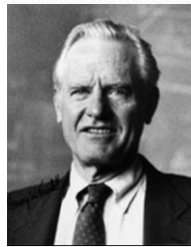
Robert Hofstadter,
Nobel Prize 1961



J.T. Friedman



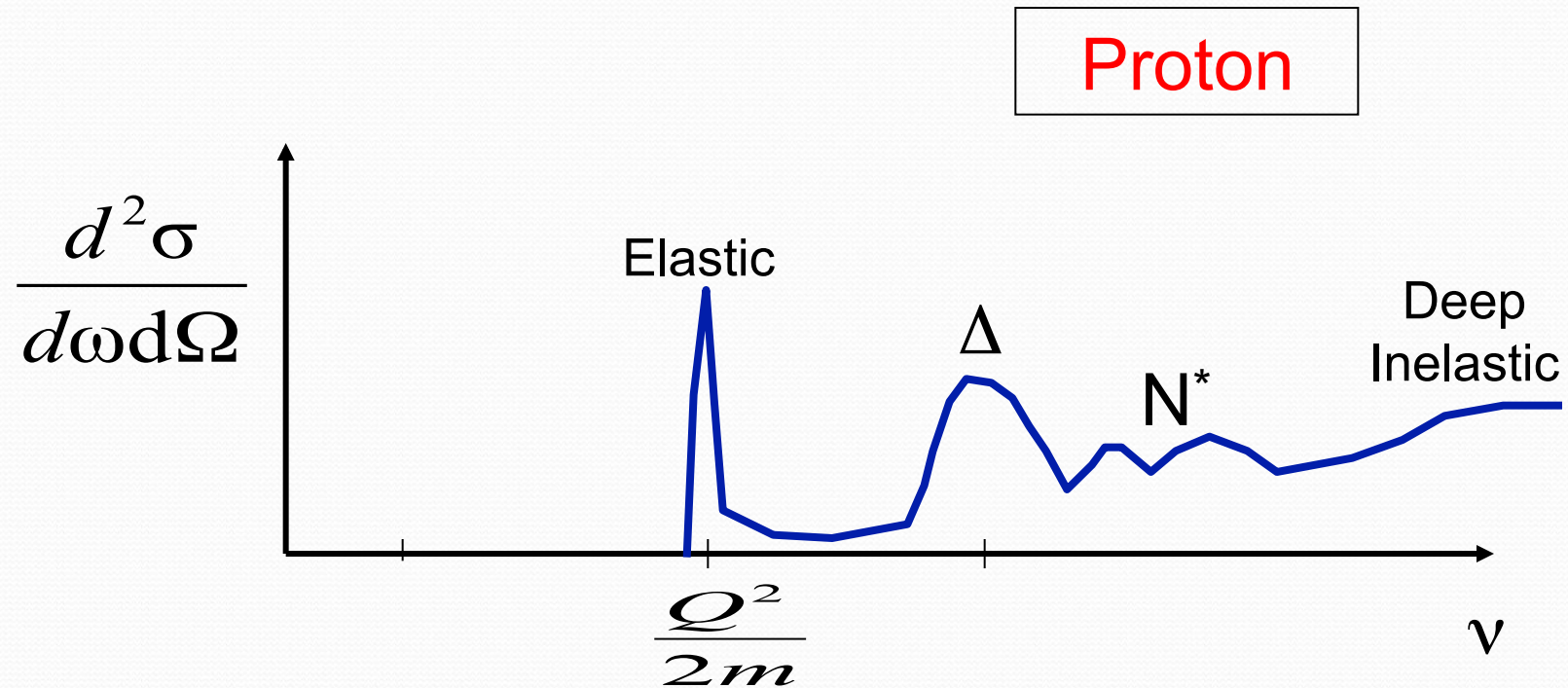
R. Taylor



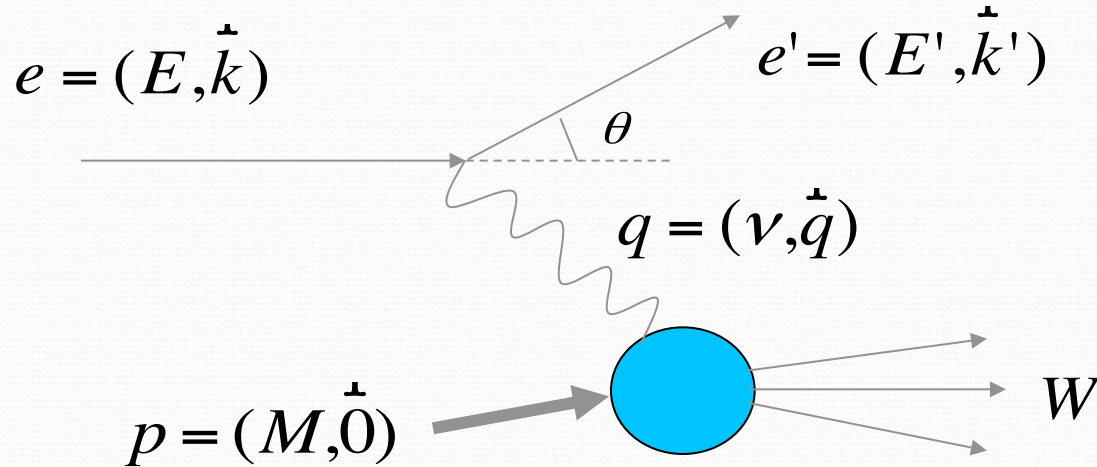
H.W. Kendall

Nobel Prize 1990

Typical Electron Scattering Spectra at Fixed Q^2



Inclusive Electron Scattering



4-momentum transfer squared

$$Q^2 = -q^2 = 4EE' \sin^2 \frac{\theta}{2}$$

Invariant mass squared

$$W^2 = M^2 + 2M\nu - Q^2$$

Unpolarized:

$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_M \left[\frac{1}{\nu} F_2(\nu, Q^2) + \frac{2}{M} F_1(\nu, Q^2) \tan^2 \frac{\theta}{2} \right]$$

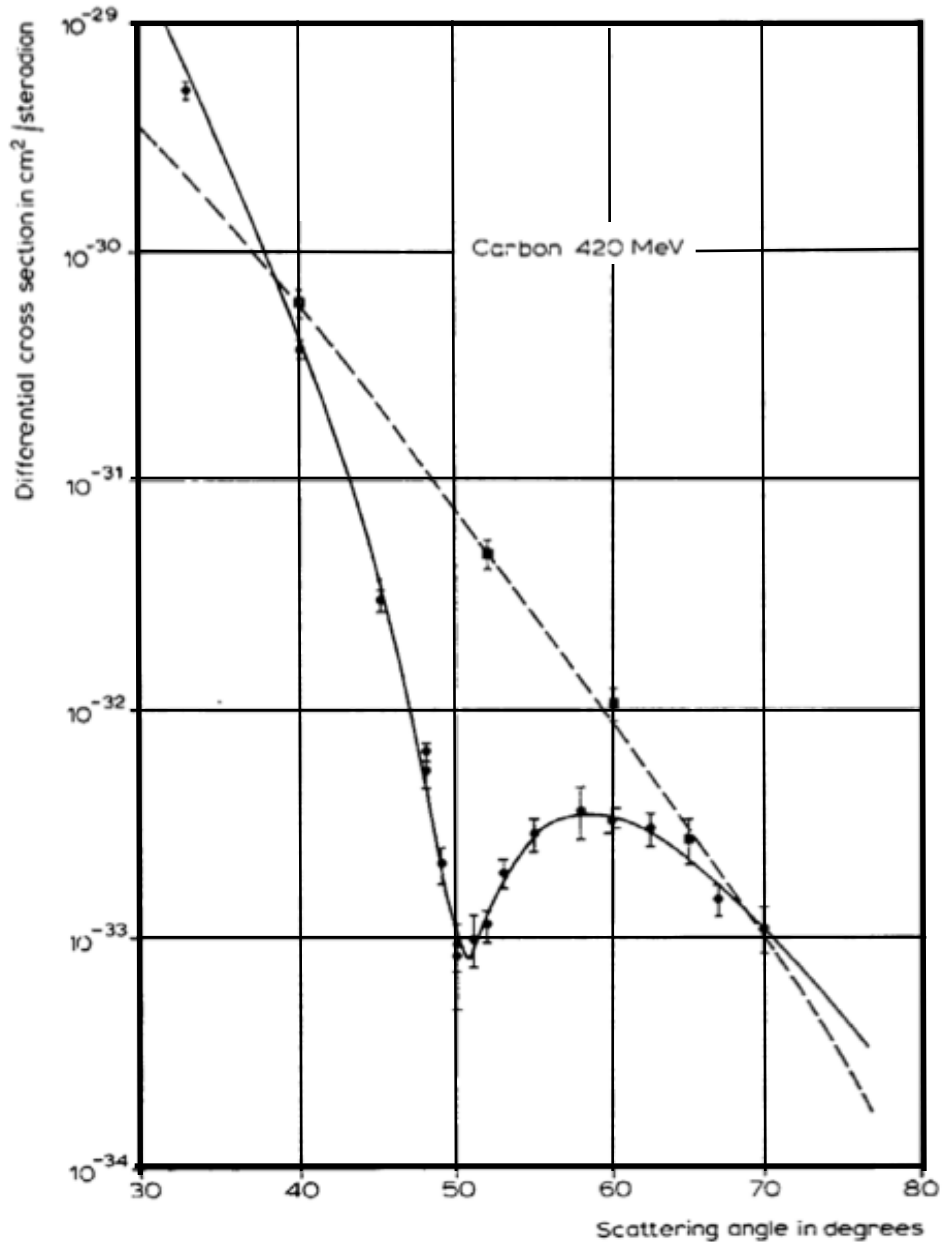
$$\sigma_M = \frac{\alpha^2 E' \cos^2(\theta/2)}{4E^3 \sin^4(\theta/2)}$$

F_1 and F_2 : information on the nucleon/nuclear structure

Nucleon Form Factors

Charge and Magnetization Distributions

Elastic Electron Scattering



Robert Hofstadter,
Nobel Prize 1961



Scattering cross section of nuclei:

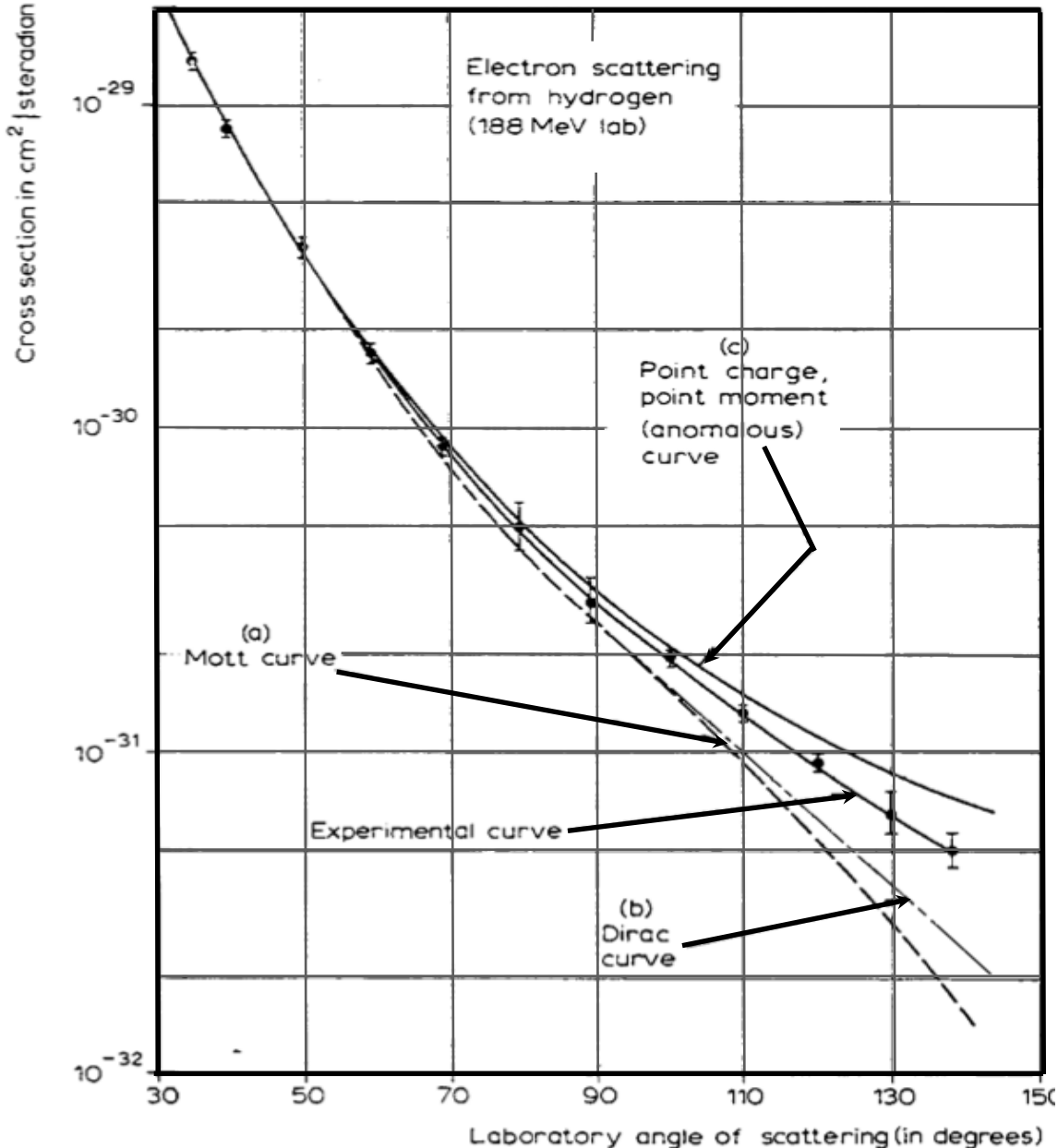
$$\frac{d\sigma}{d\Omega} = \frac{d\sigma}{d\Omega} \Big|_{\text{Ruth.}} \frac{E'}{E} \cos^2 \frac{\theta}{2} |F(q^2)|^2$$

Structure reflects finite charge radius,
through Fourier transform, of ~ 4 fm.

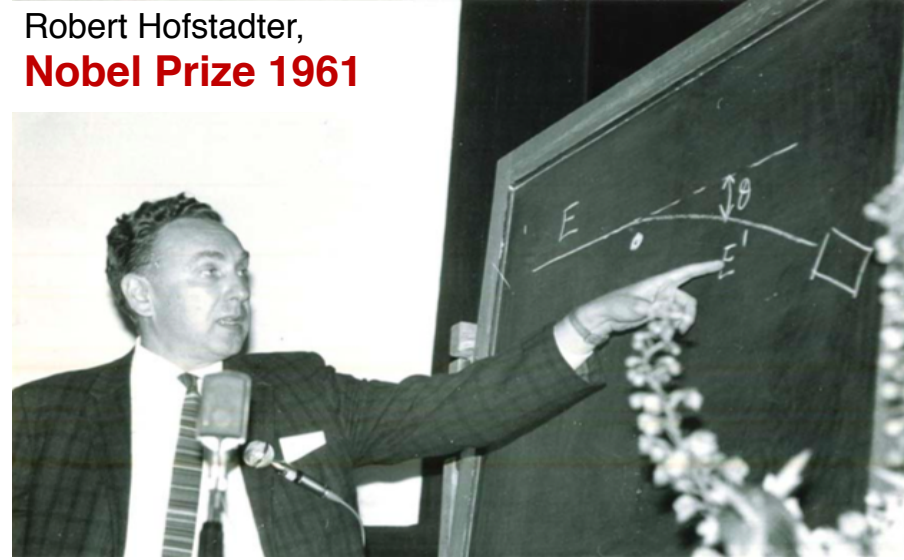
Elastic Electron Scattering

~200 MeV

Discovery: Proton Has Structure



Robert Hofstadter,
Nobel Prize 1961



Scattering off a spin-1/2 Dirac particle:

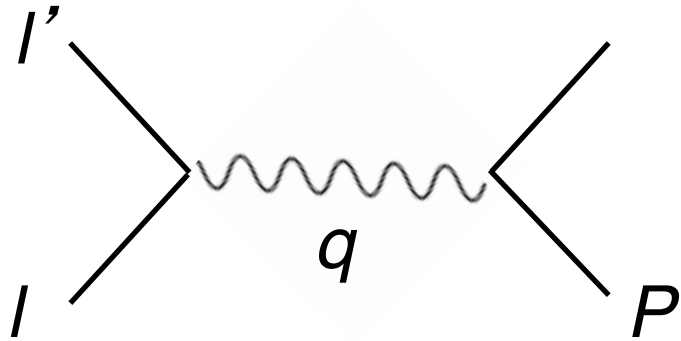
$$\frac{d\sigma}{d\Omega} = \left(\frac{\alpha}{4ME \sin^2(\theta/2)} \right)^2 \frac{E'}{E} \left[\frac{q^2}{2M} \sin^2(\theta/2) + \cos^2(\theta/2) \right]$$

The proton has an anomalous magnetic moment,

$$g_p \neq 2, \quad g_p \simeq 5.6$$

and, hence, internal (spin) structure.

Elastic Electron Scattering



$$d\sigma \propto \langle |\mathcal{M}|^2 \rangle = \frac{g_e^4}{q^4} L_{\text{lepton}}^{\mu\nu} K_{\mu\nu \text{ nucleon}}$$

The lepton tensor is calculable:

$$L_{\text{lepton}}^{\mu\nu} = 2 (k^\mu k'^\nu + k^\nu k'^\mu + g^{\mu\nu} (m^2 - k \cdot k'))$$

The nucleon tensor is not; it's general (spin-independent, parity conserved) form is:

$$K_{\mu\nu \text{ nucleon}} = -K_1 g_{\mu\nu} + \frac{K_2}{M^2} p_\mu p_\nu + \frac{K_4}{M^2} q_\mu q_\nu + \frac{K_5}{M^2} (p_\mu q_\nu + p_\nu q_\mu)$$

Charge conservation at the proton vertex reduces the number of structure functions:

$$q_\mu K_{\text{nucleon}}^{\mu\nu} \rightarrow K_4 = f(K_1, K_2), \quad K_5 = g(K_2)$$

and one obtains the Rosenbluth form, with electric and magnetic form factors:

$$\frac{d\sigma}{d\Omega} = \left(\frac{\alpha}{4ME \sin^2(\theta/2)} \right)^2 \frac{E'}{E} [2K_1 \sin^2(\theta/2) + K_2 \cos^2(\theta/2)], \quad K_{1,2}(q^2)$$

Elastic Scattering on a Proton

From relativistic quantum mechanics one can derive the the formula electron-proton scattering where one has assumed the exchange of a single virtual photon.

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \cdot \frac{E'}{E} \left[\frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2 \frac{\theta}{2} \right]$$

where G_E and G_M form factors take into account the finite size of the proton.

$$G_E = G_E(Q^2), G_M = G_M(Q^2); G_E(0)=1, G_M(0) = \mu_p$$

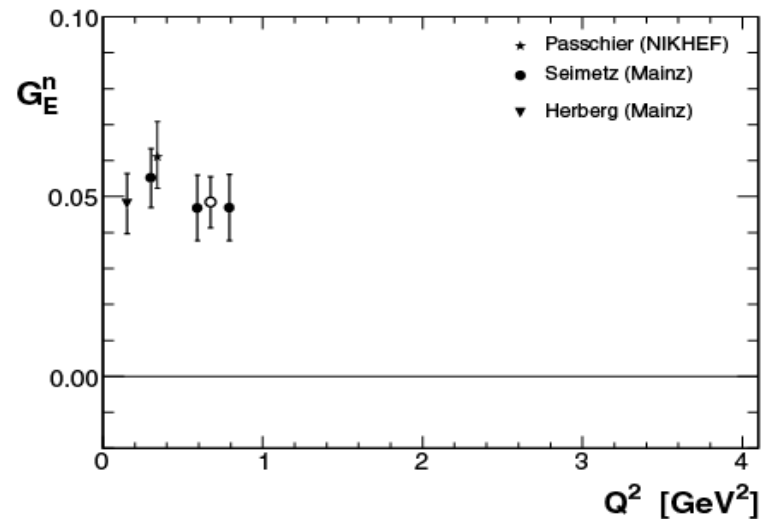
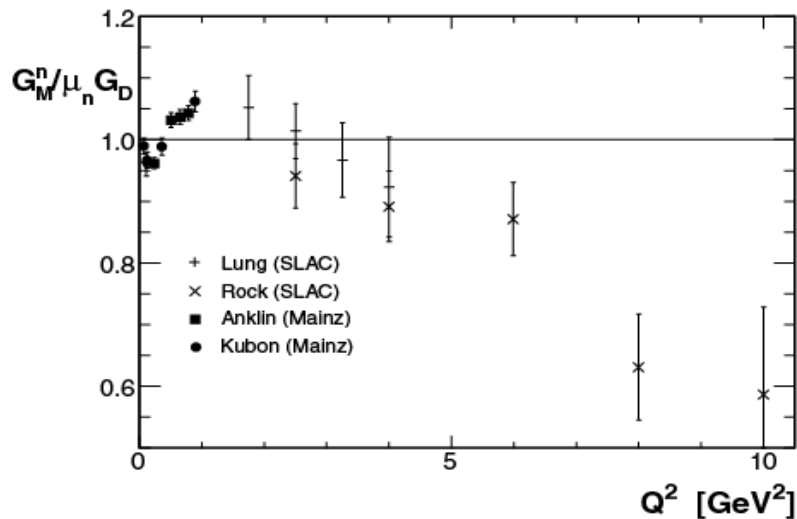
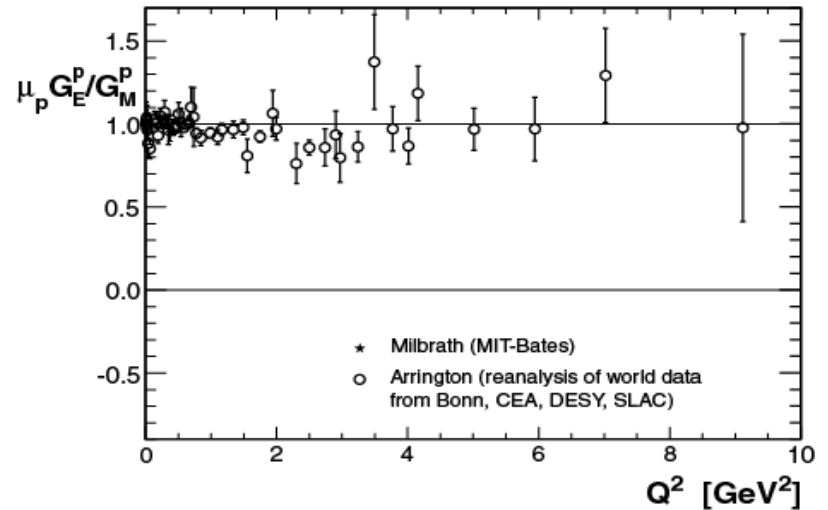
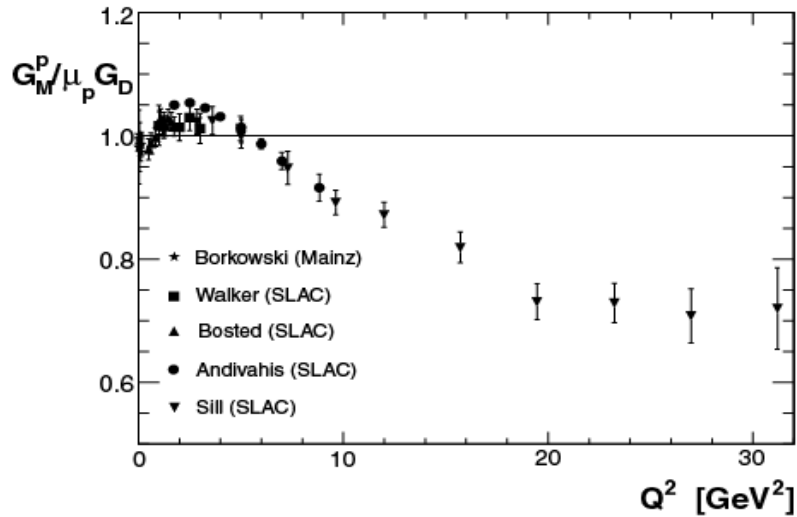
$$Q^2 = 4 E E' \sin^2(\theta/2) \text{ and } \tau = Q^2 / 4m_p^2$$

Elastic cross sections at small angles and small Q^2 's are dominated by G_E (Prad Hall B)

Elastic cross Sections at small angles and small Q^2 's are dominated by G_M (GMP Hall A)

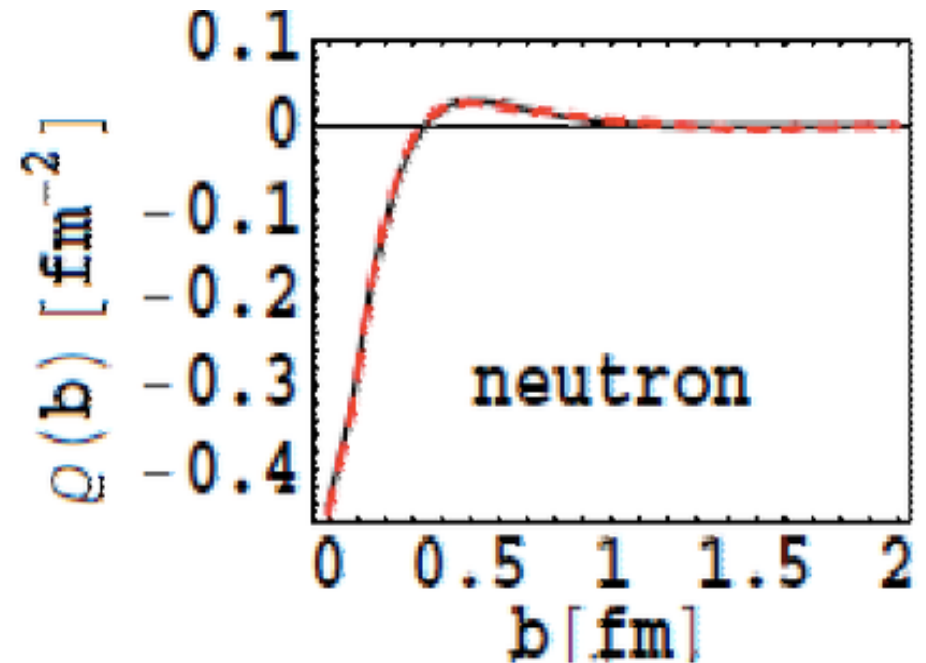
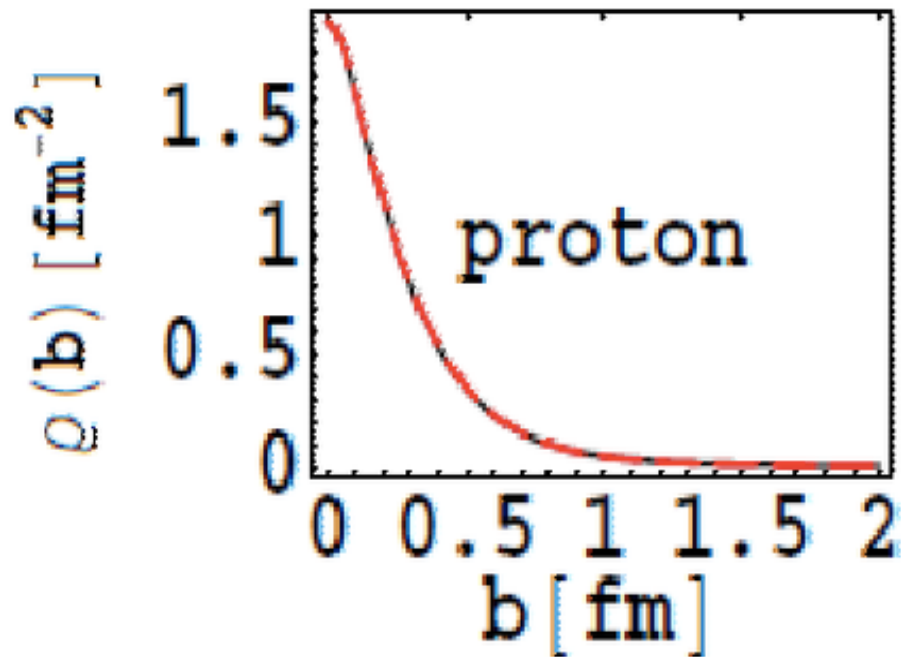
For moderate Q^2 's one can separate G_E and G_M with Rosenbluth or asymmetry measurements.

Before JLab and Recent non-JLab Data



Form Factors \rightarrow Charge/Current Distributions

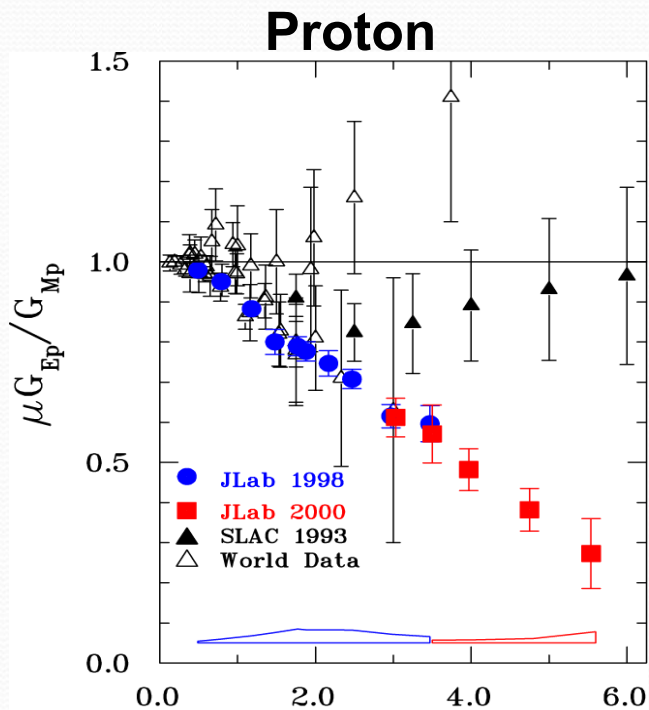
Elastic electric form factor \rightarrow Charge distributions



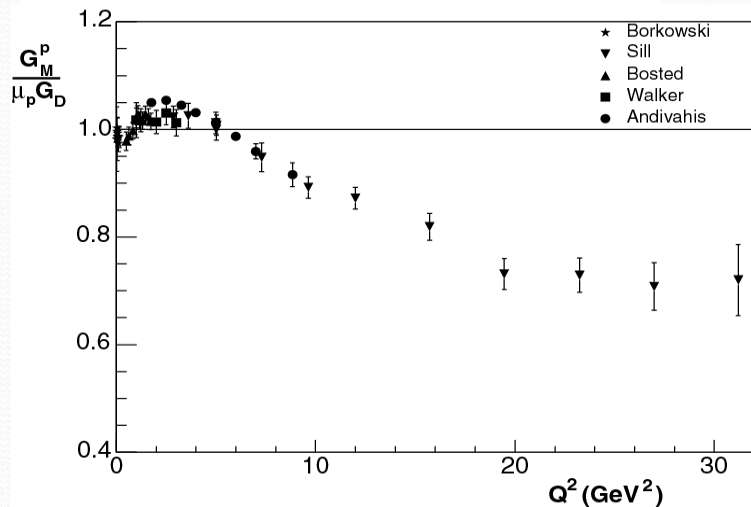
JLab Data on EM Form Factors

Testing Ground for Theories of Nucleon Structure

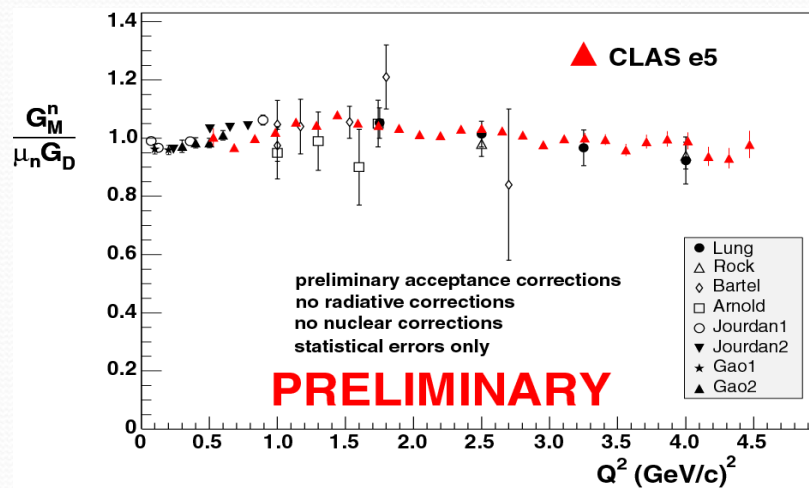
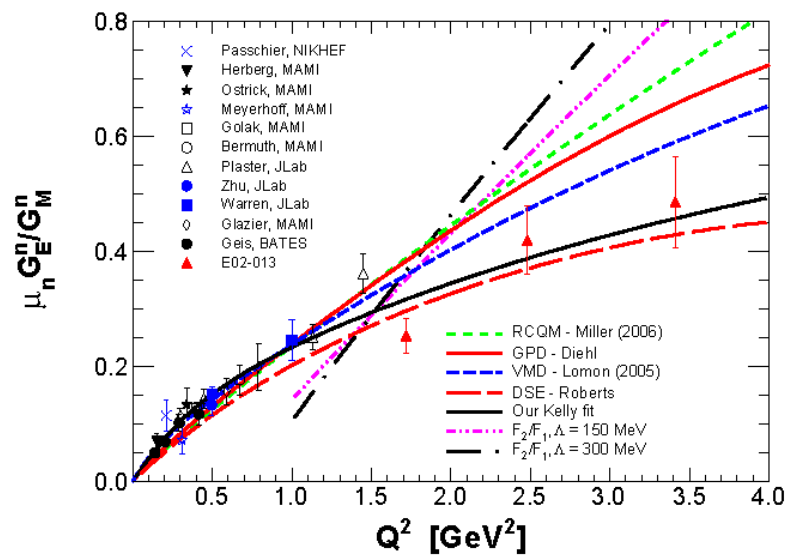
Electric



Magnetic



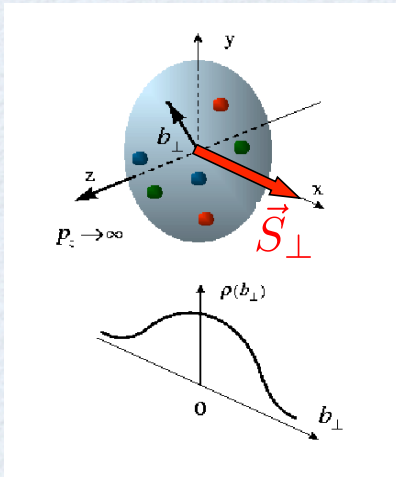
Neutron



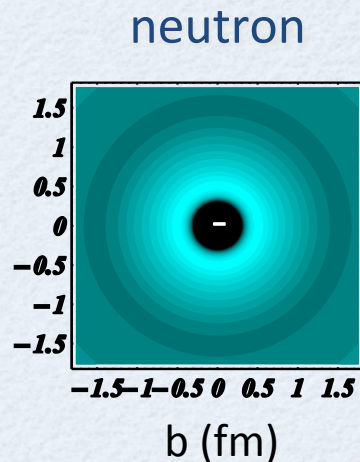
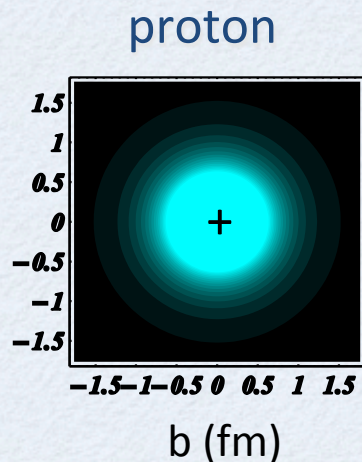
Form factors: 2D light-front densities of hadrons

$$\rho^N(\vec{b}) = \int_0^\infty \frac{dQ}{2\pi} Q J_0(bQ) F_1(Q^2) + \sin(\phi_b - \phi_S) \int_0^\infty \frac{dQ}{2\pi} \frac{Q^2}{2M_N} J_1(bQ) F_2(Q^2)$$

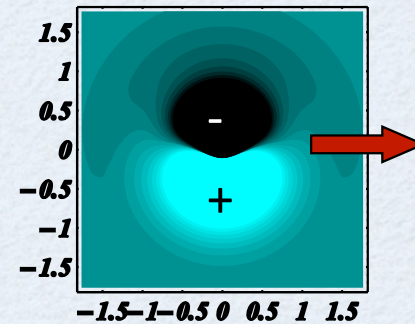
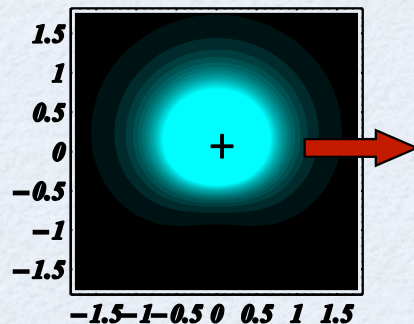
→ unpolarized Dirac FF F_1
 → transverse polarization Pauli FF F_2



unpolarized charge density



density for transverse polarization



Burkardt (2000, 2003)

Miller (2007)

Carlson, Vdh (2008)

G_E^p : JLab Polarization-Transfer Data

Using Focal Plane Polarimeter in Hall A

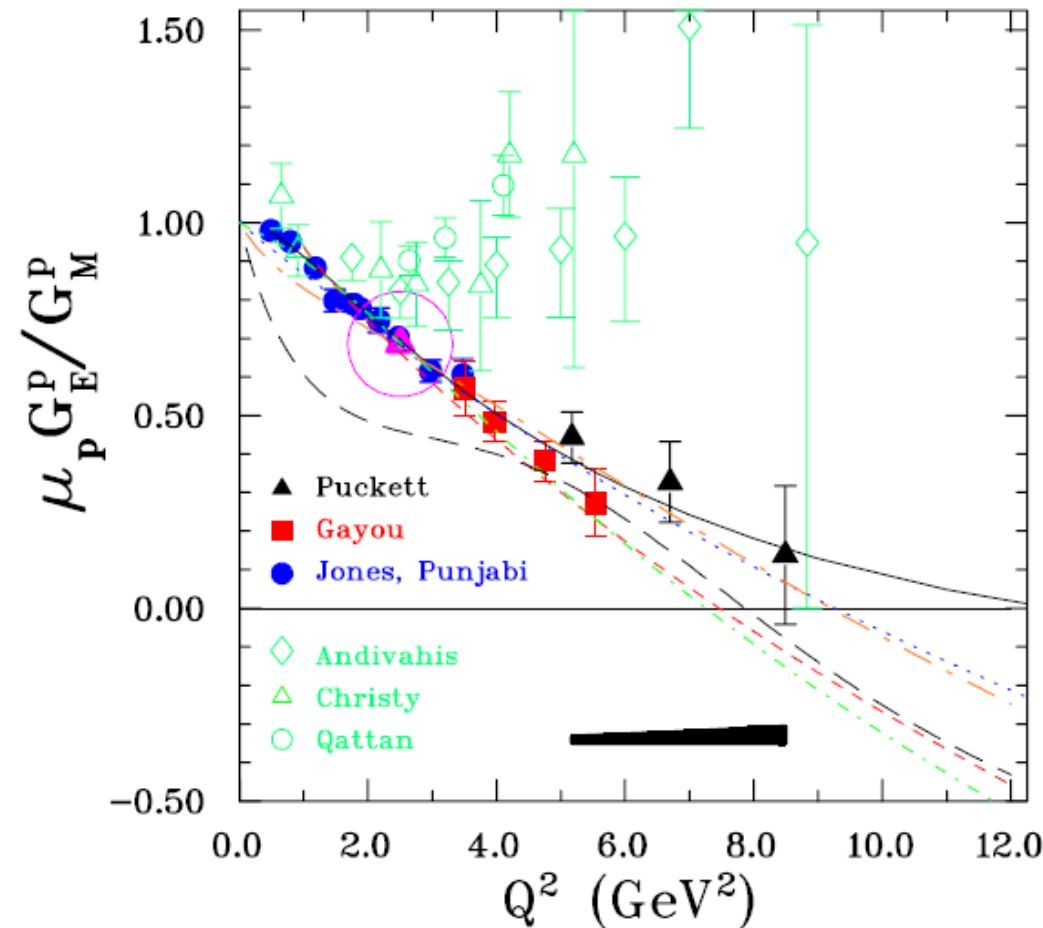
- E93-027 PRL 84, 1398 (2000)
- E99-007 PRL 88, 092301 (2002)
- E04-108, [arXiv:1005.3419v2](https://arxiv.org/abs/1005.3419v2) (2010)

Clear discrepancy between polarization transfer and Rosenbluth data

- Investigate possible theoretical sources for discrepancy
→ likely two-photon contributions

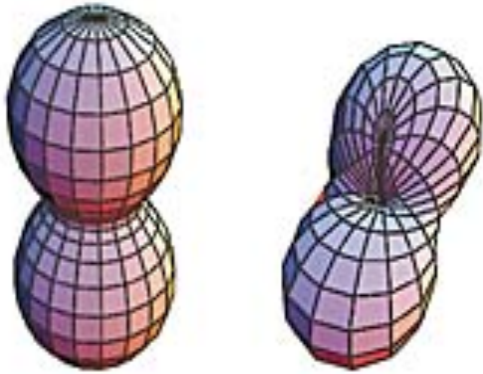
Information on the shape of the proton and the orbital angular momentum.

Transverse density .

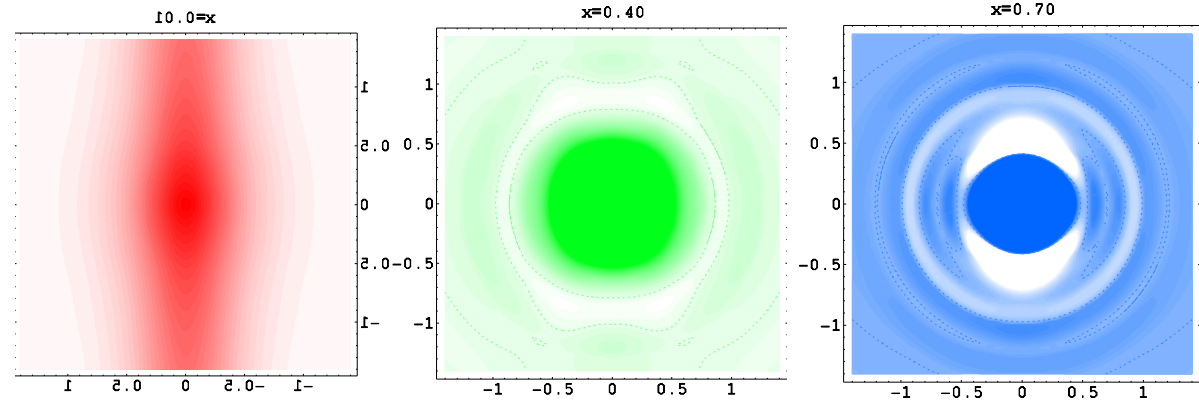


The Proton's Shape

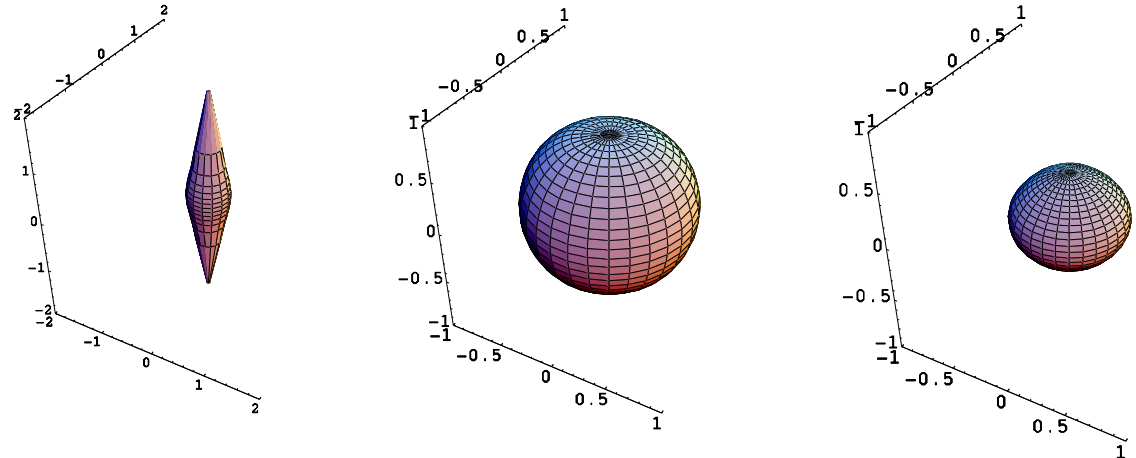
It's a Ball. No, It's a Pretzel.
Must Be a Proton.
(K. Chang, NYT, May 6, 2003)



Belitsky, Ji and Yuan: PRD 69, 074014(04)

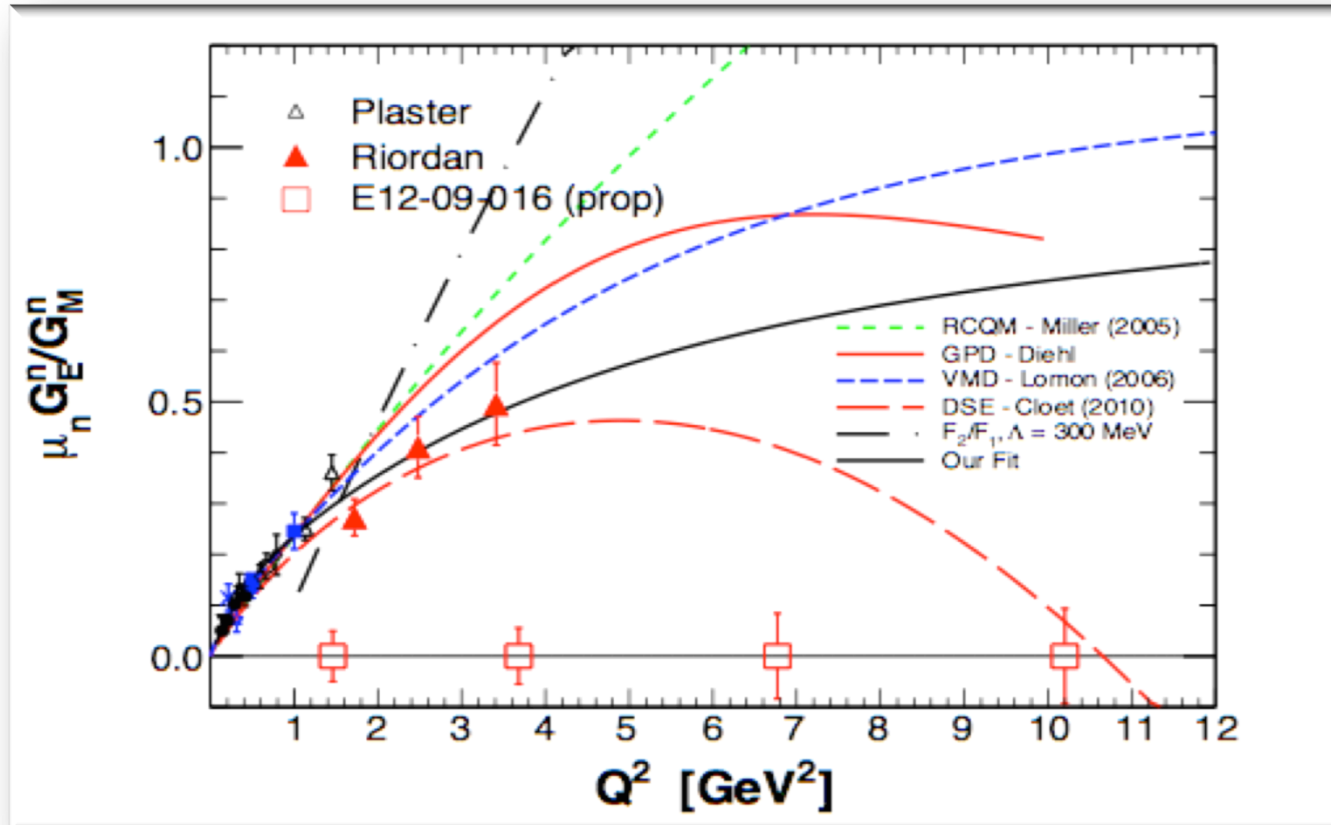


quark spin parallel to that
of the proton (left), quark spin
perpendicular to the proton spin
(right).



G. Miller, PRC 68, 022201 (03)

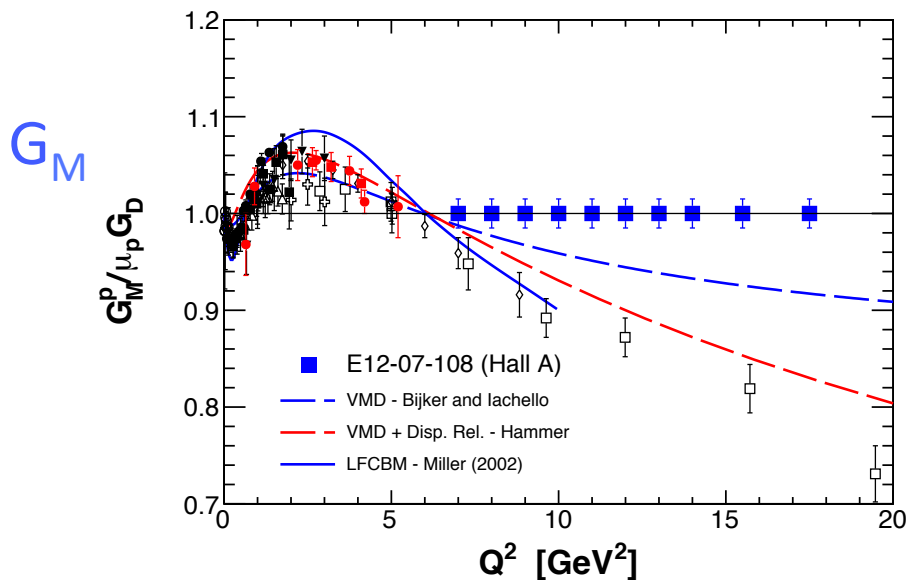
G_E^n : 6 GeV Results and 12 GeV Plan



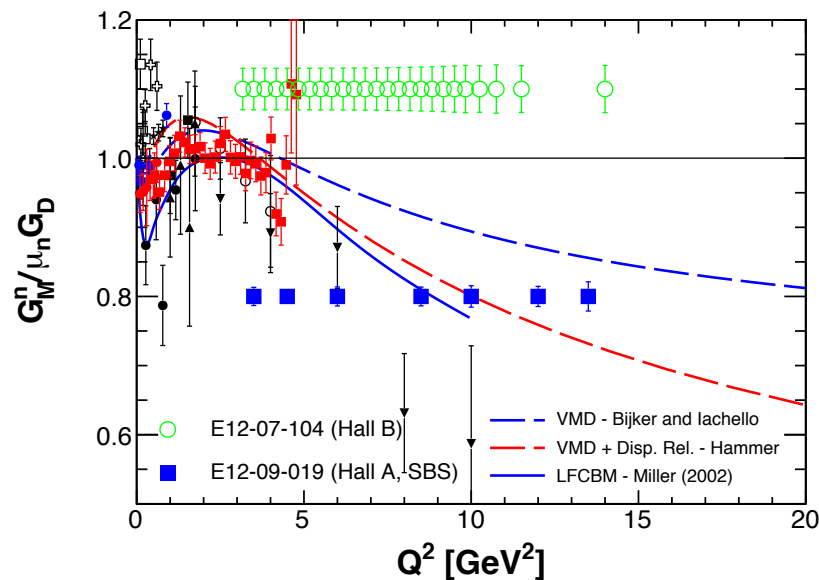
- *The dramatic turnover of the Argonne DSE model would be clearly visible.*
- *If the turnover is seen, it would provide strong evidence for the importance of diquark degrees of freedom in the nucleon form factors.*

Planned JLab Measurements of Form Factors

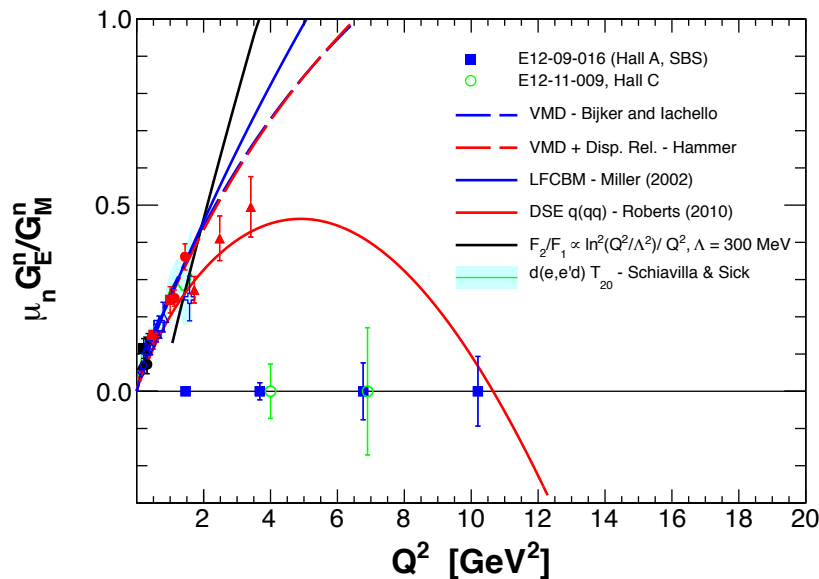
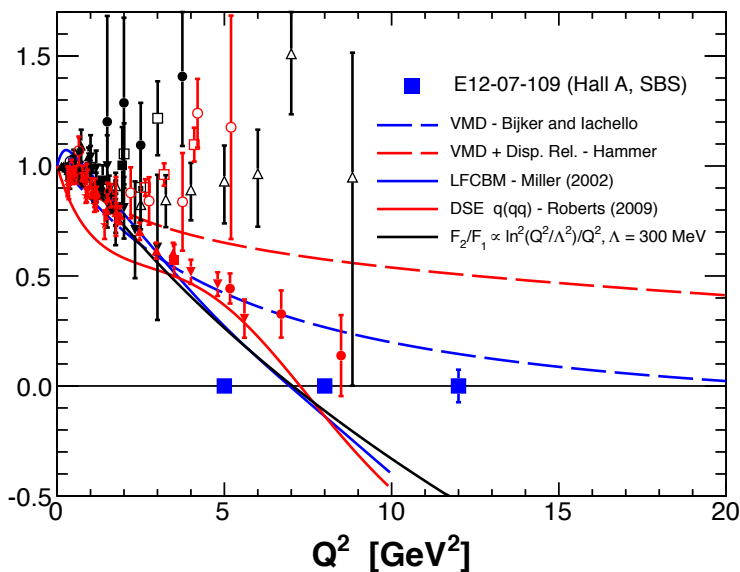
Proton



Neutron



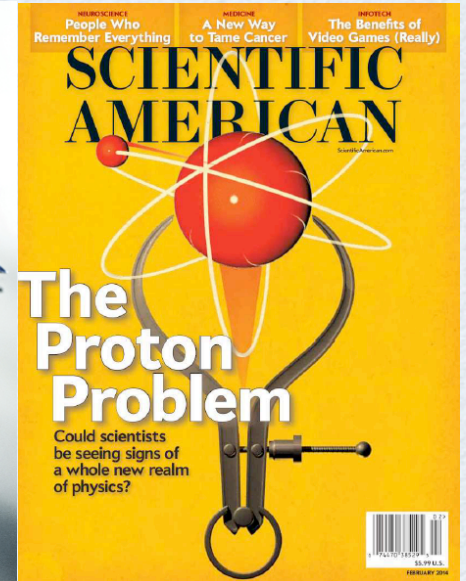
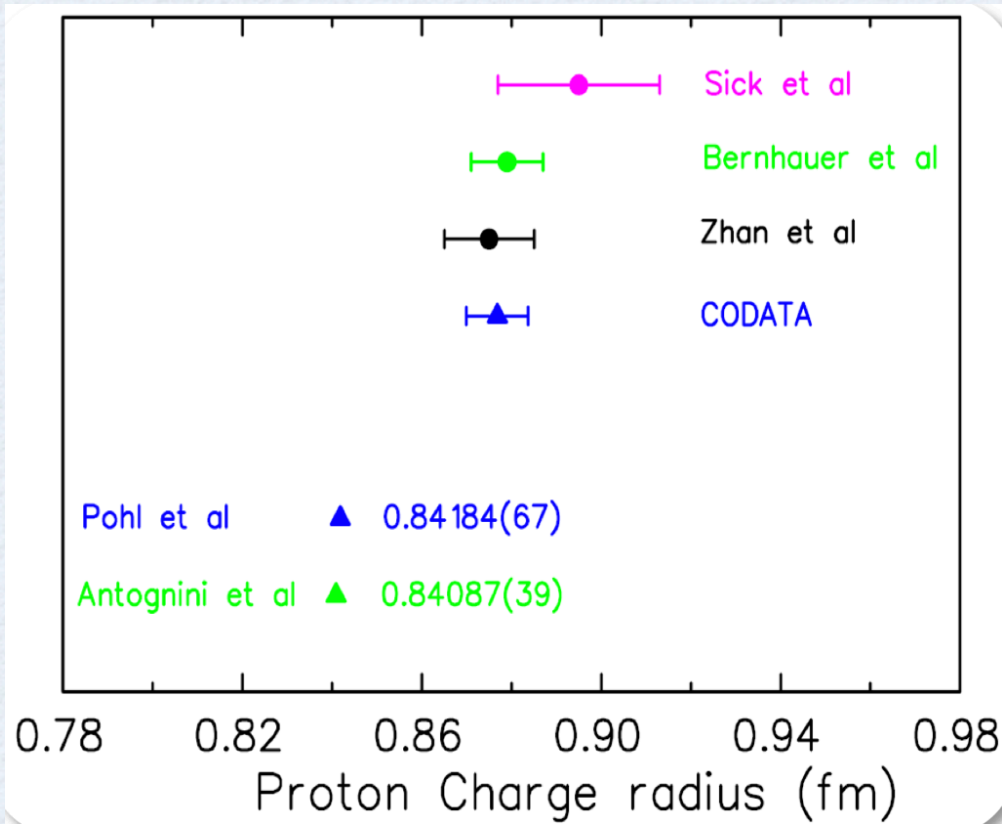
G_E



Proton Radius Puzzle

Electron probe vs. muon probe

Proton radius puzzle



μH data:

$$R_E = 0.8409 \pm 0.0004 \text{ fm}$$

Pohl et al. (2010)

Antognini et al. (2013)



7σ difference !?

ep data:

$$R_E = 0.8775 \pm 0.0051 \text{ fm}$$



Charge Radius of the Proton

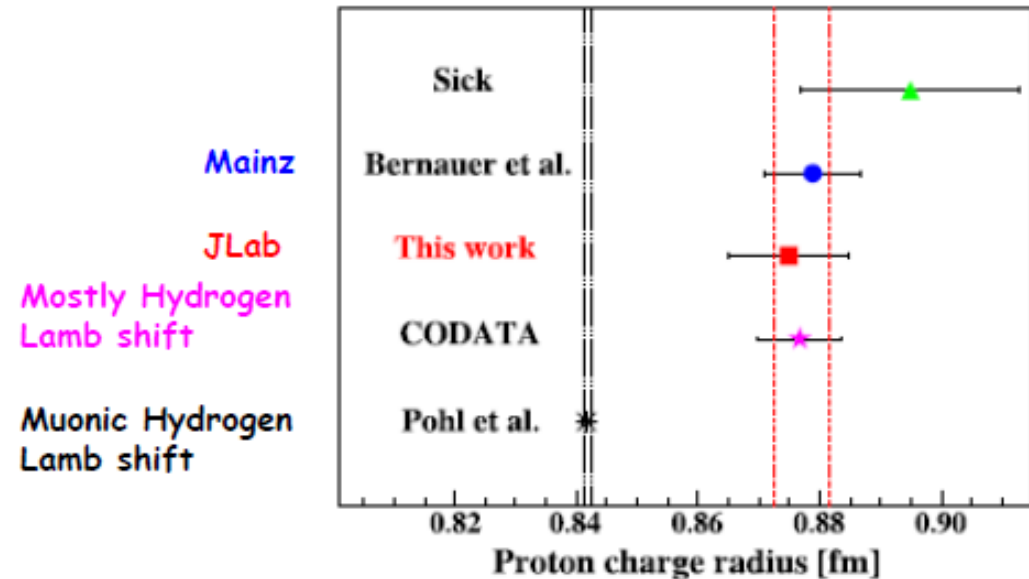
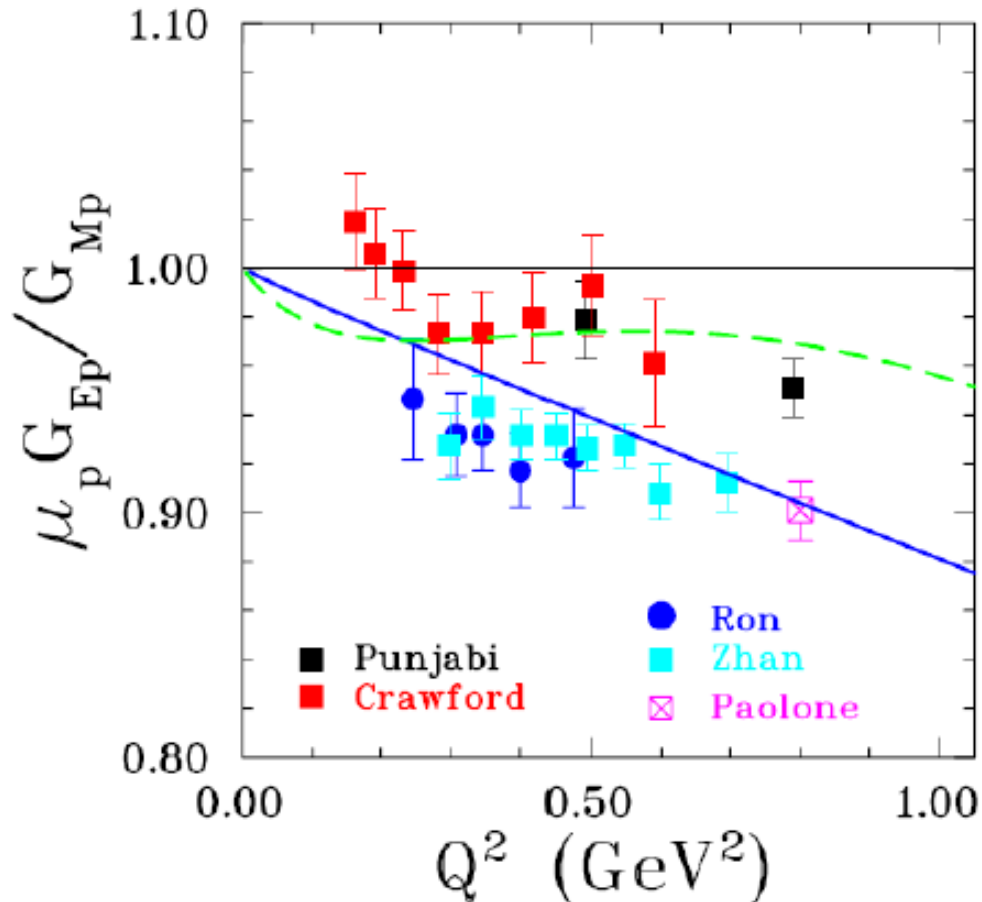
- Proton G_E has no measured minima and it is too light for the Fourier transformation to work in a model independent way.
- Thus for the proton we make use of the fact that as Q^2 goes to zero the charge radius is proportional to the slope of G_E

$$G_E(Q^2) = 1 + \sum_{n \geq 1} \frac{(-1)^n}{(2n + 1)!} \langle r^{2n} \rangle Q^{2n}$$

$$r_p \equiv \sqrt{\langle r^2 \rangle} = \left(-6 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \right)^{1/2}$$

We don't measure to Q^2 of zero, so this is going to be an extrapolation problem.

Systematic issues with low- Q^2 G_{Ep} polarization data!



r_p from muonic hydrogen Lamb shift disagrees with ep scattering and electronic hydrogen Lamb shift determinations

Beam-target asymmetry and recoil polarization data disagree at low Q^2 !

Tension among low- Q^2 G_E/G_M ratios from polarization observables not yet understood, but at least one of these experiments has to have an unaccounted-for source of systematic error!

Proton radius puzzle: what's next ?

- ➔ μH Lamb shift: muonic D, muonic ^3He , ^4He have been performed
- ➔ electronic H Lamb shift: higher accuracy measurements underway
- ➔ electron scattering analysis: **Lorenz et al.**
 - radius extraction fits (use fits with correct analytical behavior: 2π cut)
 - radiative corrections, two-photon exchange corrections

new fit $R_E = 0.904 (15) \text{ fm}$ (4σ from μH) **Lee, Arrington, Hill (2015)**

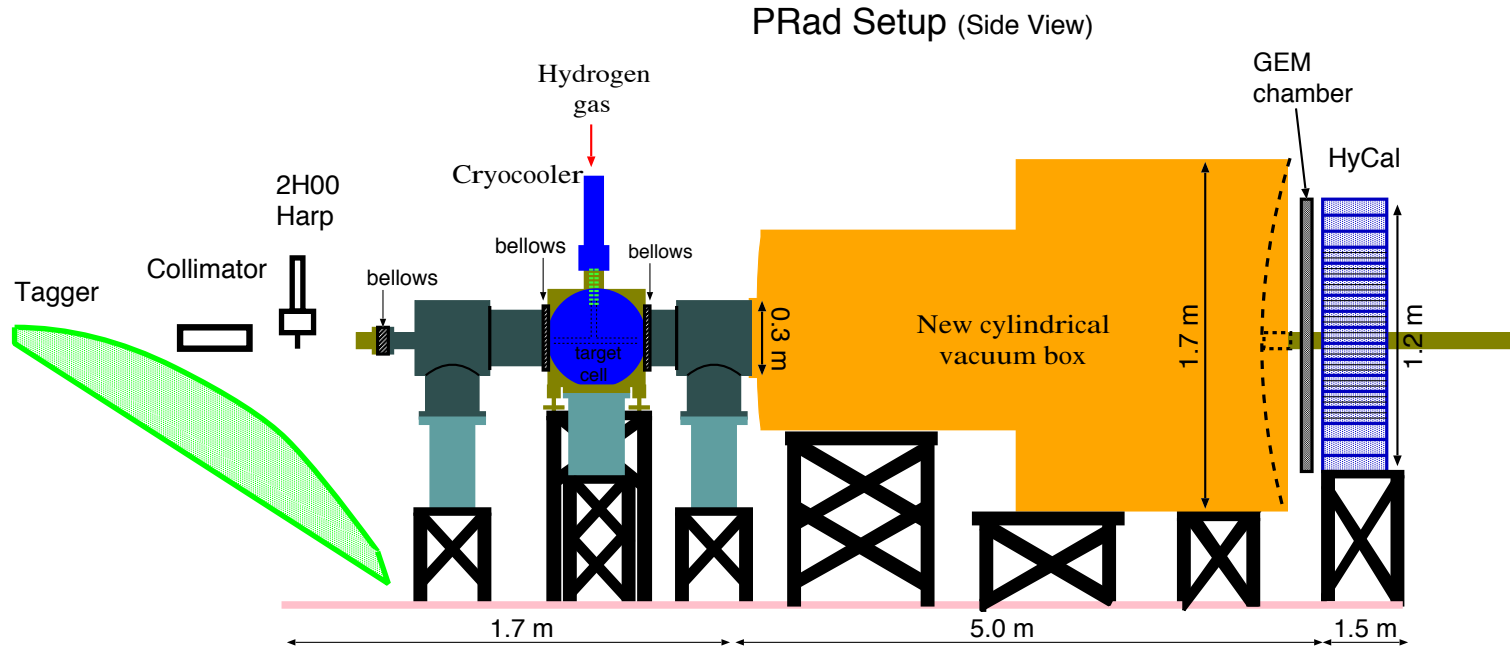
➔ electron scattering experiments:
new G_{Ep} experiments down to $Q^2 \approx 2 \times 10^{-4} \text{ GeV}^2$

- **MAMI/A1**: Initial State Radiation (2013/4)
- **JLab/Hall B**: HyCal, magnetic spectrometer-free experiment, norm to Møller (2016/7)
see talk: H. Gao
- **MESA**: low-energy, high resolution spectrometers (2019)

➔ muon scattering experiments: **MUSE@PSI** (2017/8)

➔ e^-e^+ versus $\mu^-\mu^+$ photoproduction: lepton universality test

PRad Experimental Setup in Hall B at JLab



- **High resolution, large acceptance calorimeter**
- **Windowless H₂ gas flow target**
- **Simultaneous detection of elastic and Moller electrons**
- **GEM detectors**
- **Q² range of $2 \times 10^{-4} - 0.14 \text{ GeV}^2$**

Future sub 1% measurements:

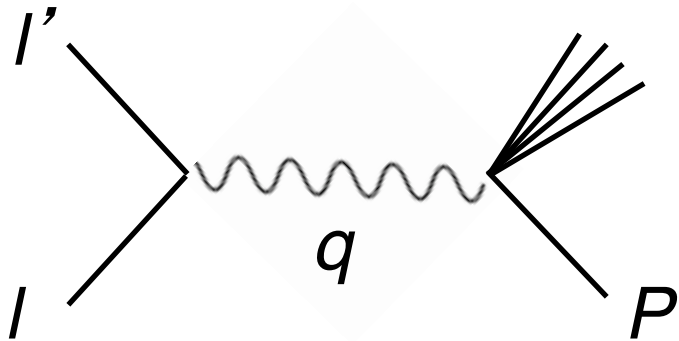
- (1) ep elastic scattering at Jlab (PRad)
- (2) μ p elastic scattering at PSI - 16 U.S. institutions! (MUSE)
- (3) ISR experiments at Mainz

Ongoing H spectroscopy experiments

Deep-Inelastic Scattering Unpolarized Nucleon Structure

Parton Distributions:
Flavor Structure: Valence and Sea
Gluons

Inelastic Scattering



Considerably more complex, indeed!

Simplify - consider *inclusive* inelastic scattering,

$$d\sigma \propto \langle |\mathcal{M}|^2 \rangle = \frac{g_e^4}{q^4} L_{\text{lepton}}^{\mu\nu} W_{\mu\nu \text{ nucleon}}, \quad W_{\mu\nu \text{ nucleon}}(p, q)$$

Again, two (parity-conserving, spin-independent) structure functions:

$$W_1, W_2 \quad \text{or, alternatively expressed,} \quad F_1, F_2$$

which may depend on two invariants,

$$Q^2 = -q^2, \quad x = -\frac{q^2}{2q \cdot p}, \quad 0 < x < 1$$

So much for the structure, the physics is in the structure functions.

Elastic scattering off Dirac Protons

Compare:

$$L_{\text{lepton}}^{\mu\nu} = 2 (k^\mu k'^\nu + k^\nu k'^\mu + g^{\mu\nu} (m^2 - k \cdot k'))$$

with:

$$K_{\mu\nu \text{ nucleon}} = K_1 \left(-g_{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) + \frac{K_2}{M^2} \left(p^\mu + \frac{1}{2} q^\mu \right) \left(p^\nu + \frac{1}{2} q^\nu \right)$$

which uses the relations between $K_{1,2}$ and $K_{4,5}$

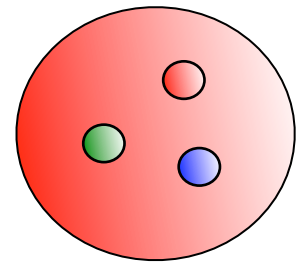
Then, e.g. by substitution of $k' = k - q$ in L :

$$K_1 = -q^2, \quad K_2 = 4M^2$$

Note, furthermore, that inelastic cross section reduces to the elastic one for:

$$W_{1,2}(q^2, x) = -\frac{K_{1,2}(q^2)}{2Mq^2} \delta(x - 1)$$

Elastic scattering off Dirac Partons



Imagine *incoherent* scattering off *Dirac* Partons (quarks) q :

$$W_1^q = \frac{e_q^2}{2m_q} \delta(x_q - 1), \quad W_2^q = -\frac{2m_q e_q^2}{q^2} \delta(x_q - 1) \quad \text{and} \quad x_q = -\frac{q^2}{2q \cdot p_q}$$

and, furthermore, suppose that the quarks carry a fraction, z , of the proton momentum

$$p_q = z_q p, \quad \text{so that} \quad x_q = \frac{x}{z_q} \quad (\text{also note } m_q = z_q M !)$$

which uses the relations between $K_{1,2}$ and $K_{4,5}$

Now,

$$MW_1 = M \sum_q \int_0^1 \frac{e_q^2}{2M} \delta(x - z_q) f_q(z_q) dz_q = \frac{1}{2} \sum_q e_q^2 f_q(x) \equiv F_1(x)$$
$$-\frac{q^2}{2Mx} W_2 = \sum_q \int_0^1 x e_q^2 \delta(x - z_q) f_q(z_q) dz_q = x \sum_q e_q^2 f_q(x) \equiv F_2(x)$$

Two important *observable* consequences,

Bjorken scaling: $F_{1,2}(x)$, not $F_{1,2}(x, Q^2)$

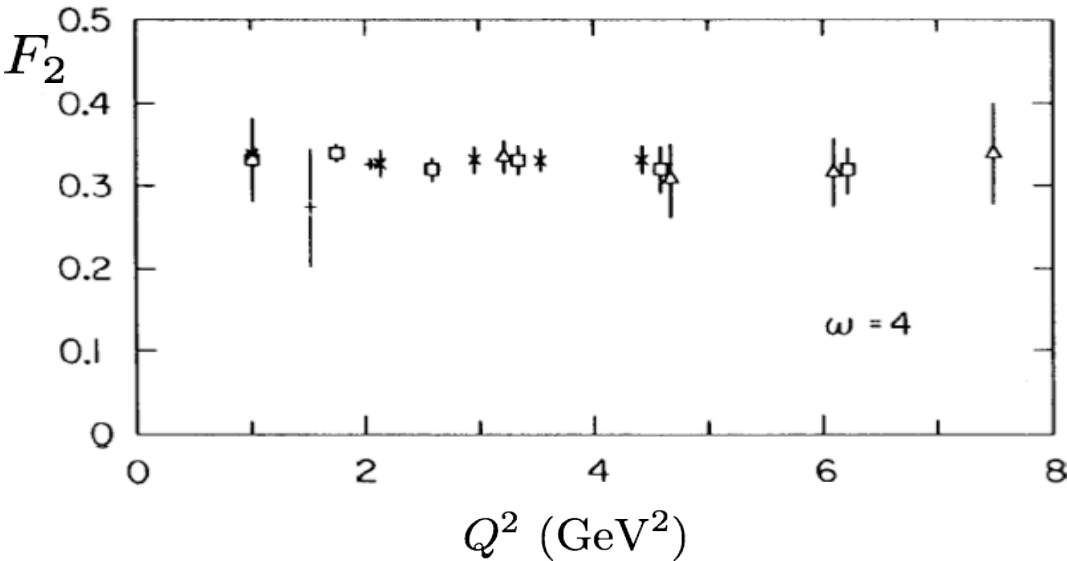
Callan-Gross relation: $F_2 = 2xF_1(x)$

Deep-Inelastic Electron Scattering

Discovery of Quarks (Partons)

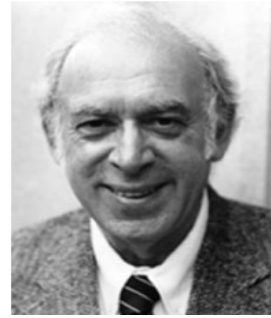
Bjorken scaling:

+ 6° □ 18°
 × 10° △ 26°



Point particles cannot be further resolved; their measurement does not depend on wavelength, hence Q^2 ,

Spin-1/2 quarks cannot absorb longitudinally polarized vector bosons and, conversely, spin-0 (scalar) quarks cannot absorb transversely polarized photons.



J.T. Friedman



R. Taylor

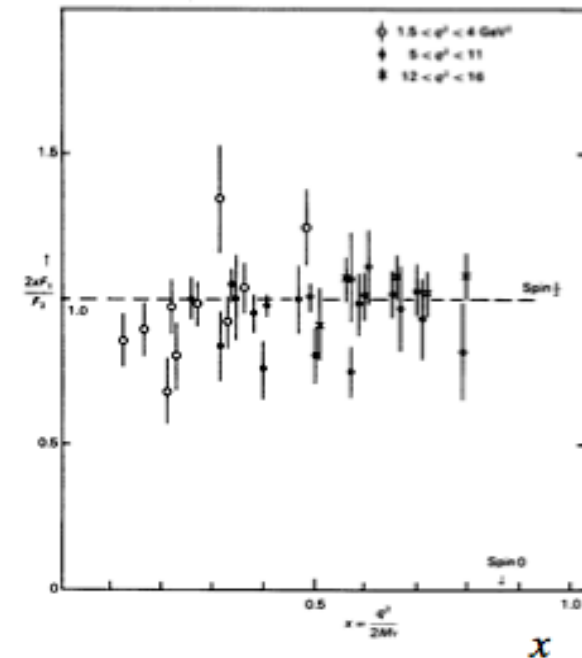


H.W. Kendall

Nobel Prize 1990

Callan-Gross relation:

$$\frac{2xF_1}{F_2}$$



spin 1/2

spin 0

Deep-Inelastic Neutrino Scattering

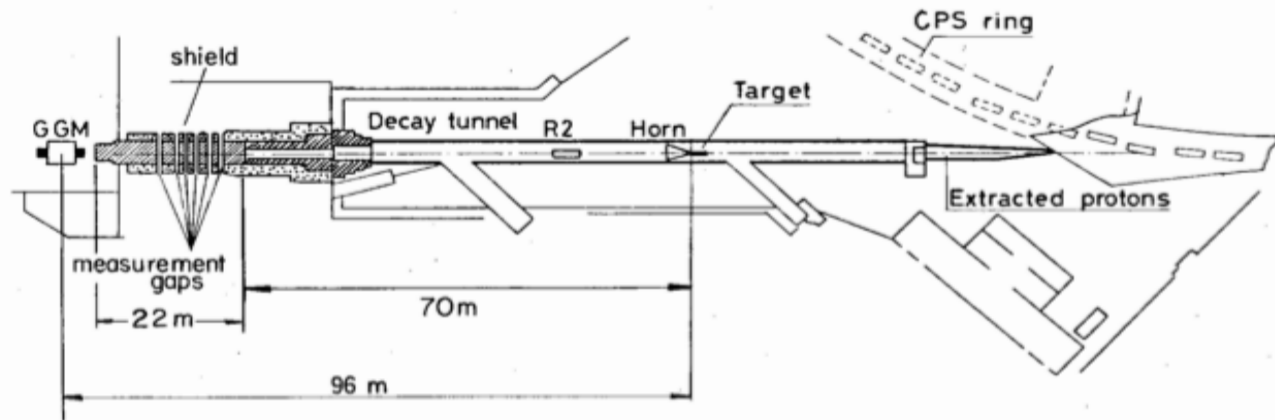


Picture from CERN...

*Gargamelle bubble chamber,
observation of weak neutral
current (1973).*

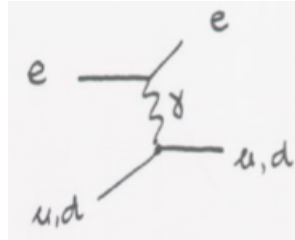
Charged-current DIS!

- Nucl.Phys. **B73** (1974) 1
- Nucl.Phys. **B85** (1975) 269
- Nucl.Phys. **B118** (1977) 218
- Phys.Lett. **B74** (1978) 134



Deep-Inelastic Scattering - Fractional Electric Charges

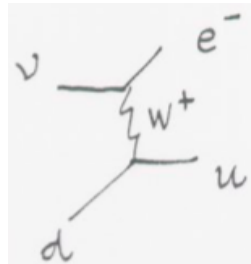
**Neutral-current (photon)
DIS:**



$$F_2 = x \sum e_q^2 (q + \bar{q}), \quad p : uud, \quad n : ddu$$

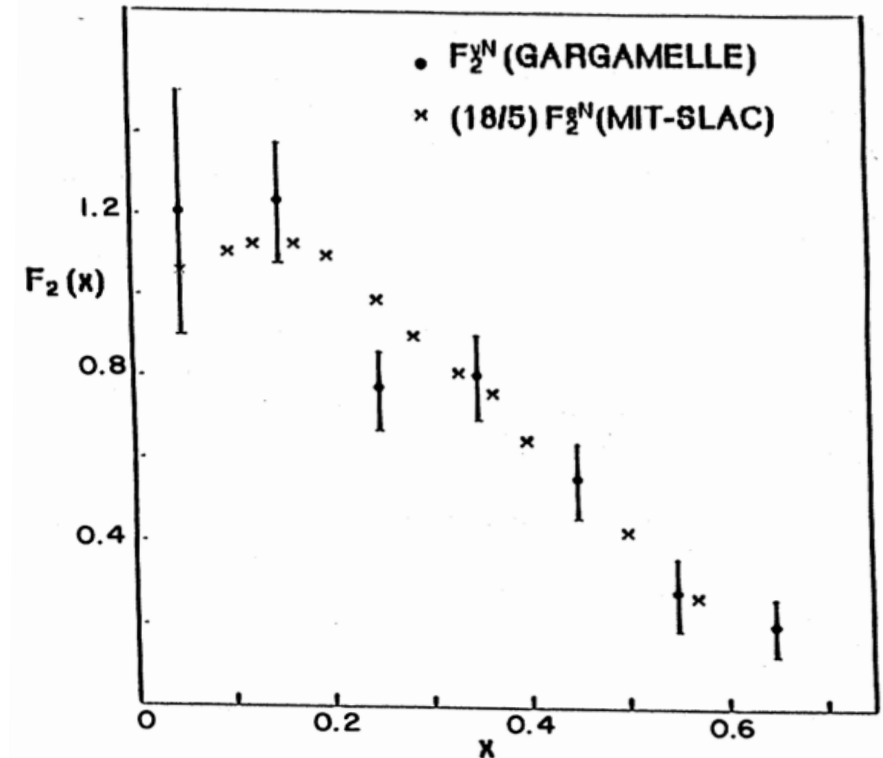
$$F_2^N = x \frac{e_u^2 + e_d^2}{2} (u + \bar{u} + d + \bar{d})$$

Charged-current DIS:



$$F_2^{\nu p} = 2x(d + \bar{u}), \quad F_2^{\nu n} = 2x(u + \bar{d})$$

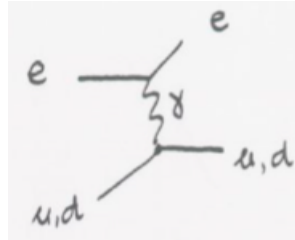
$$F_2^{\nu N} = x(u + \bar{u} + d + \bar{d})$$



Deep-Inelastic Scattering - Fractional Electric Charges

Neutral-current (photon)

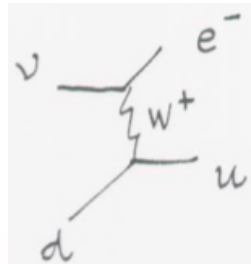
DIS:



$$F_2 = x \sum e_q^2 (q + \bar{q}), \quad p : uud, \quad n : ddu$$

$$F_2^N = x \frac{e_u^2 + e_d^2}{2} (u + \bar{u} + d + \bar{d})$$

Charged-current DIS:

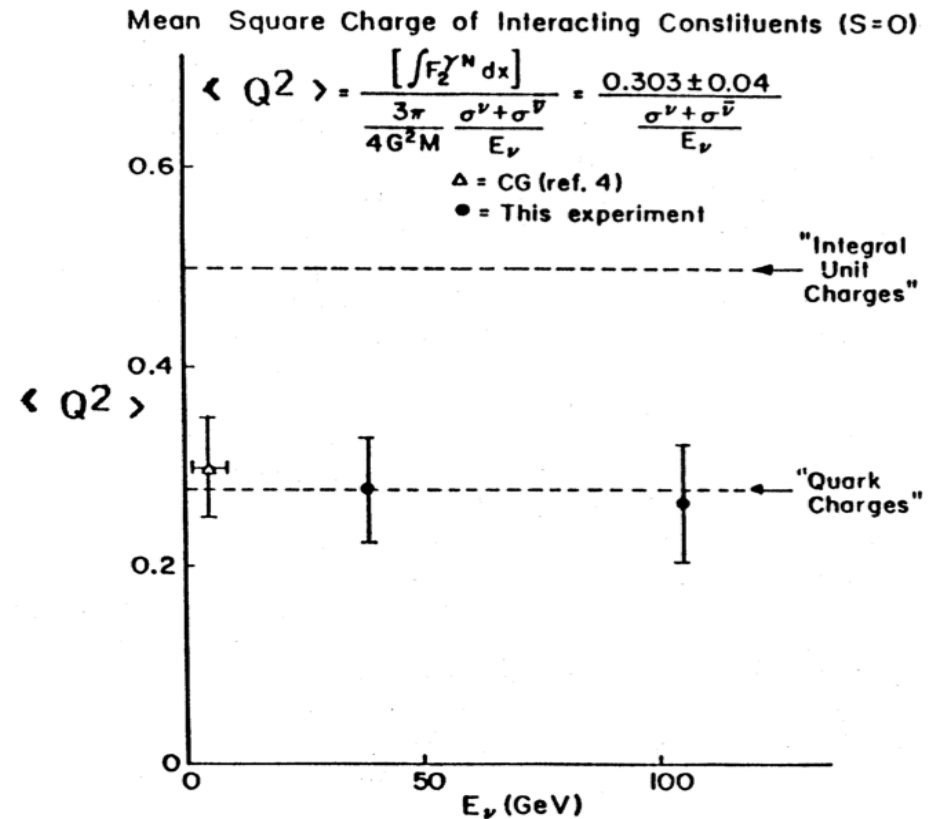


$$F_2^{\nu p} = 2x(d + \bar{u}), \quad F_2^{\nu n} = 2x(u + \bar{d})$$

$$F_2^{\nu N} = x(u + \bar{u} + d + \bar{d})$$

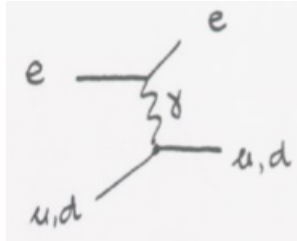
Ratio:

$$\frac{F_2^N}{F_2^{\nu N}} = \frac{1}{2}(e_u^2 + e_d^2) = \frac{5}{18} \simeq 0.28$$



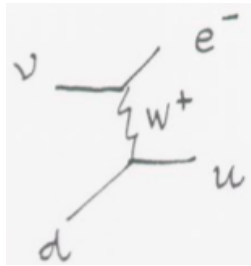
Deep-Inelastic Scattering - Momentum Conservation

Neutral-current (photon) DIS:



$$F_2^N = x \frac{e_u^2 + e_d^2}{2} (u + \bar{u} + d + \bar{d})$$

Charged-current DIS:



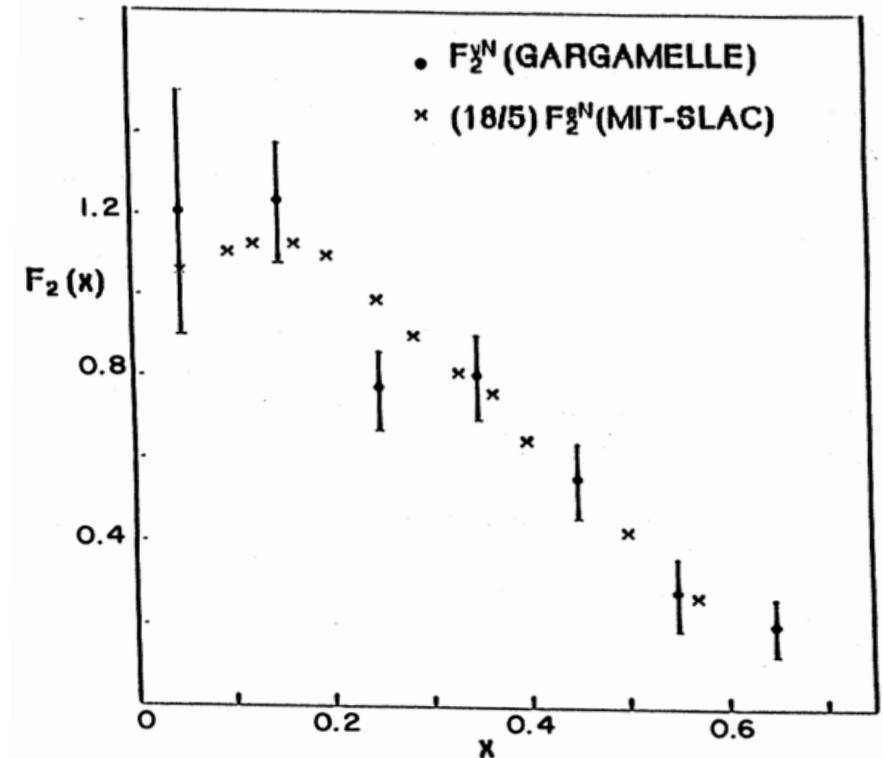
$$F_2^{\nu N} = x(u + \bar{u} + d + \bar{d})$$

Momentum fraction:

$$\int_0^1 F_2^N dx = \frac{e_u^2 + e_d^2}{2} \int_0^1 x(u + \bar{u} + d + \bar{d})$$

Gargamelle: 0.49 +/- 0.07

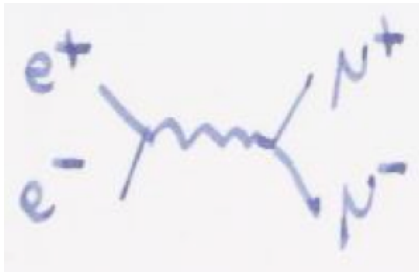
SLAC: 0.14 +/- 0.05



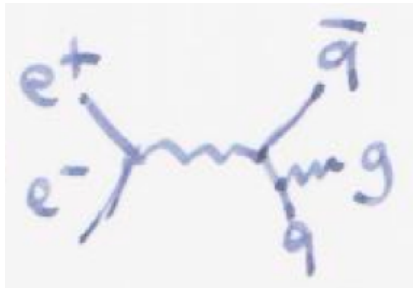
Quarks carry half of the nucleon momentum!

3-jet events at PETRA

Recall the intro on colour:

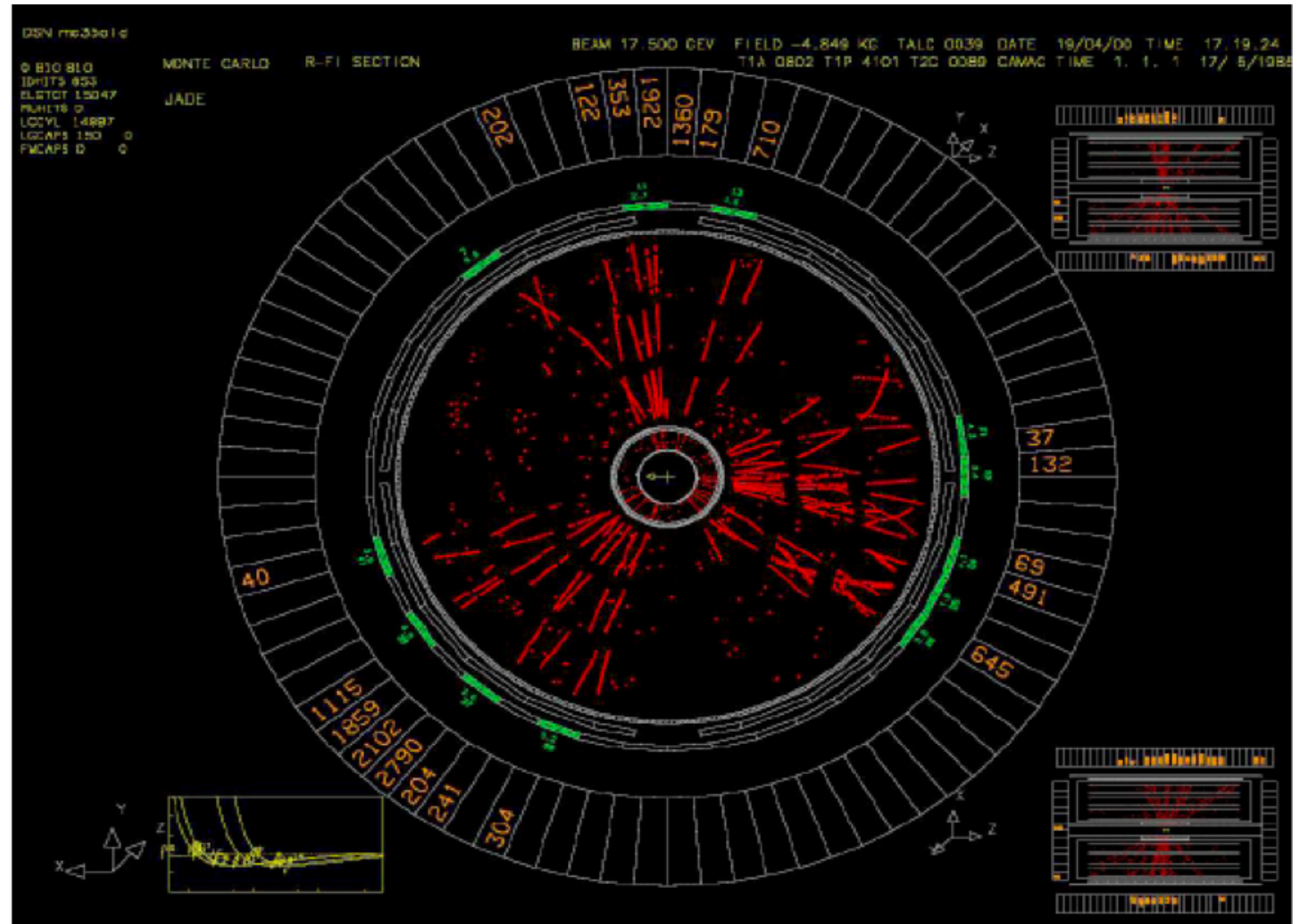


Observation of its higher order process,

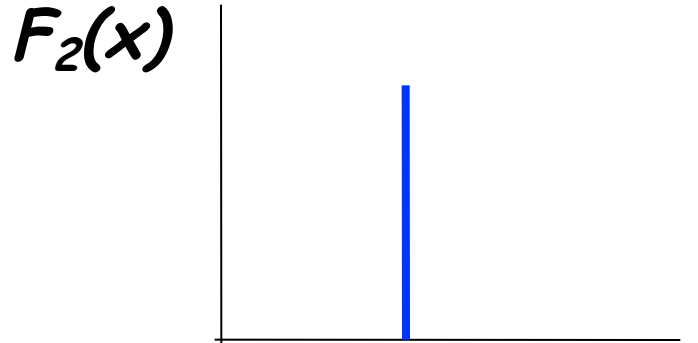


marks the discovery of the gluon.

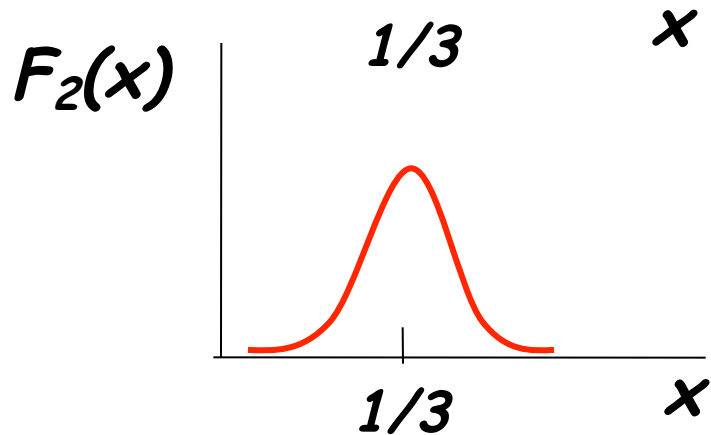
Mom. Conservation: *Gluons carry the other half of the nucleon momentum.*



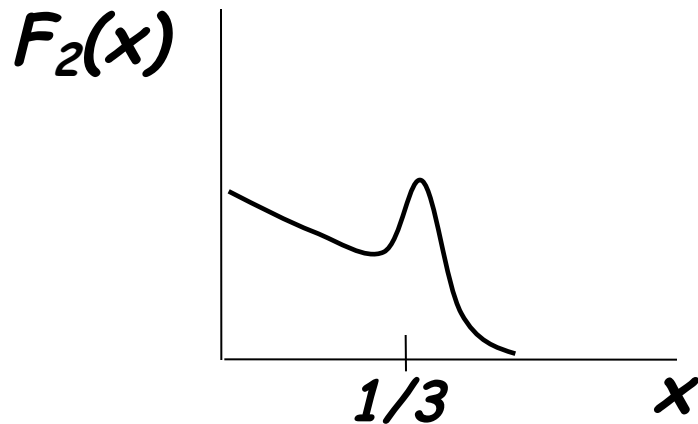
Nucleon Structure



Three quarks with 1/3 of total proton momentum each.

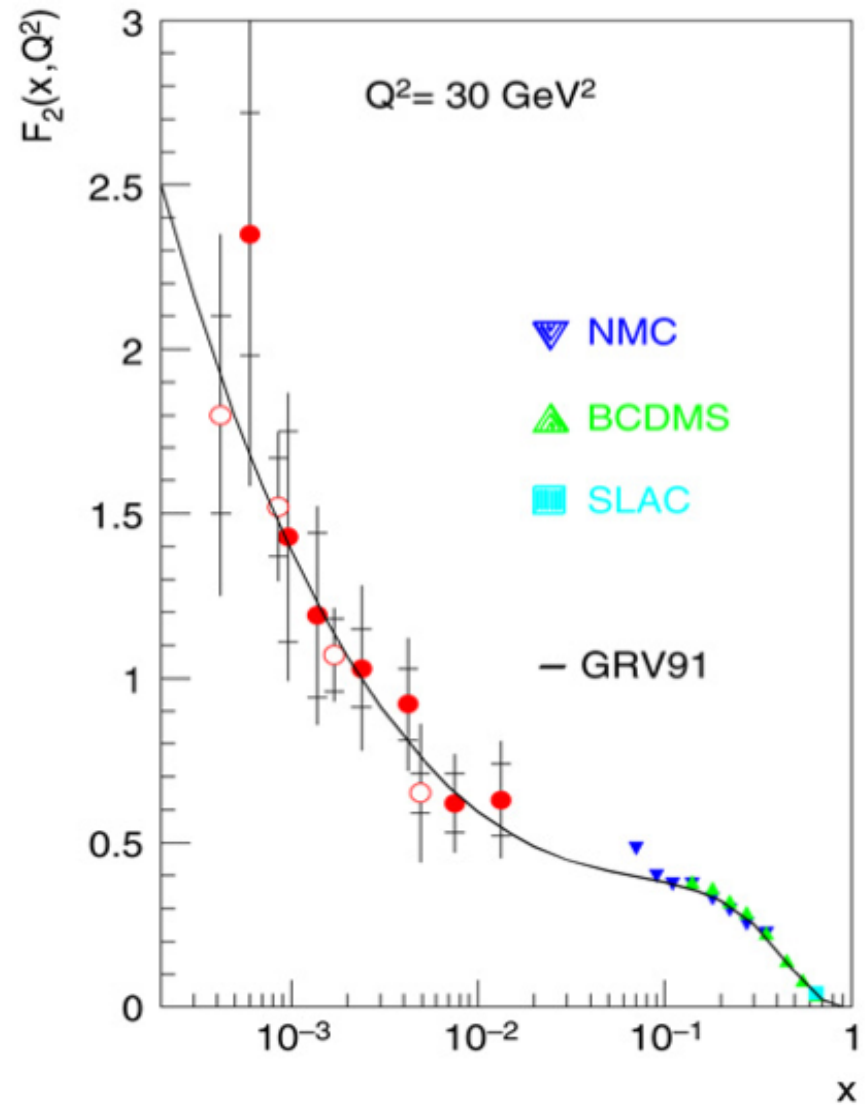
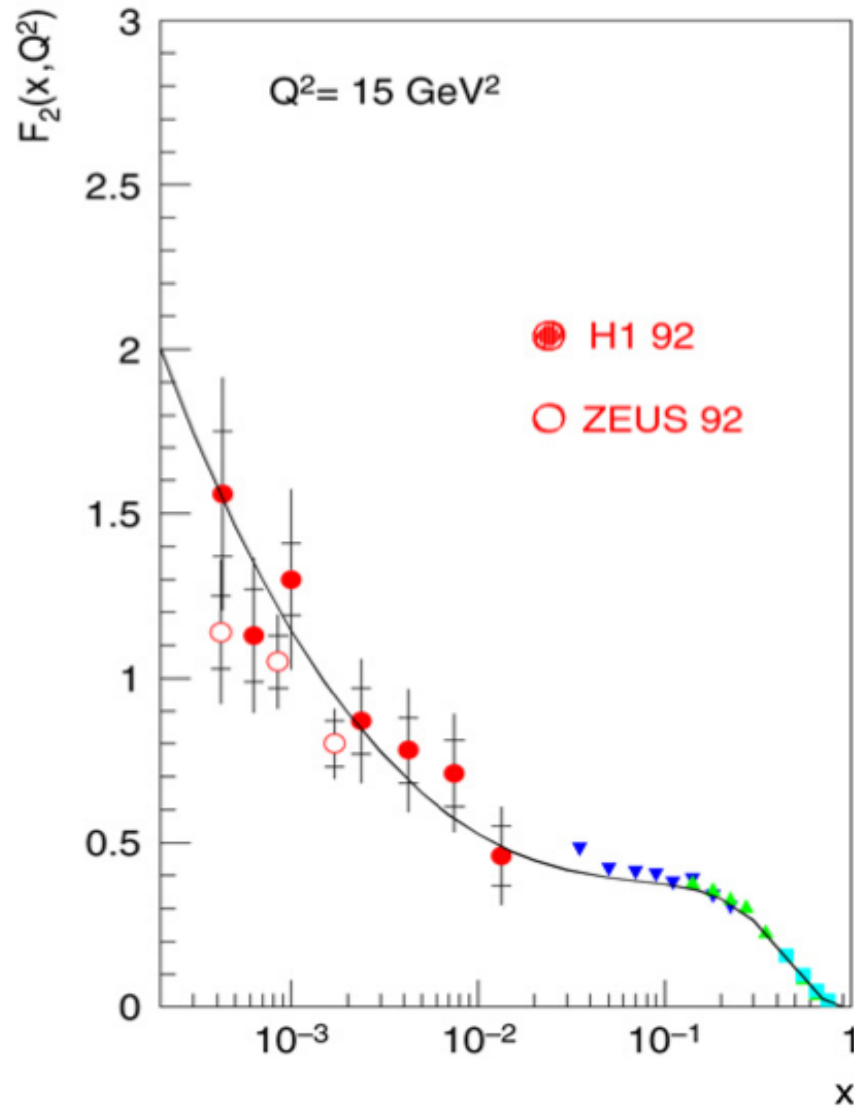


Three quarks with some momentum smearing.

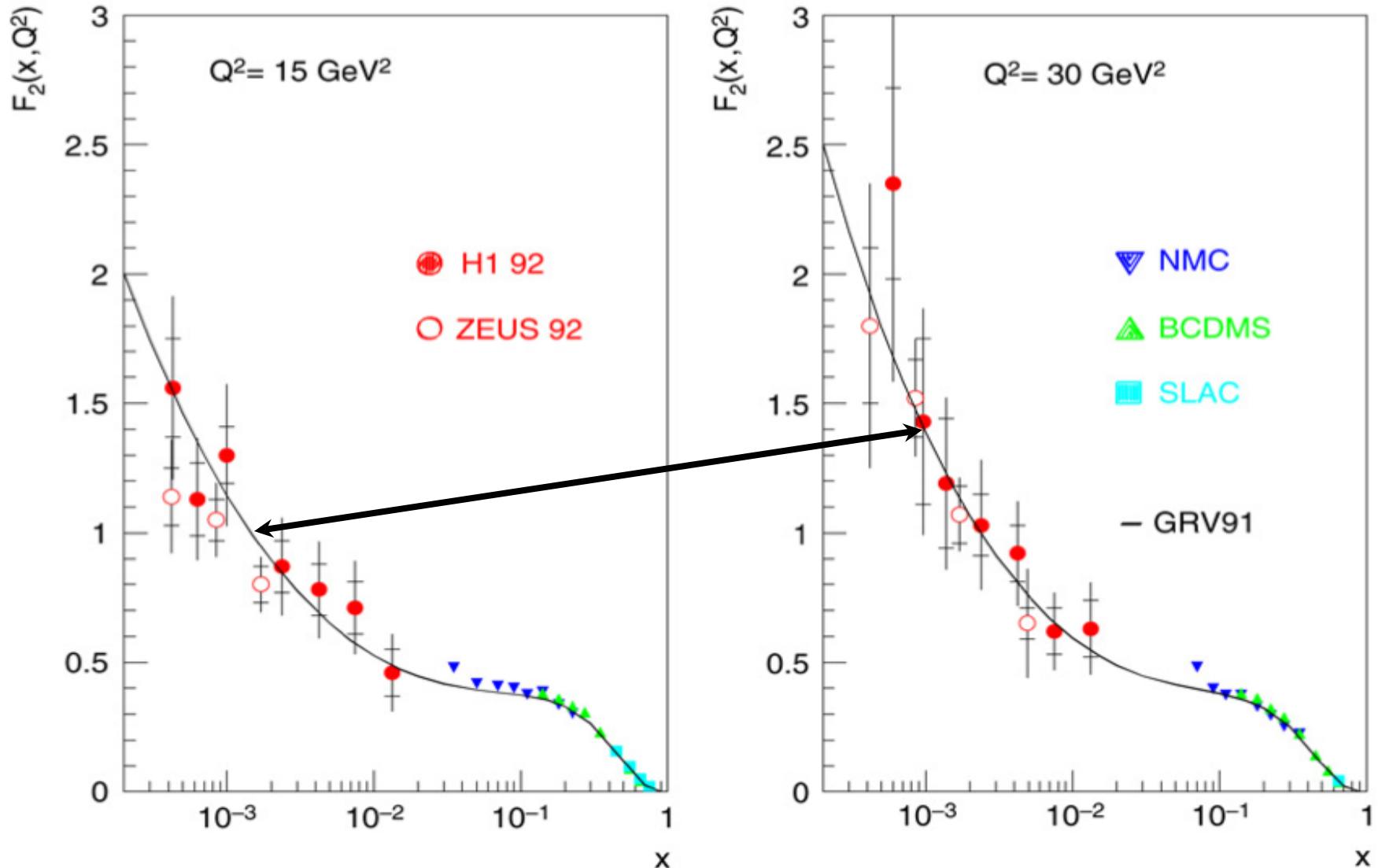


The three quarks radiate gluons to lower momentum fractions x .

HERA - Early Measurements



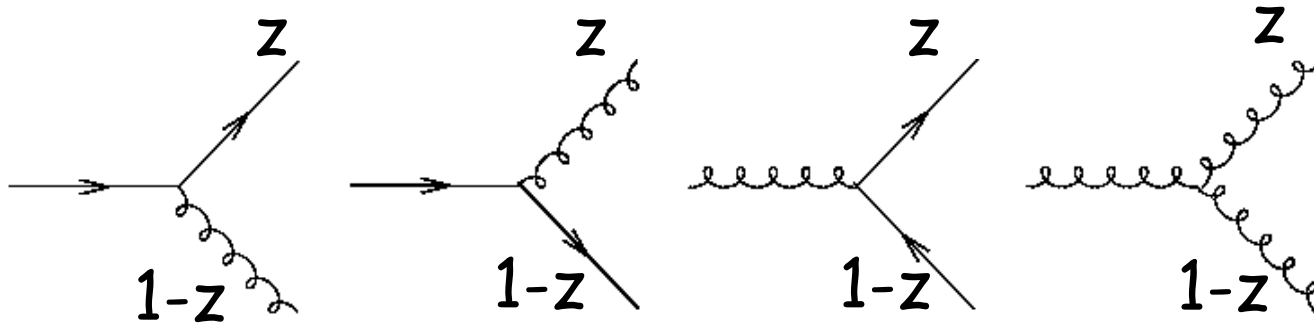
HERA - Early Measurements



Can these observations be related?

QCD Radiation

DGLAP equations are easy to “understand” intuitively, in terms of four “splitting functions”,



$P_{ab}(z)$: the probability that parton **a** will radiate a parton **b** with the fraction z of the original momentum carried by **a**.

Yu.L. Dokshitzer, Sov.Phys. JETP **46** (1977) 641,

V.N. Gribov and L.N.Lipatov, Sov. Journ. Nucl. Phys. **15** (1972) 438; *ibid* **15** (1972) 675

G.Altarelli and G.Parisi, Nucl.Phys. **B126** (1977) 298

QCD Radiation

Schematically, DGLAP equations:

$$\frac{dq_f(x, Q^2)}{d \ln Q^2} = \alpha_s [q_f \otimes P_{qq} + g \otimes P_{gq}]$$

convolution

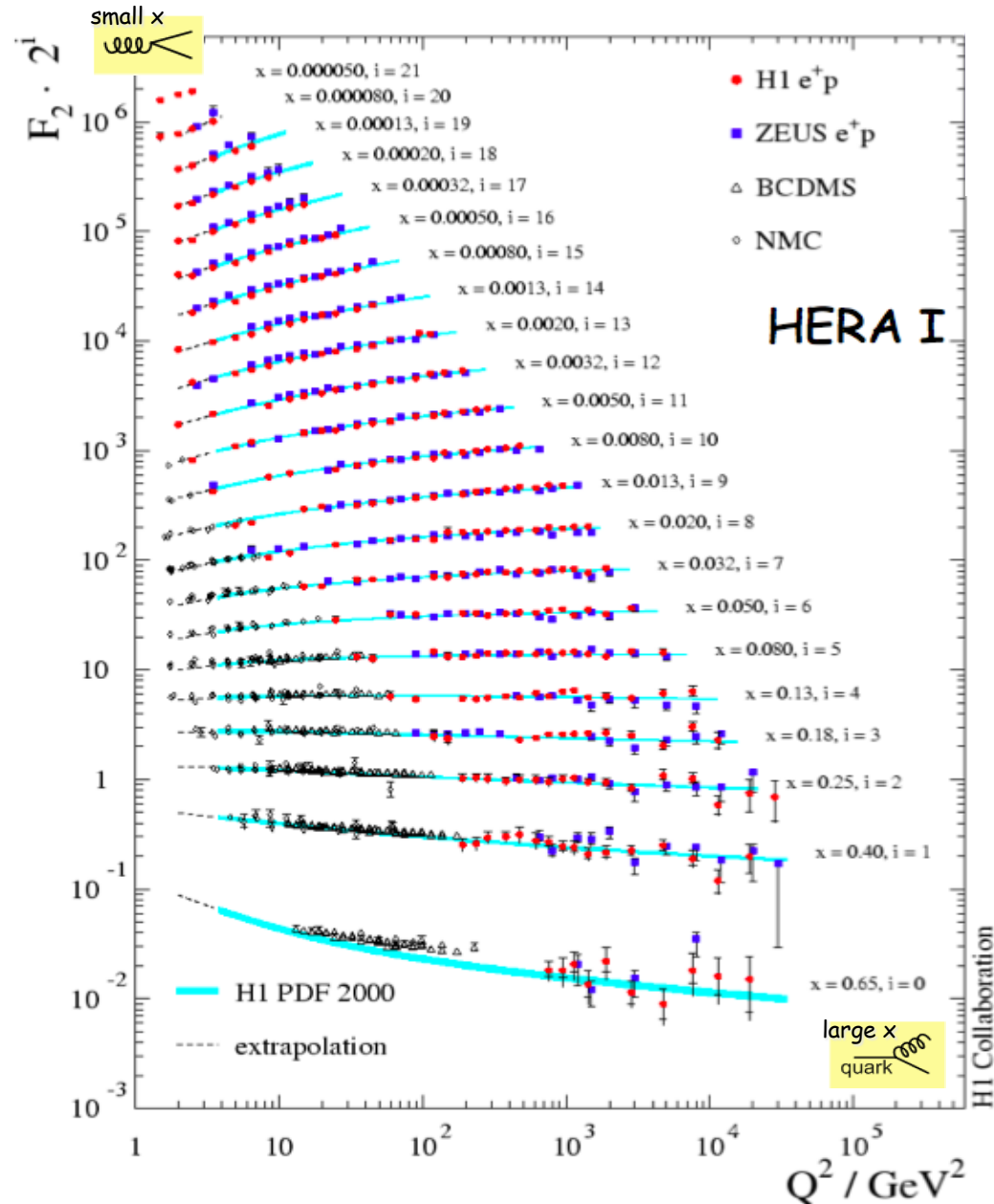
strong coupling constant

That is, the change of quark distribution q with Q^2 is given by the probability that q and g radiate q .

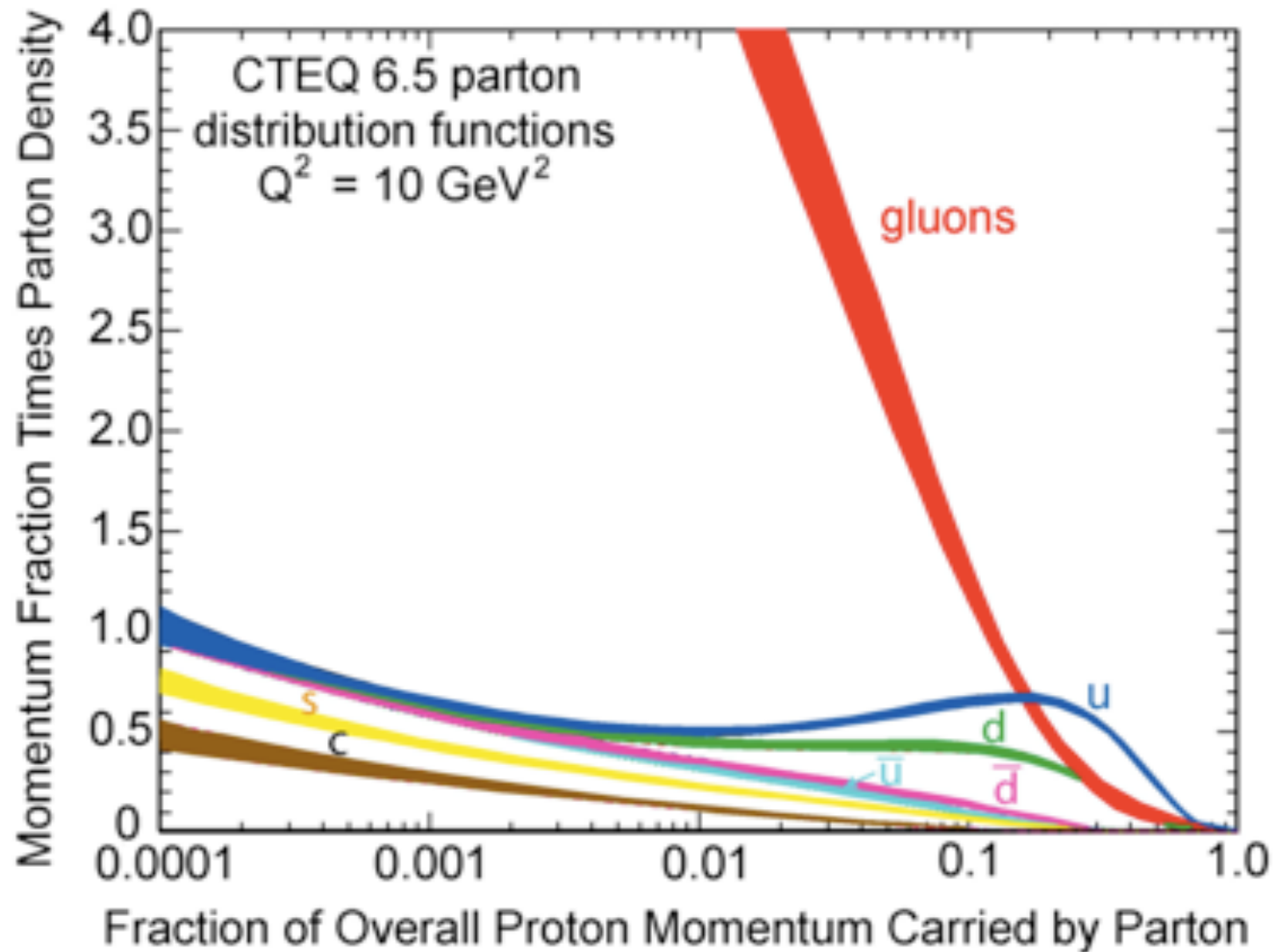
Similarly, for gluons:

$$\frac{dg(x, Q^2)}{d \ln Q^2} = \alpha_s [\sum q_f \otimes P_{qg} + g \otimes P_{gg}]$$

Bjorken scaling and QCD Radiation

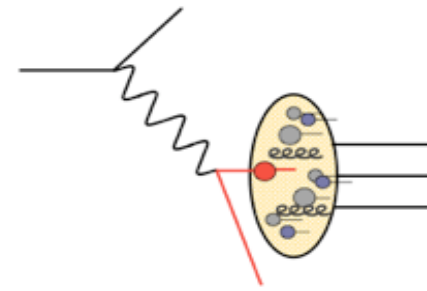


Modern understanding of nucleon composition



Brief Summary:

DIS



DIS probe nucleon or nuclear structure,
described in terms of quarks and gluons,

Feynman's parton model - point like partons, which

behave *incoherently* - combined with QCD radiation are remarkably successful in describing DIS cross sections.

QCD evolution allows one to relate quantitatively processes at different scales Q^2 ,

Parton distributions $f(x)$ are intrinsic properties of the nucleon and (thus) process independent.

This is great for RHIC, LHC, and many other areas.

Gluons are a very significant part of the nucleon

Structure Functions at High x

Valence Quark Distributions

Why Are PDFs at High x Important?

- Valence quark dominance: simpler picture
 - direct comparison with nucleon structure models
 - SU(6) symmetry, broken SU(6), diquark
- $x \rightarrow 1$ region amenable to pQCD analysis
 - hadron helicity conservation?
- Clean connection with QCD, via lattice moments
- Input for search for physics beyond the Standard Model at high energy collider
 - evolution: high x at low $Q^2 \rightarrow$ low x at high Q^2
 - small uncertainties amplified
 - example: HERA 'anomaly' (1998)
- Input to nuclear, high energy and astrophysics calculations

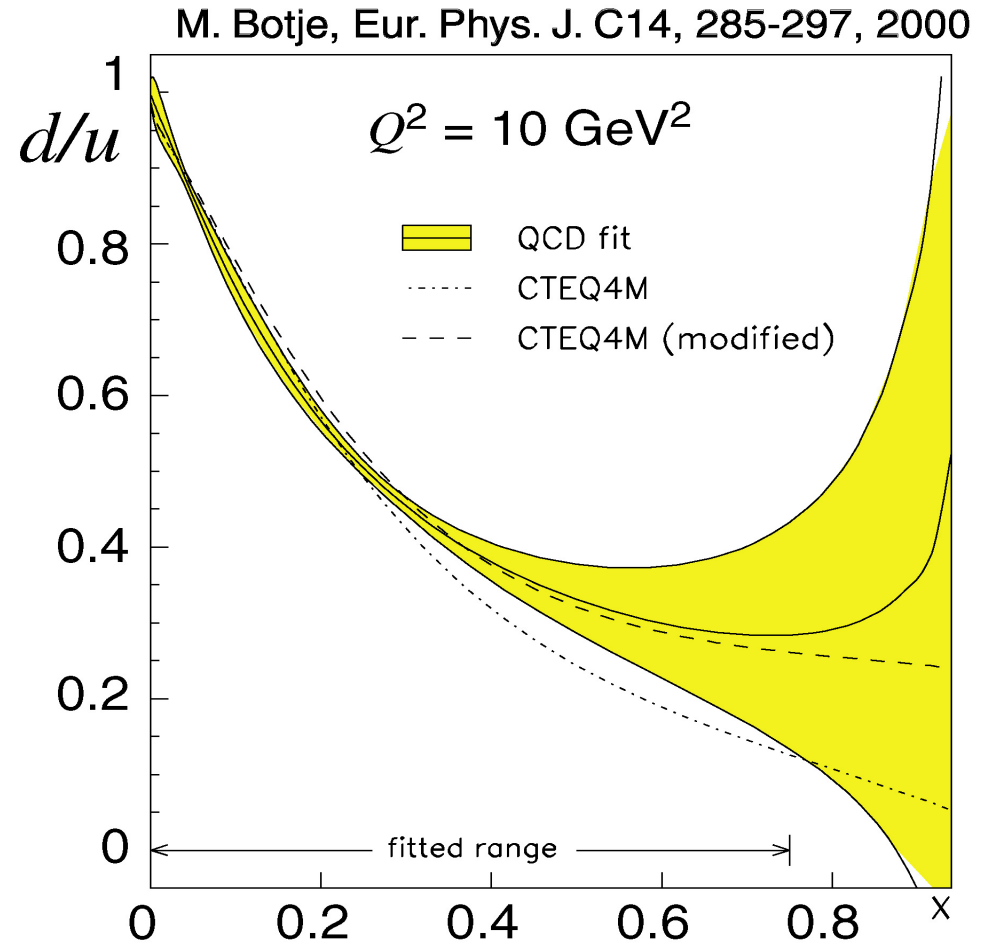
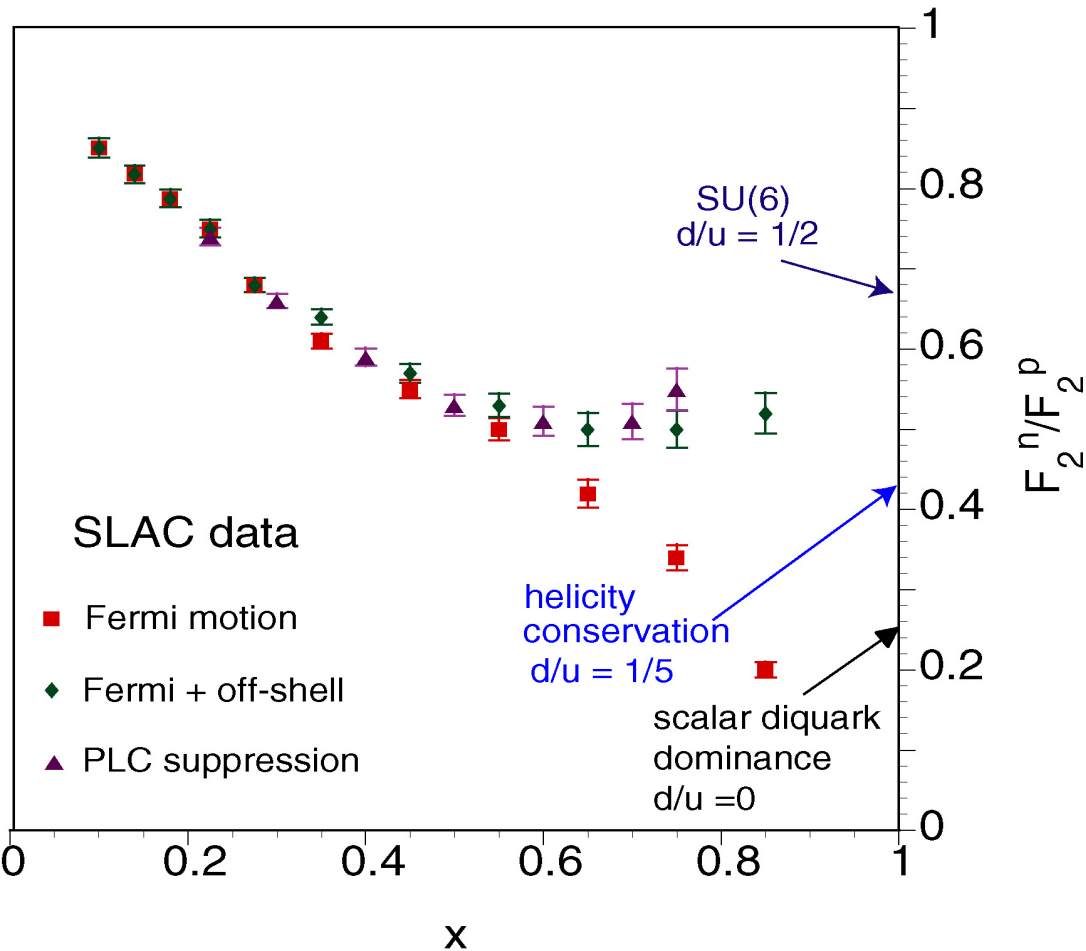
Predictions for High x

Proton Wavefunction (Spin and Flavor Symmetric)

$$\begin{aligned}
 |p \uparrow\rangle = & \frac{1}{\sqrt{2}} |u \uparrow (ud)_{S=0}\rangle + \frac{1}{\sqrt{18}} |u \uparrow (ud)_{S=1}\rangle - \frac{1}{3} |u \downarrow (ud)_{S=1}\rangle \\
 & - \frac{1}{3} |d \uparrow (uu)_{S=1}\rangle - \frac{\sqrt{2}}{3} |d \downarrow (uu)_{S=1}\rangle
 \end{aligned}$$

Nucleon Model	F_2^n/F_2^p	d/u	$\Delta u/u$	$\Delta d/d$	A_1^n	A_1^p
SU(6)	2/3	1/2	2/3	-1/3	0	5/9
Scalar diquark	1/4	0	1	-1/3	1	1
pQCD	3/7	1/5	1	1	1	1

$F_2^n/F_2^p \rightarrow d/u$ ratio at high- x



Hadronic physics output 1: d/u ratio

→ d/u ratio at high x of interest for nonperturbative models of nucleon

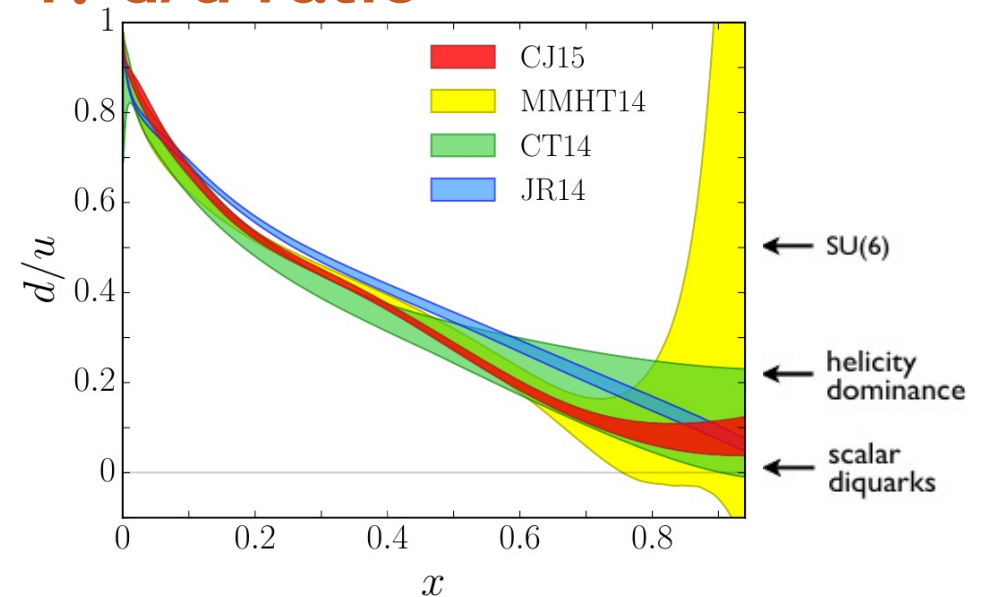
→ **CJ15:**

more flexible parametrization

$$d \rightarrow d + b x^c u$$

allows finite, nonzero $x = 1$ limit

(standard PDF form gives 0 or ∞ unless $a_2^d = a_2^u$)



MMHT14: fitted deuteron corrections
standard d parametrization
→ “UNDERCONSTRAINED”

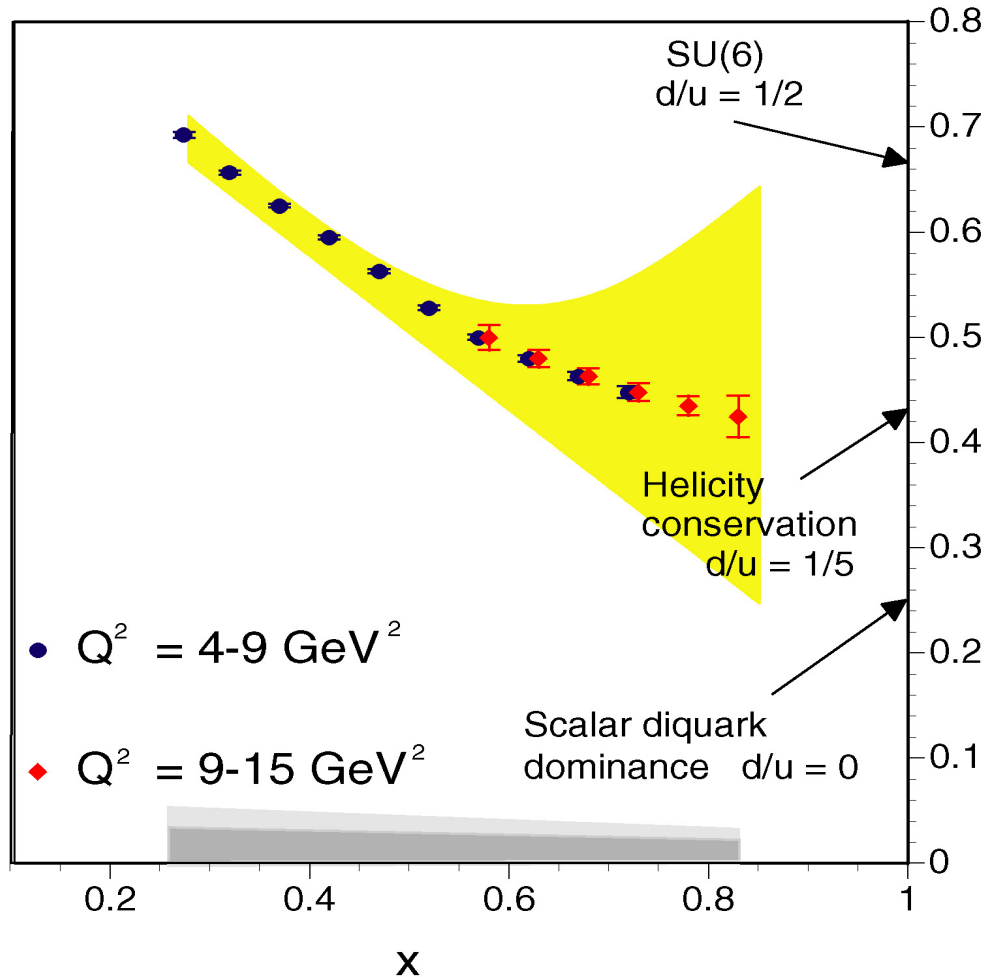
JR14 (and ABM12):

Similar deuteron corrections
standard d ; no lepton/W asym.
→ “OVERCONSTRAINED”

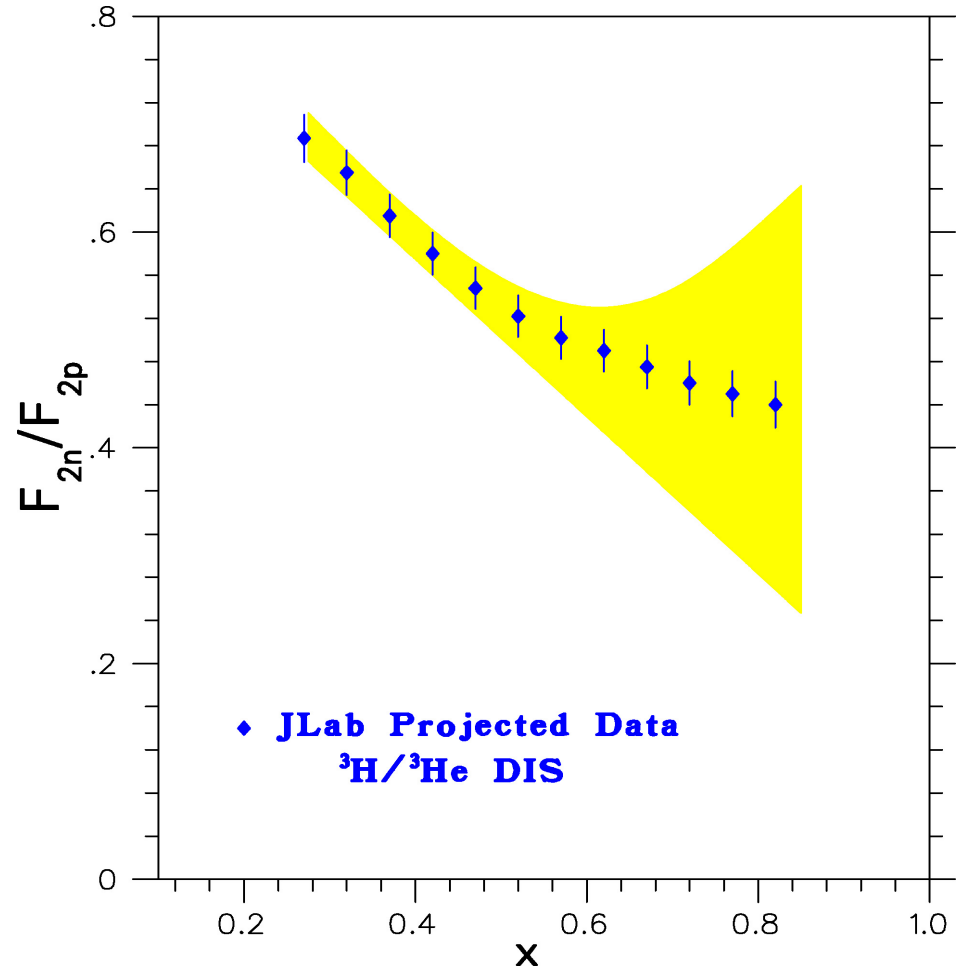
CT14: $\beta_u = \beta_d \implies d/u$ finite
No nuclear corrections

$F_2^n/F_2^p \rightarrow d/u$ ratio at high- x

BONUS at Hall B 11 GeV with CLAS12



Hall A 11 GeV with HRS



Longstanding issue in proton structure

Proton PVDIS: d/u at high x

$$A_{PV} = \frac{G_F Q^2}{\sqrt{2}\pi\alpha} [a(x) + f(y)b(x)]$$

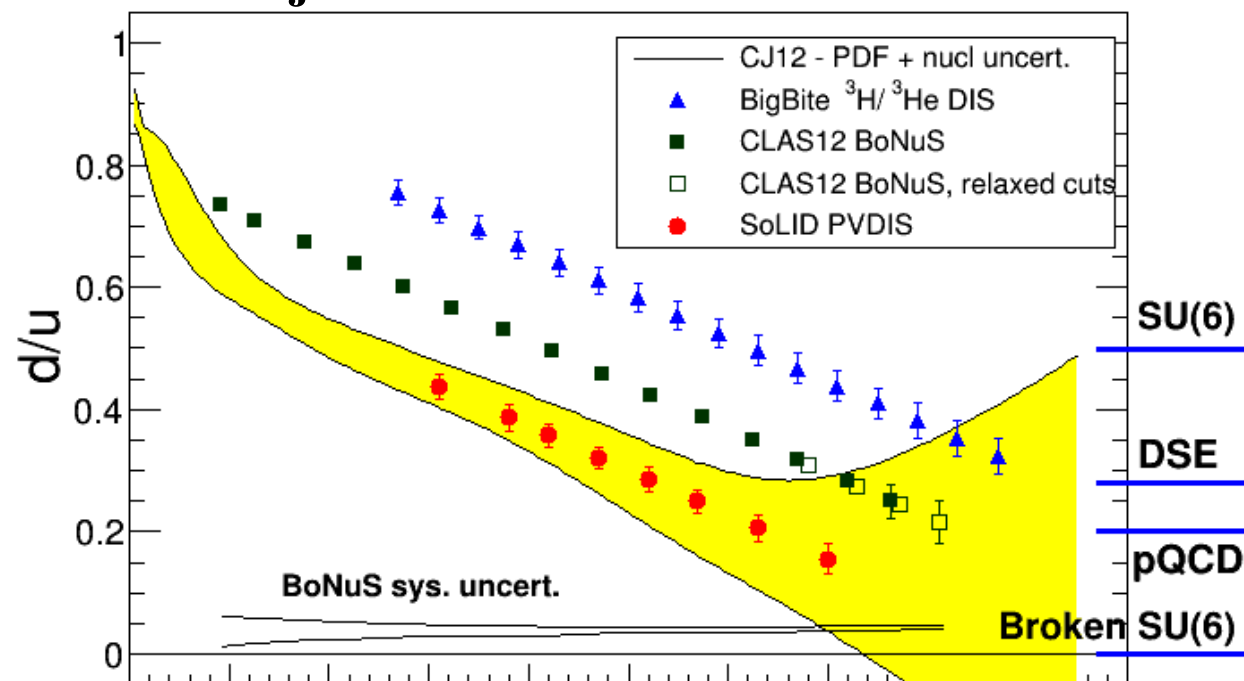
$$a^P(x) \approx \frac{u(x) + 0.91d(x)}{u(x) + 0.25d(x)}$$

SU(6): $d/u \sim 1/2$

Broken SU(6): $d/u \sim 0$

Perturbative QCD: $d/u \sim 1/5$

Projected 12 GeV d/u extractions



- 3 JLab 12 GeV experiments:
 - CLAS12 BoNuS spectator tagging
 - BigBite – DIS $^3\text{H}/^3\text{He}$ ratio
 - **SoLID – PVDIS ep**
- **The SoLID extraction of d/u is directly from ep DIS:**
 - **No nuclear corrections**
 - **No assumption of charge symmetry**

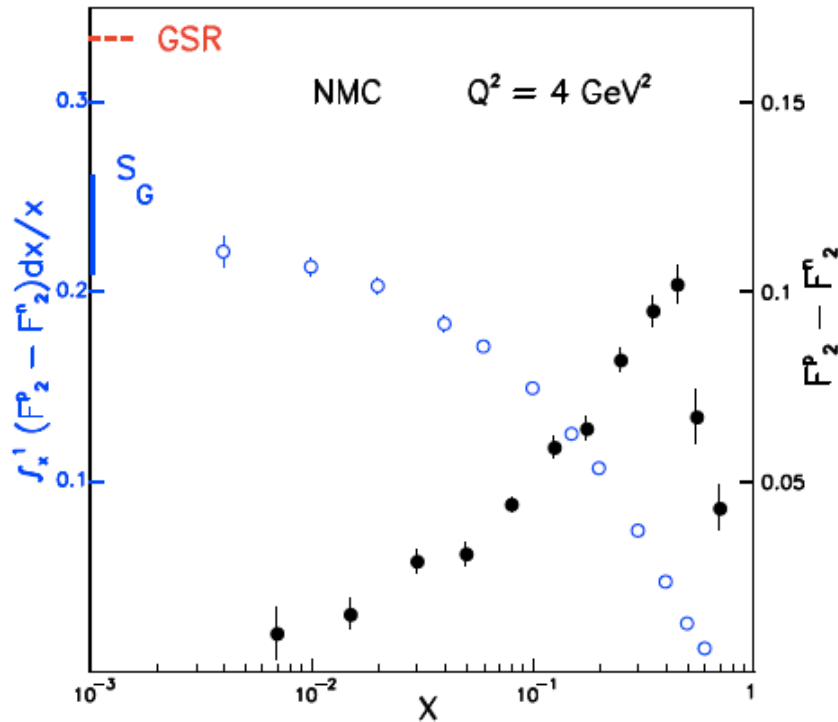
Sea Quark Distributions

Sea Asymmetry (\bar{d}/\bar{u})
Strange Sea

Flavor structure of the proton sea

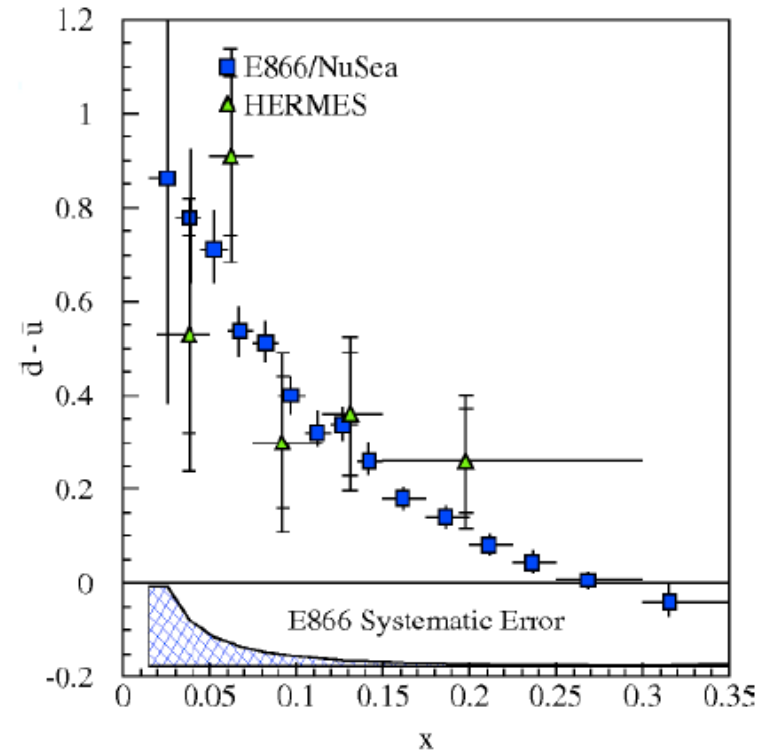
□ The proton sea is not SU(3) symmetric!

Violation of Gottfried sum rule



$$\begin{aligned}
 S_G &= \int_0^1 [(F_2^p(x) - F_2^n(x)) / x] dx \\
 &= \frac{1}{3} + \frac{2}{3} \int_0^1 (\bar{u}_p(x) - \bar{d}_p(x)) dx \\
 &= \frac{1}{3} \quad (\text{if } \bar{u}_p = \bar{d}_p) \quad \text{NMC: } S_G = 0.235 \pm 0.026
 \end{aligned}$$

Confirmed by Drell-Yan exp't

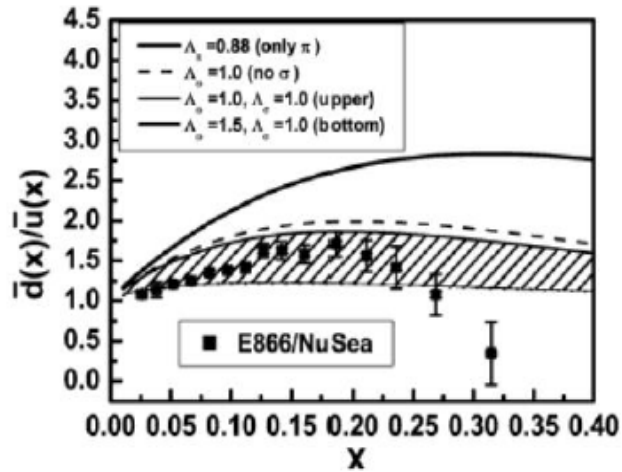


Why $\bar{d}(x) \neq \bar{u}(x)$?

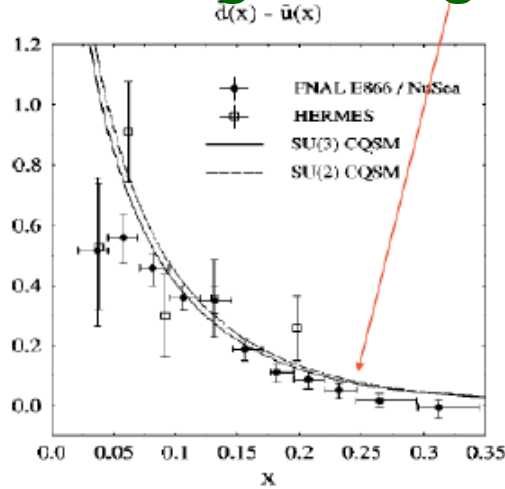
Why does $\bar{d}(x) - \bar{u}(x)$ **change sign?**

Challenges for $\bar{d}(x) - \bar{u}(x)$

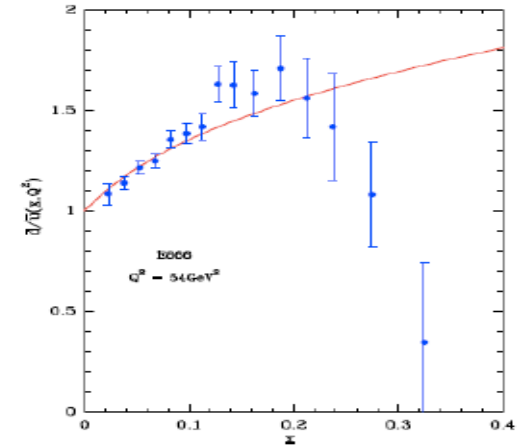
□ All known models predict no sign change!



Meson cloud

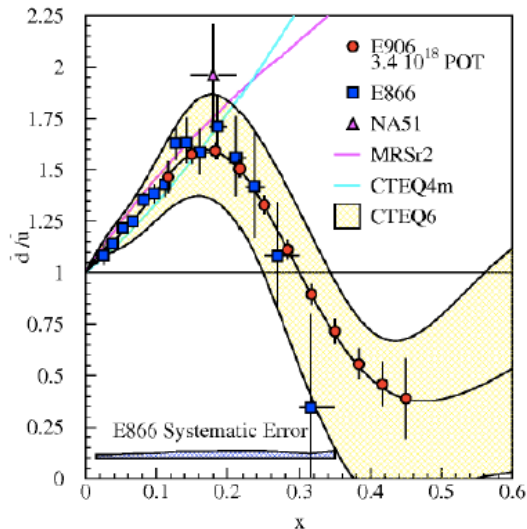


Chiral-quark soliton model

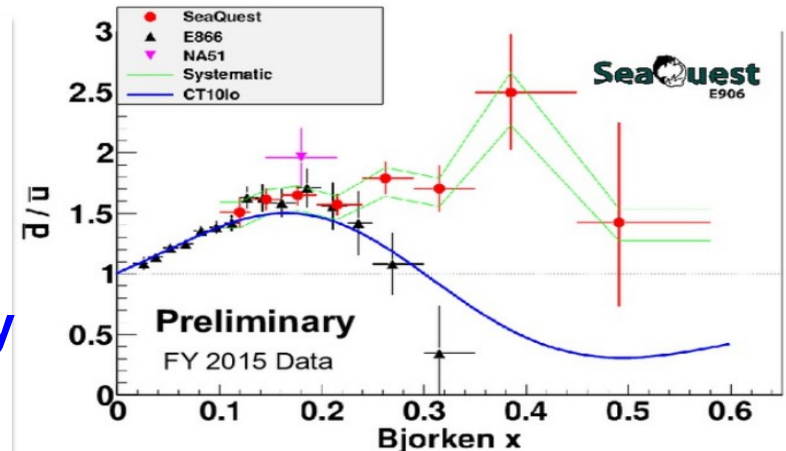


Statistic model

□ Future experiments – E906, ...

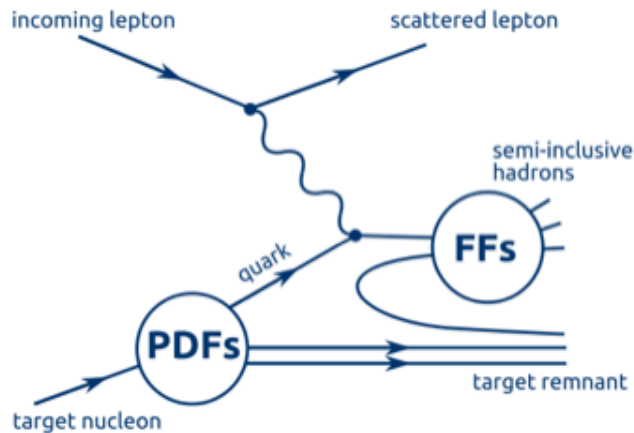


Preliminary
From
Seaquest



B.Kerns, DNP April 2016

Semi-Inclusive DIS



$$Q(x) \equiv u(x) + \bar{u}(x) + d(x) + \bar{d}(x)$$

$$S(x) \equiv s(x) + \bar{s}(x)$$

$$K = K^+ + K^-$$

$$\frac{d^2 N^K(x)}{d^2 N^{DIS}(x)} \stackrel{\text{isoscalar target (D)}}{\underset{\text{LO}}{=}} \frac{\text{Fragmentation function} \quad \text{Parton distribution function} \quad \text{Fragmentation function}}{\text{Parton distribution function}} \frac{Q(x) \int D_Q^K(z) dz + S(x) \int D_S^K(z) dz}{5Q(x) + 2S(x)}$$

= Multiplicities

First Hermes extraction:
Phys.Lett. B666, 446 (2008)

Updated and final data now!

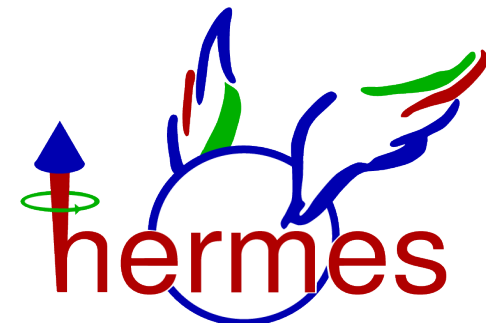
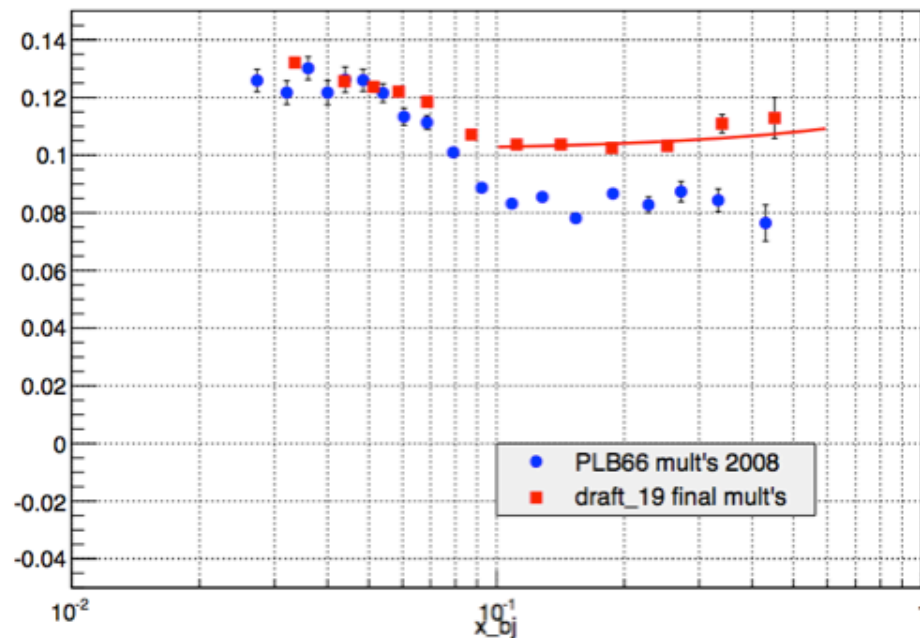
- Q^2 Negative squared 4-momentum transfer to the target
- X Parton fractional momentum
- Z Fractional energy transfer to the produced hadron
- $P_{h\perp}$ Hadron transverse momentum with respect to the virtual photon direction



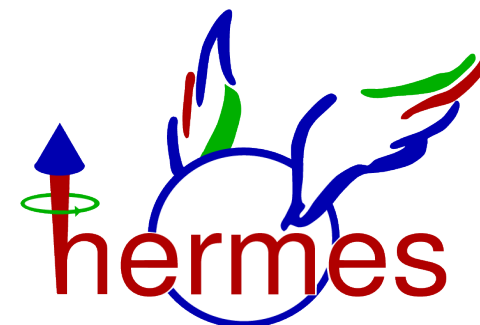
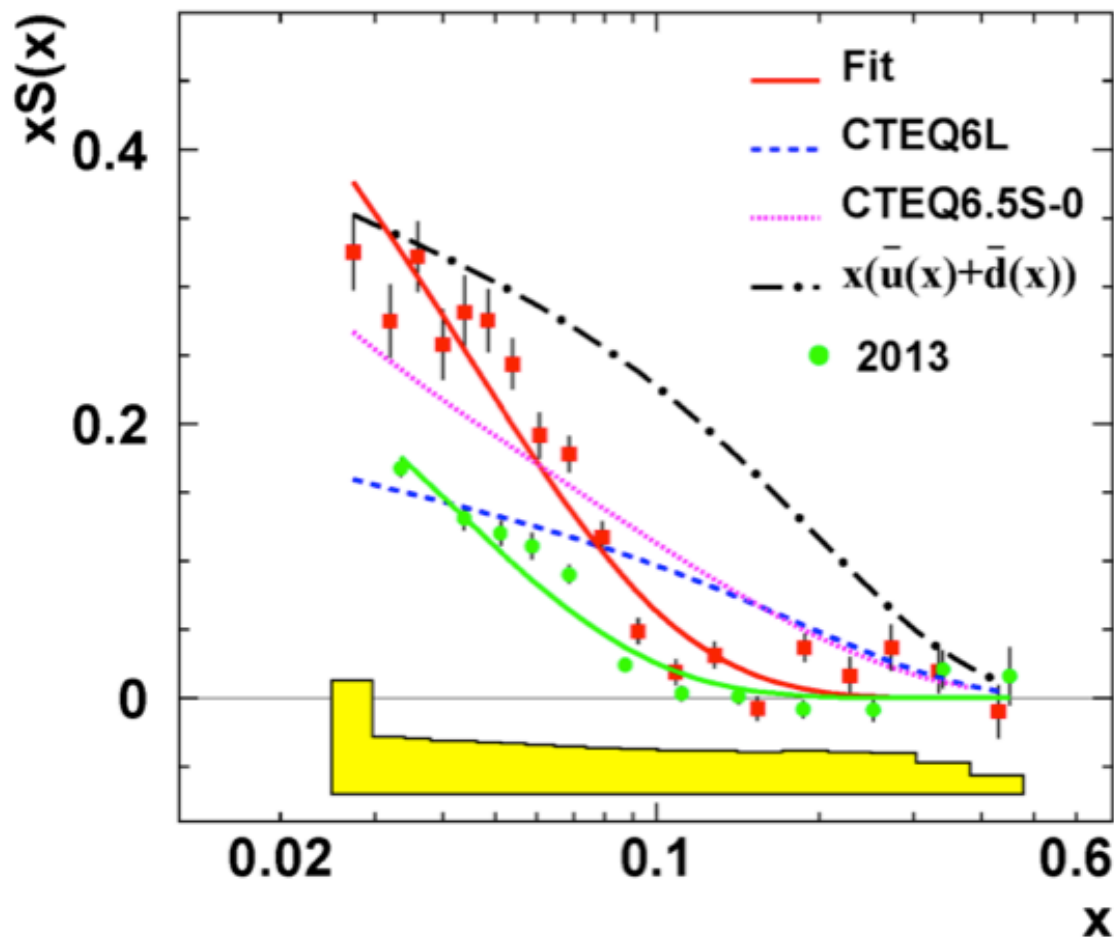
New multiplicities

- More data (~ factor 2)
- New 3-dimensional (x - z - $P_{h\perp}$) unfolding to correct for acceptance, radiative effects, smearing, decay in flight and secondary strong interactions
- Final 3-dimensional results corrected to 4π Born

kaon multiplicities, plb66 vs 2012



Old versus new $S(x)$



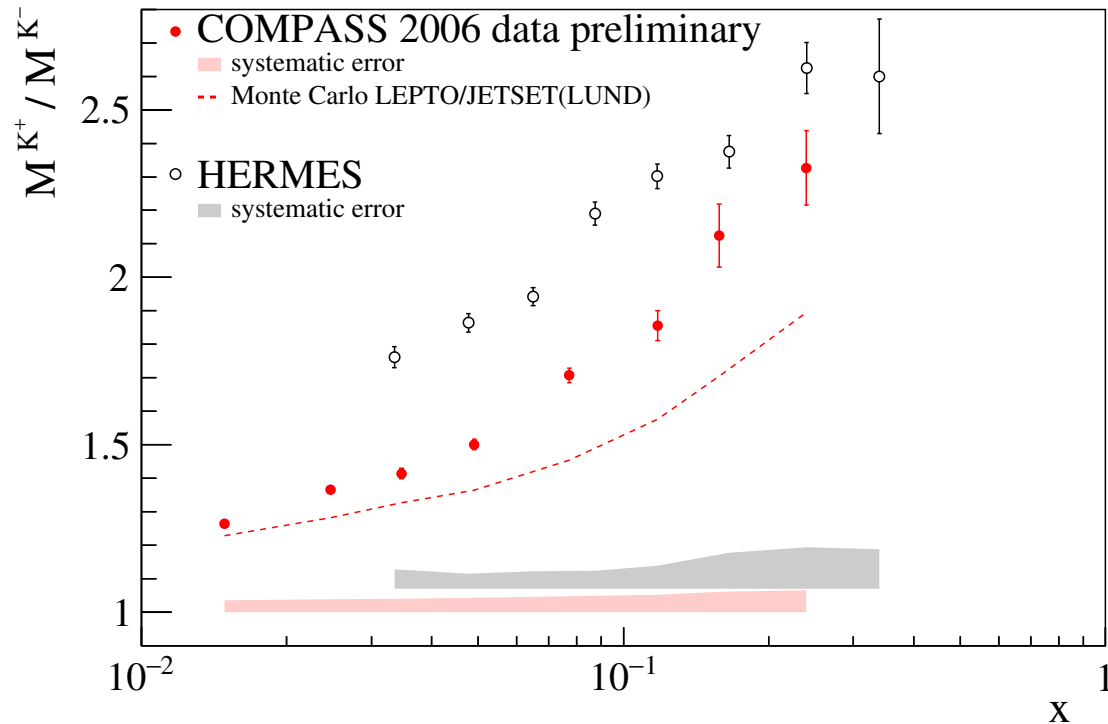
Kaon multiplicity ratio



- π case, there is a good agreement between COMPASS and HERMES for the π^+/π^- multiplicity ratio

Despite the difference in the shape of π multiplicity sum

- **K** case: clear discrepancy between COMPASS and HERMES even for the K^+/K^- multiplicity ratio
- DSS next fit of Kaon FF



Summary

- Electron Scattering to study Nucleon Structure
- Elastic: Form Factors
 - charge/current distributions
 - transverse density
 - G_E^p @ large Q^2 surprise \rightarrow shape of proton, 2- γ effects
 - proton radius puzzle
- Deep-Inelastic Scattering
 - Unpolarized Structure functions \rightarrow Parton Distributions
 - High-x, valance quark distributions, d/u
 - Sea distributions: $d_{\text{bar}}/u_{\text{bar}}$ asymmetry
 - poor knowledge on strange sea