

# **QCD in Collisions with Polarized Beams**

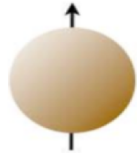
**Jianwei Qiu  
Brookhaven National Laboratory  
Stony Brook University**

**Annual Hua-Da School on QCD: EIC physics**

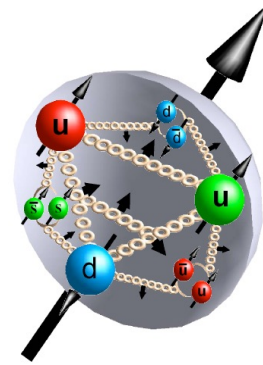
**China Central Normal University (CCNU), Wuhan, China, May 23 – June 3, 2016**

# Summary of lecture five

- Key for a good proton spin decomposition – sum rule:



$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + (L_q + L_g)$$



- ✧ Every term can be related to a physical observable with controllable approximation – “independently measurable”

*DIS scheme is ok for F2, but, less effective for other observables*

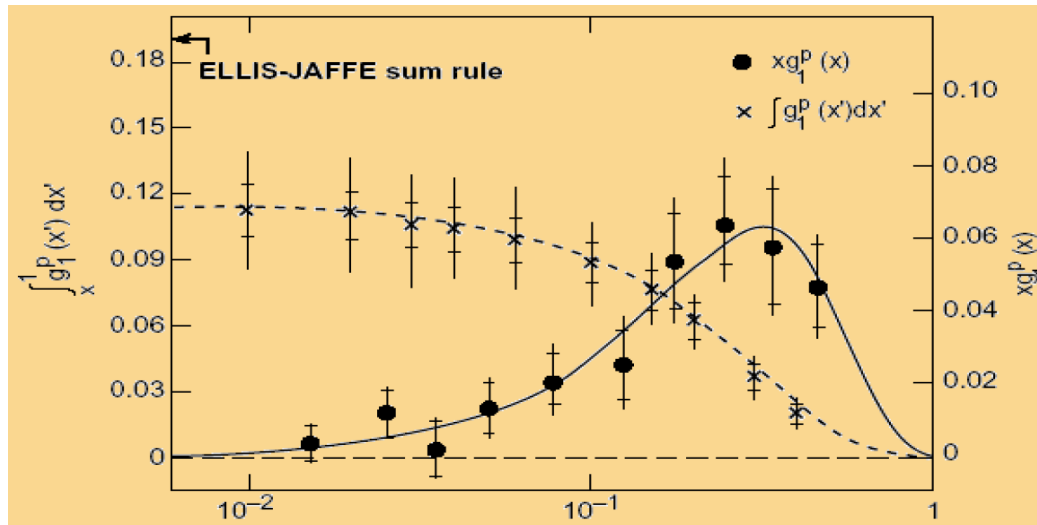
*Additional symmetry constraints, leading to “better” decomposition?*

- ✧ Natural physical interpretation for each term – “hadron structure”
  - ✧ Hopefully, calculable in lattice QCD – “numbers w/o distributions”
- Since the “spin crisis” in the 80<sup>th</sup>, we have learned a lot about proton spin – likely, we will need for orbital contribution

**Thank you!**

# Proton “spin crisis” – excited the field

## □ EMC (European Muon Collaboration '87) – “the Plot”:



$$g_1(x) = \frac{1}{2} \sum_q e_q^2 [\Delta q(x) + \Delta \bar{q}(x)] + \mathcal{O}(\alpha_s) + \mathcal{O}(1/Q)$$

✧ Combined with earlier SLAC data:

$$\int_0^1 g_1^p(x) dx = 0.126 \pm 0.018$$

✧ Combined with:  $g_A^3 = \Delta u - \Delta d$  and  $g_A^8 = \Delta u + \Delta d - 2\Delta s$

from low energy neutron & hyperon  $\beta$  decay

➡ 
$$\Delta\Sigma = \sum_q [\Delta q + \Delta \bar{q}] = 0.12 \pm 0.17$$

## □ “Spin crisis” or puzzle:

- ✧ Strange sea polarization is sizable & negative
- ✧ Very little of the proton spin is carried by quarks

➡ *New era of spin physics*

# Proton spin decomposition

## □ The “big” question:

If there are infinite possibilities, why bother and what do we learn?

## □ The “origin” of the difficulty/confusion:

QCD is a gauge theory: a pure quark field in one gauge is a superposition of quarks and gluons in another gauge

## □ The fact:

None of the items in all spin decompositions are **direct** physical observables, unlike cross sections, asymmetries, ...


## □ Ambiguity in interpretation – two old examples:

### ✧ Factorization scheme:

$$F_2(x, Q^2) = \sum_{q, \bar{q}} C_q^{\text{DIS}}(x, Q^2/\mu^2) \otimes q^{\text{DIS}}(x, \mu^2) \quad \text{No glue contribution to } F_2?$$

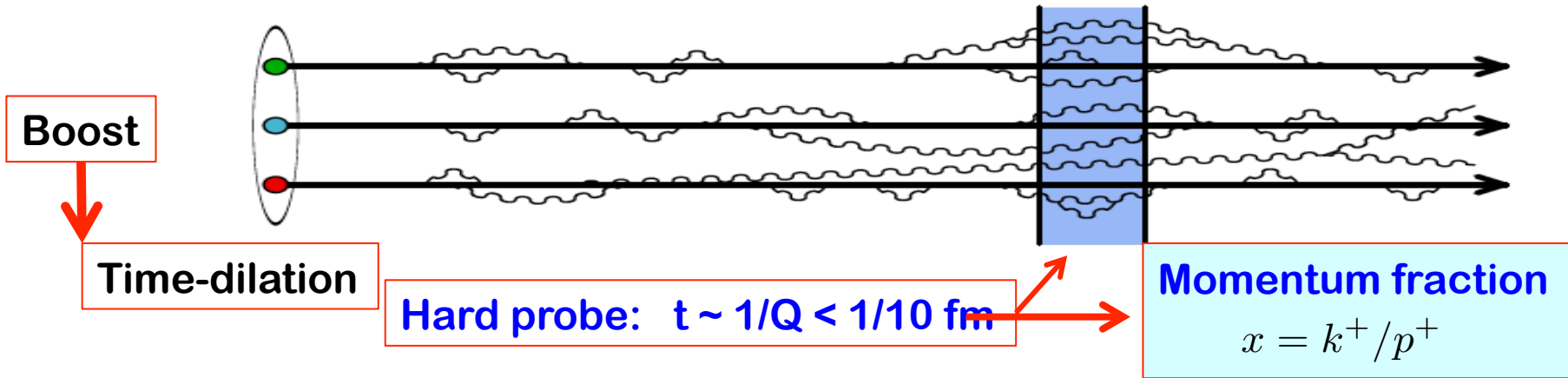
### ✧ Anomaly contribution to longitudinal polarization:

$$g_1(x, Q^2) = \sum_{q, \bar{q}} \tilde{C}_q^{\text{ANO}} \otimes \Delta q^{\text{ANO}} + \tilde{C}_g^{\text{ANO}} \otimes \Delta G^{\text{ANO}}$$

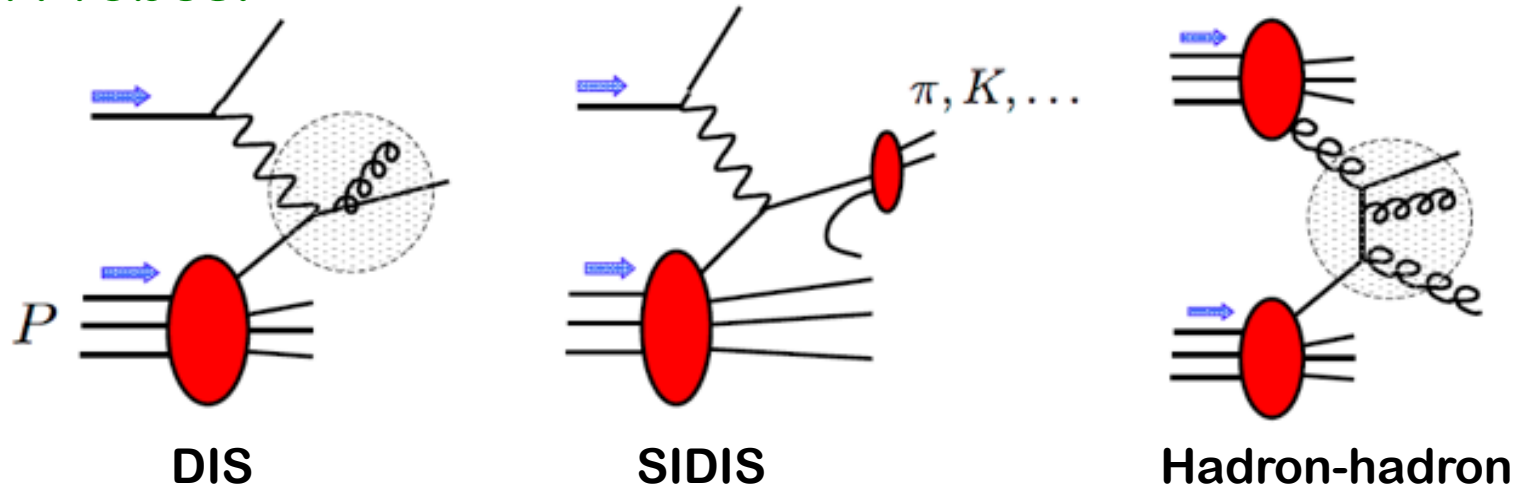
  $\Delta\Sigma \longrightarrow \Delta\Sigma^{\text{ANO}} - \frac{n_f \alpha_s}{2\pi} \Delta G^{\text{ANO}}$  *Larger quark helicity?*

# Probes and facilities

- High energy scattering – to see quarks and gluons:



- Spin Probes:



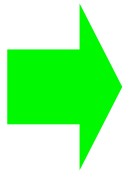
HEMES, COMPASS, JLab, Future EIC, ...

RHIC, FermiLab, JPAC, ...

# Earlier “solution” to the “crisis”

- Large  $\Delta G$  to cancel the “true”  $\Delta q$ :

$$\Delta q = \int_0^1 dx \Delta q(x) = \langle P, s_{\parallel} | \bar{\psi}_q(0) \gamma^+ \gamma_5 \psi_q(0) | P, s_{\parallel} \rangle$$



$$\Delta\Sigma \rightarrow \Delta\Sigma - \frac{n_f \alpha_s(Q^2)}{2\pi} \Delta G(Q^2)$$

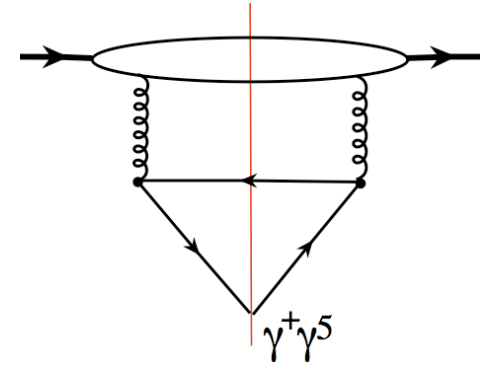
- What value of  $\Delta G$  is needed?

$$\Delta G(Q^2) \sim 2 \quad \text{at } Q \sim 1 \text{ GeV}$$

- Question: How to measure  $\Delta G$  independently?

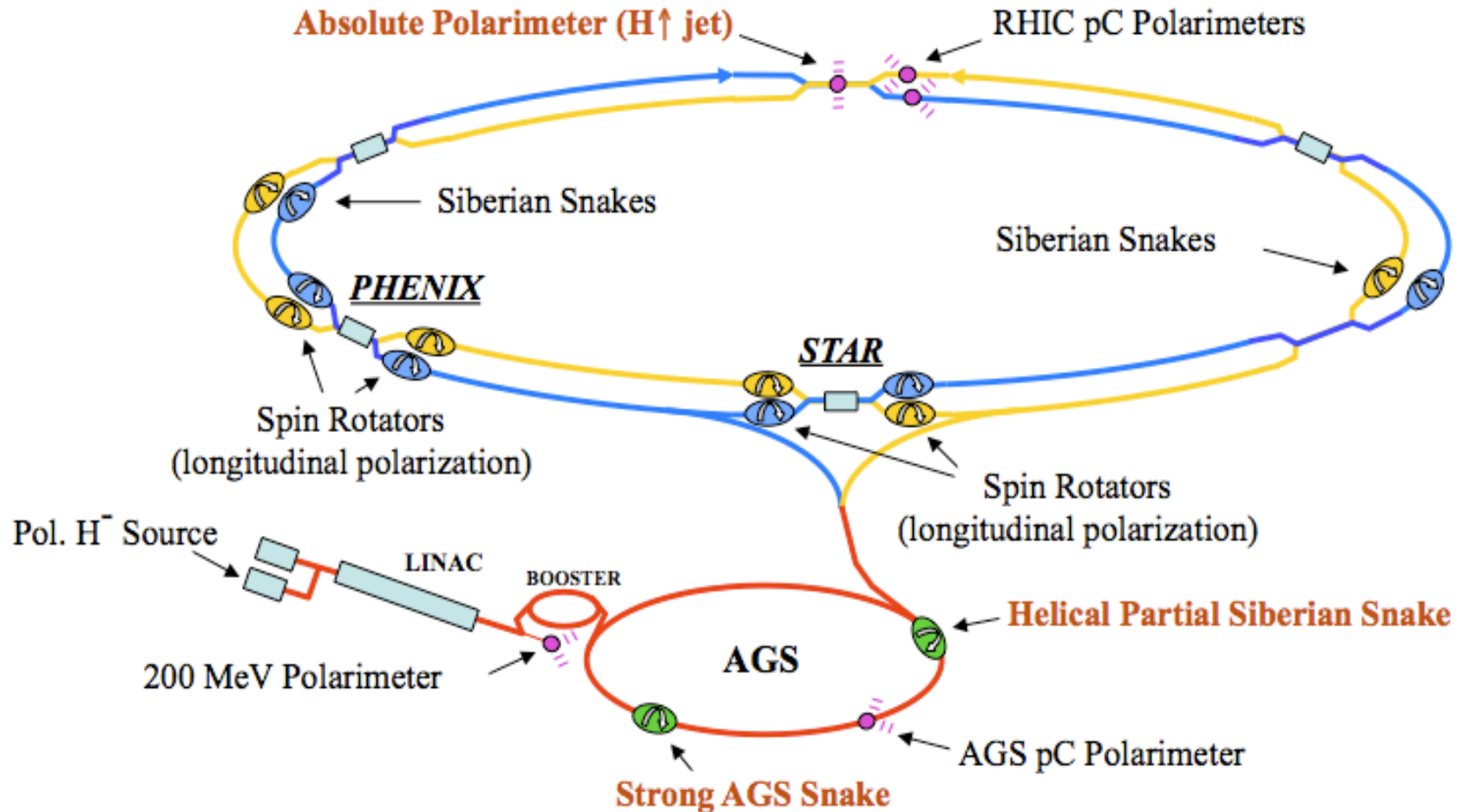
- ✧ Precision inclusive DIS
- ✧ Jets in SIDIS
- ✧ Hadronic collisions – RHIC spin, ...

*Lead to the first goal of RHIC spin program*



# RHIC spin program

## □ The machine:



Collider of two 100 GeV (250 GeV) polarized proton beams

# RHIC spin program

## Research

## Status

## Plans for 1

In this report we present the current status of the RHIC spin program and the evolution of the spin program.

The following is meant to provide an overview of the 2007 Nuclear Physics Division presentation in the 2005 1

<http://spi:>

Christine Aidala<sup>a</sup>, Mei Abhay Deshpande<sup>c,e</sup>, Matthias Grosse Perde Kistenev<sup>b</sup>, Stefan Kretzschmar<sup>b</sup>, Vladimir Rykov<sup>b</sup>, Nac Surrow<sup>a</sup>, Atsushi Takahashi<sup>b</sup>, Fleming Videbaek<sup>b</sup>, St

In addition to the material presented here, the development of polarized proton beams is a developing area of the program, both for proton helicity and for

Gerry Bunce and Werner Bruns, Deshpande, Wolfram Fischer, Bernd Surrow (see also: authors of Res

This report gives a RHIC spin program that will significantly advance our understanding of the spin structure of the nucleon. It is expected that the program will lead to a precision stage studying the spin structure of the nucleon.

The entire plan rests on the continued running of the RHIC. It is necessary to build the level of polarization required by the experiment. Support for development of the program is envisioned for beyond 2007.

Written by Gerry Bunce and the RHIC Spin Program

Gerry Bunce (chair), Alex Gagliardi, Yuji Goto, Matt Roser, Ralf Seidl, Jim Sowa

Elke-Caroline Aschauer, Carl Gagliardi, Itaru Nakagawa

January 2015



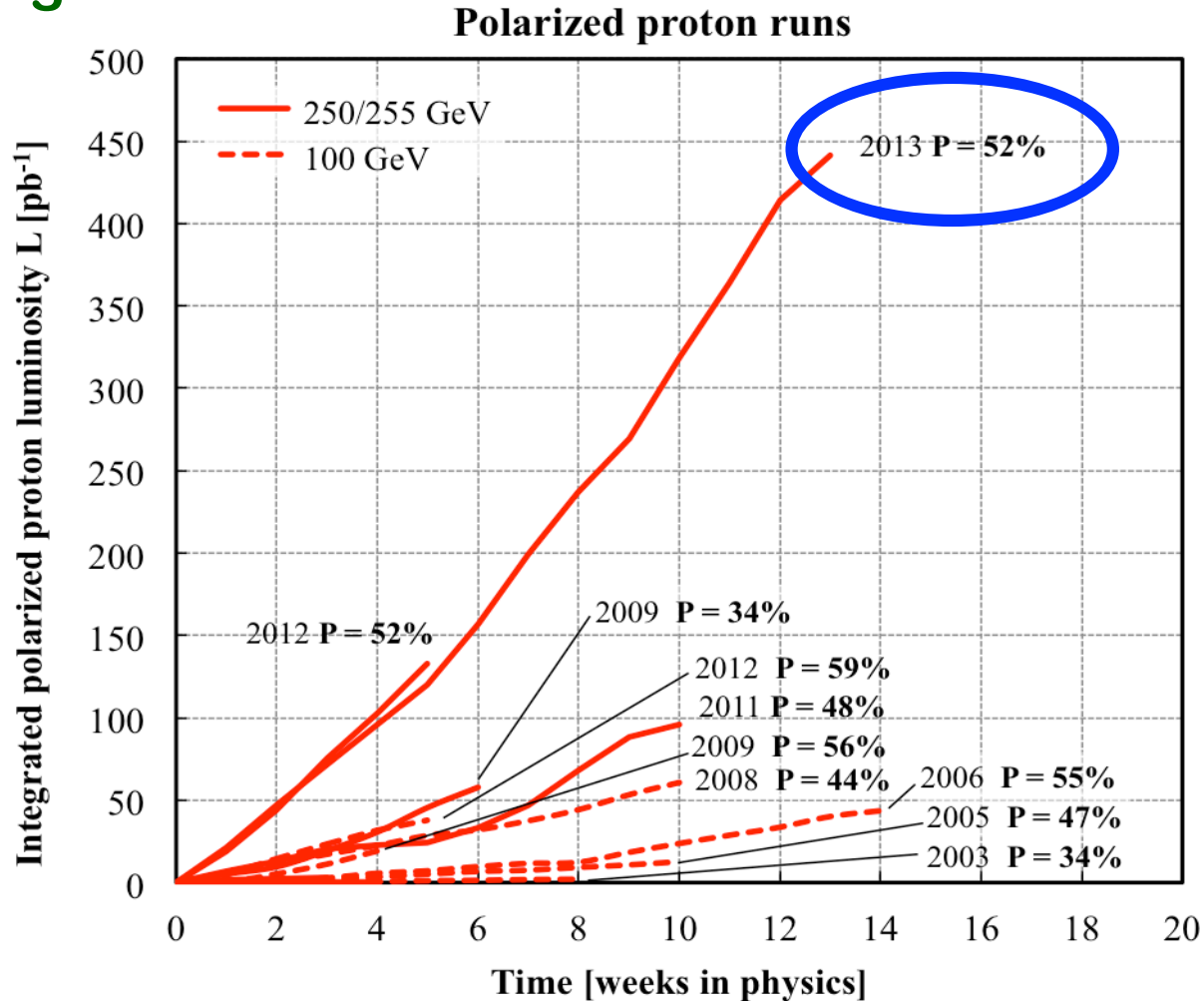


# Goals of RHIC spin program

- Determination of polarized gluon distribution ( $\Delta G$ ) over a large range of momentum fraction  $x$ , using multiple probes
- Determination of flavor identified quark and anti-quark polarization using parity violating production of  $W^\pm$
- Transverse spin phenomena in QCD:  
transversity ( $\delta q$ ), parton orbital angular momentum ( $L_q$ ),  
and etc.

# What has RHIC delivered?

## □ Learning curve:



## □ Maturity and discovery:

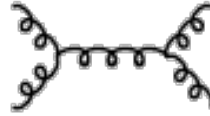
What a year of 2013!

# RHIC Measurements on $\Delta G$

## Physical channels sensitive to $\Delta G$ :

$$\bar{p} + \bar{p} \rightarrow \pi + X$$

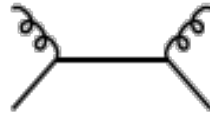
$$\bar{g}\bar{g} \rightarrow gg$$



Pion or jet production

$$\bar{p} + \bar{p} \rightarrow \text{jet} + X$$

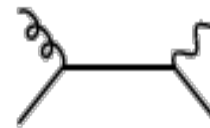
$$\bar{q}\bar{g} \rightarrow qg$$



high rates

$$\bar{p} + \bar{p} \rightarrow \gamma + X$$

$$\bar{q}\bar{g} \rightarrow \gamma q$$



Direct photon production

$$\bar{p} + \bar{p} \rightarrow \gamma + \text{jet} + X$$

low rates

$$\bar{p} + \bar{p} \rightarrow D + X$$

$$\bar{g}\bar{g} \rightarrow c\bar{c}$$



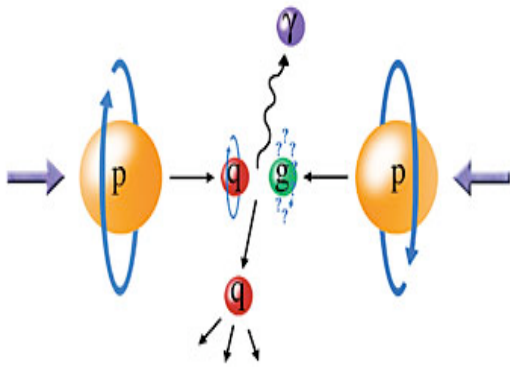
Heavy-flavour production

$$\bar{p} + \bar{p} \rightarrow B + X$$

$$\bar{g}\bar{g} \rightarrow b\bar{b}$$

separated vertex detection  
required

## Collinear QCD factorization:

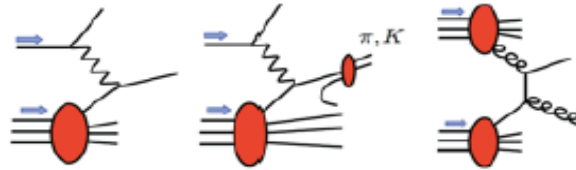


Experiments measure cross sections,  
And asymmetries, not helicity distributions!

*QCD global analyses to extract the best  
helicity distributions at NLO, to calculate  
helicity contribution to proton spin*

# Global fits for helicity PDFs @ NLO

Stratmann's talk  
@BNL Users



*uncertainties*

*last update*

## NNPDF

Ball, Forte, Guffanti, Nocera, Rodolfi, Rojo



100 replicas  
stat. approach

1303.7236

## DSSV

de Florian, Sassot, MS, Vogelsang



L.M.  $\Delta\chi^2 = 8$  (1)  
(Hessian  $\Delta\chi^2 = 1$ )

0904.3821

[DSSV+/++: 1112.0904  
1304.0079]

## LSS

Leader, Sidorov, Stamenov



Hessian  $\Delta\chi^2 = 1$

1010.0574

## BB

Blumlein, Bottcher



Hessian  $\Delta\chi^2 = 1$

1010.3113

⋮

⋮

⋮

## GRSV

Gluck, Reya, MS, Vogelsang



1<sup>st</sup> NLO analysis

9508347

## JAM

PoS DIS2013 (2013) 208

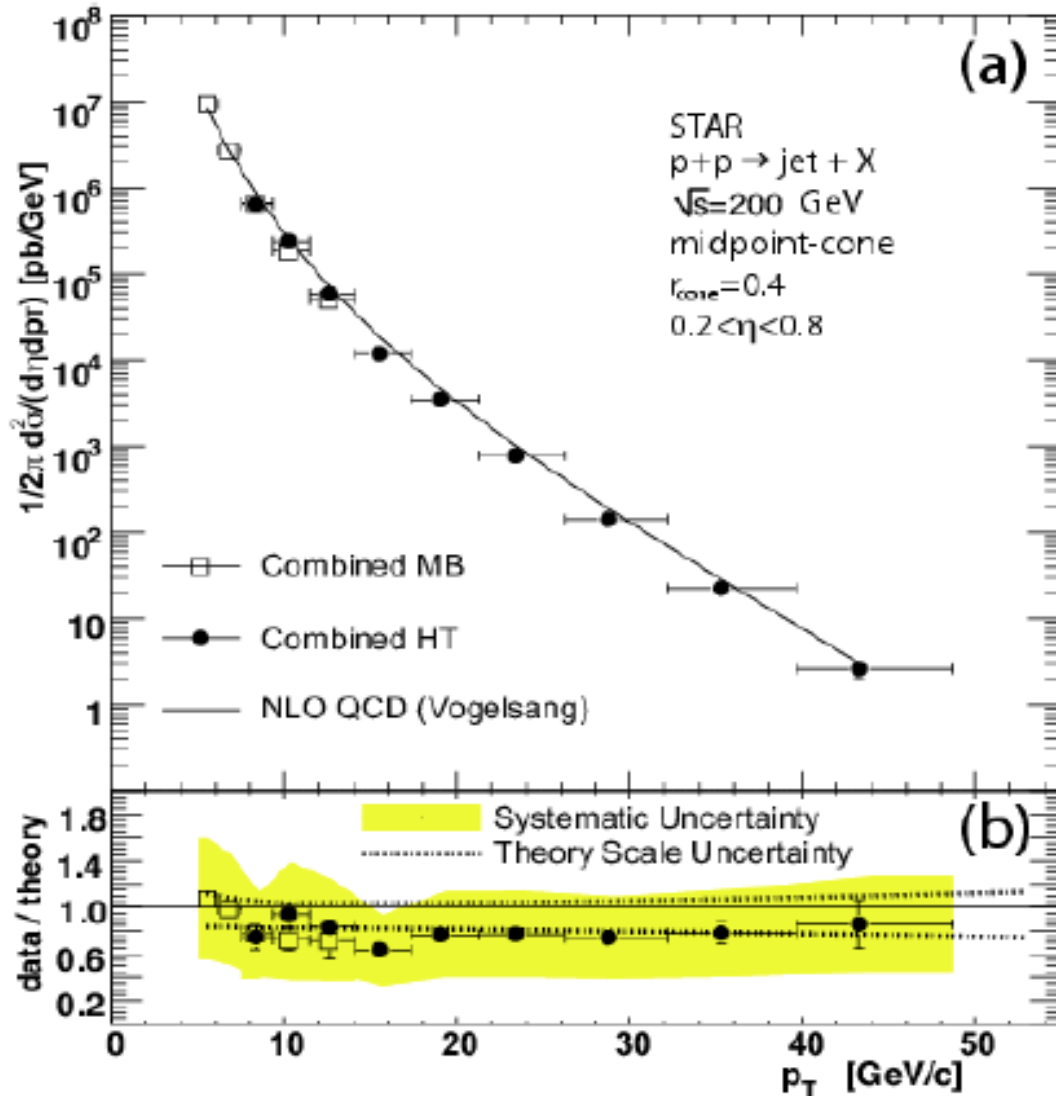


TMC, HT, ...

Accardi's talk on Tue

# Inclusive jet at 200 GeV

□ STAR:

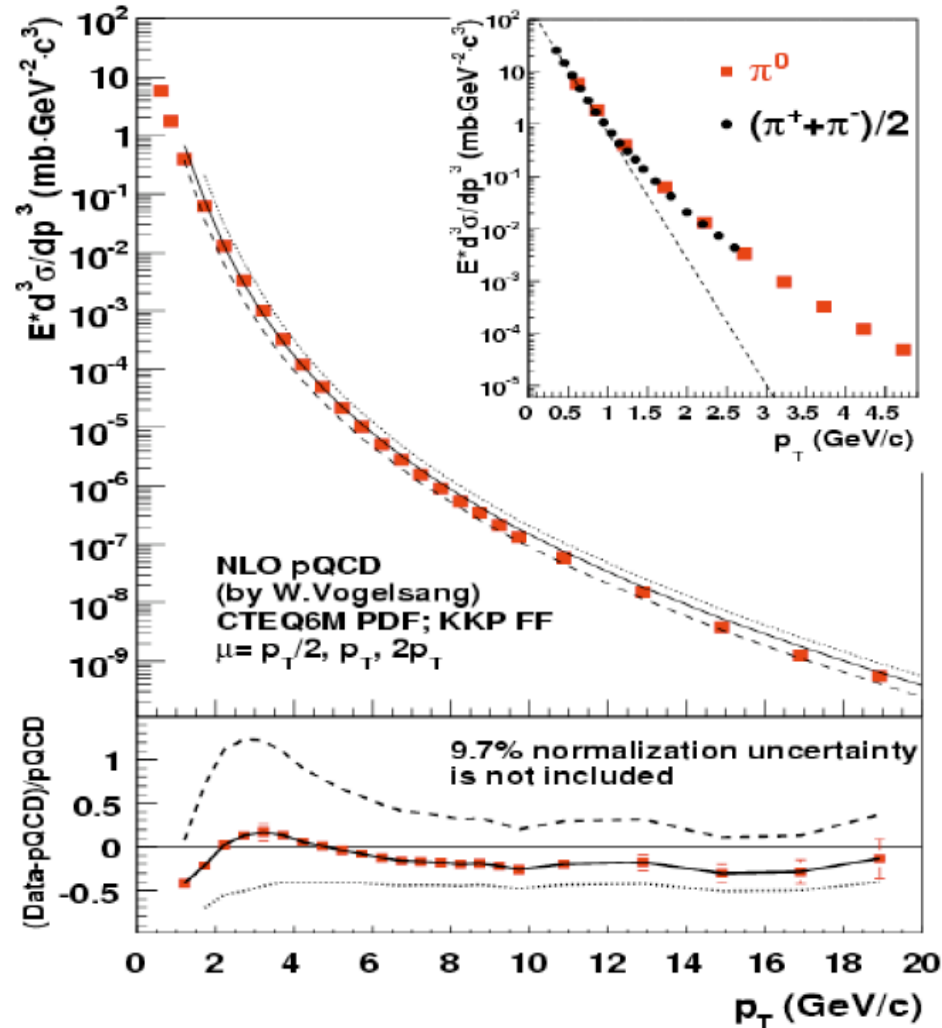


PRL97, 252001  
(2006)

QCD factorization/calculation works at RHIC energies!

# Inclusive single hadron at 200 GeV

□ PHENIX:



PRD76, 051106  
(2007)

QCD factorization/calculation works at RHIC energies!

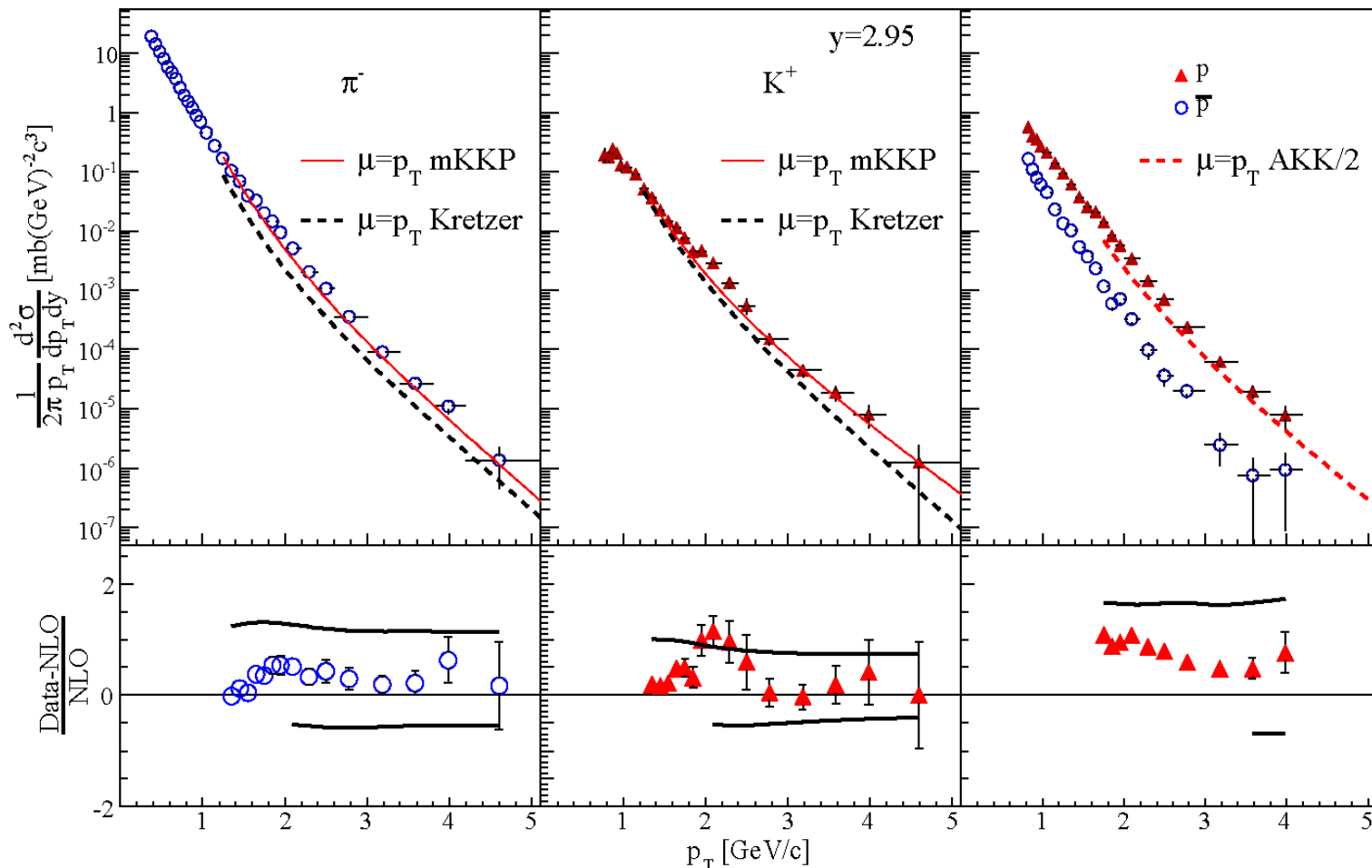
# Extend x coverage and particle type

□ BRAHMS:

Large rapidity p,K,p cross sections for p+p,

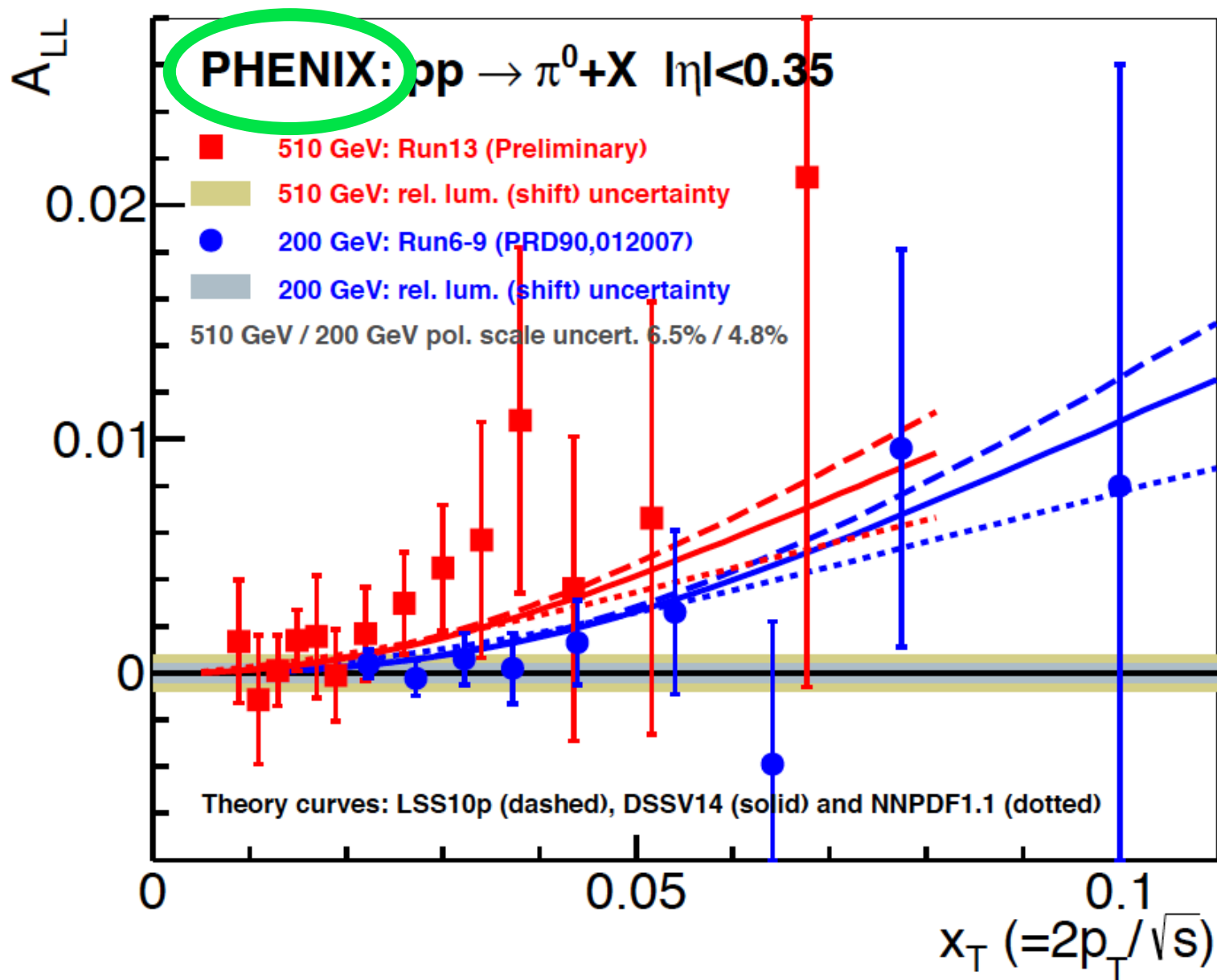
$\sqrt{s}=200$  GeV

PRL98, 252001 (2007)



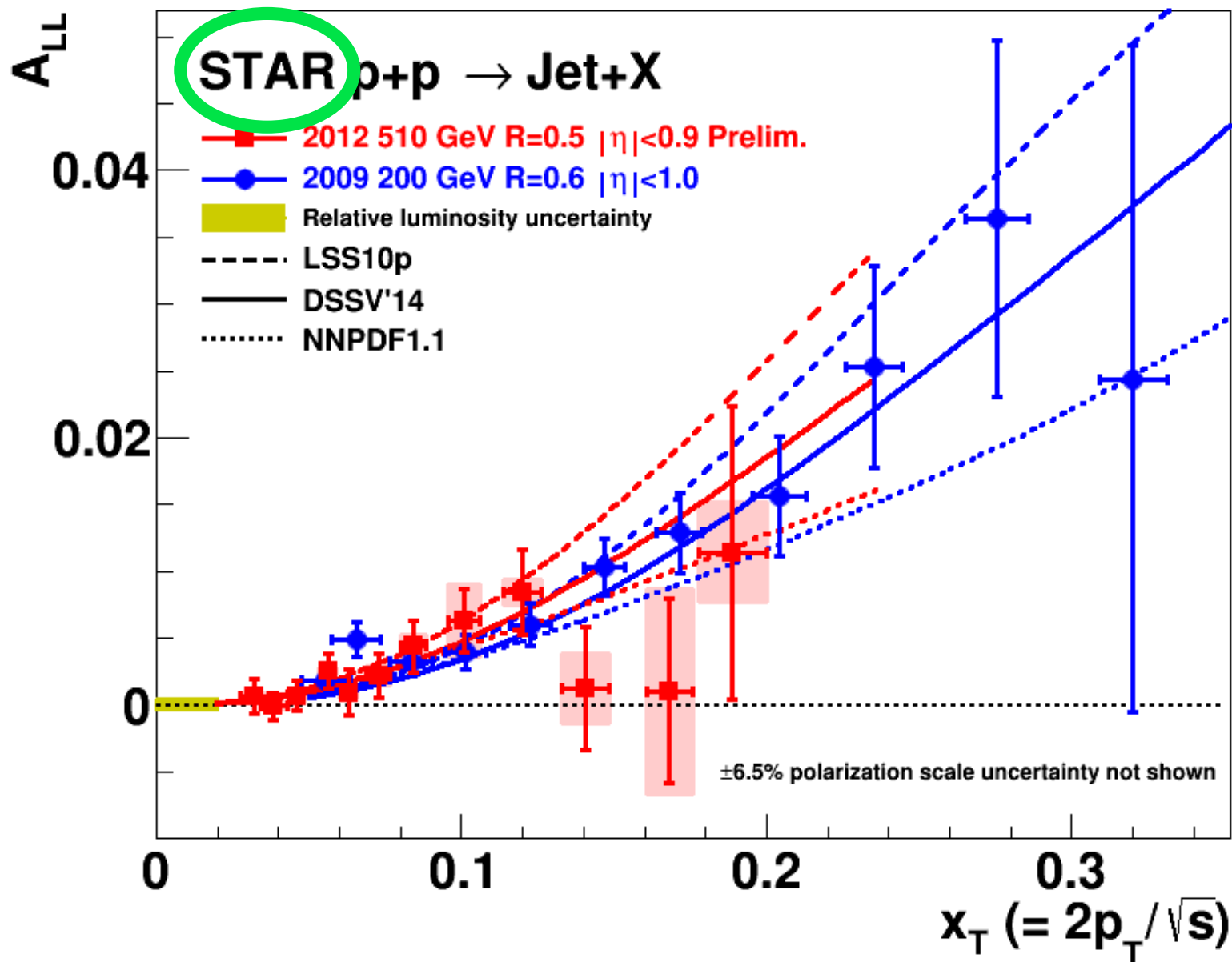
QCD factorization/calculation works at RHIC energies!

# RHIC Measurements on $\Delta G$



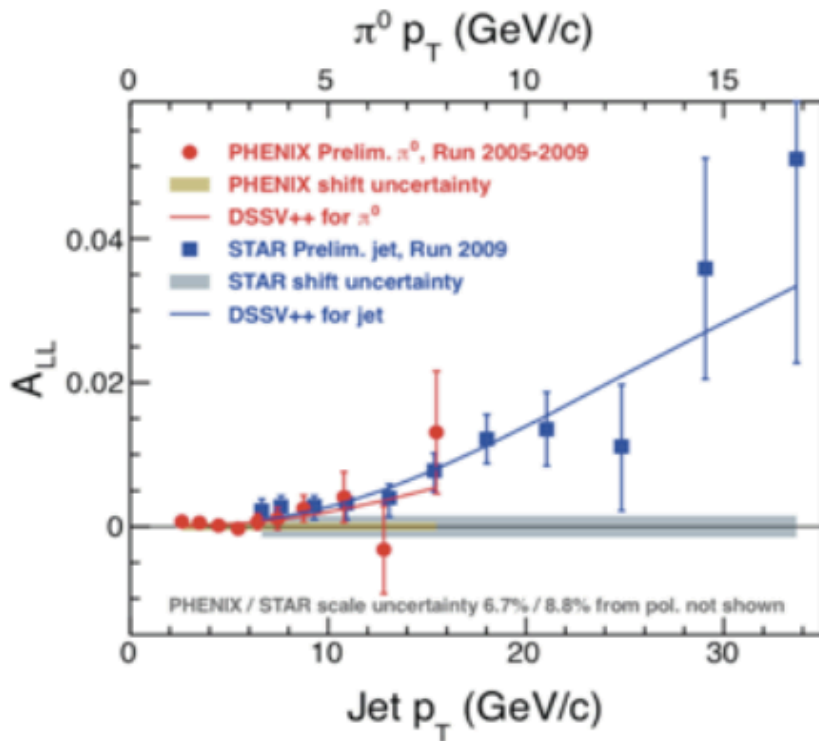


# RHIC Measurements on $\Delta G$



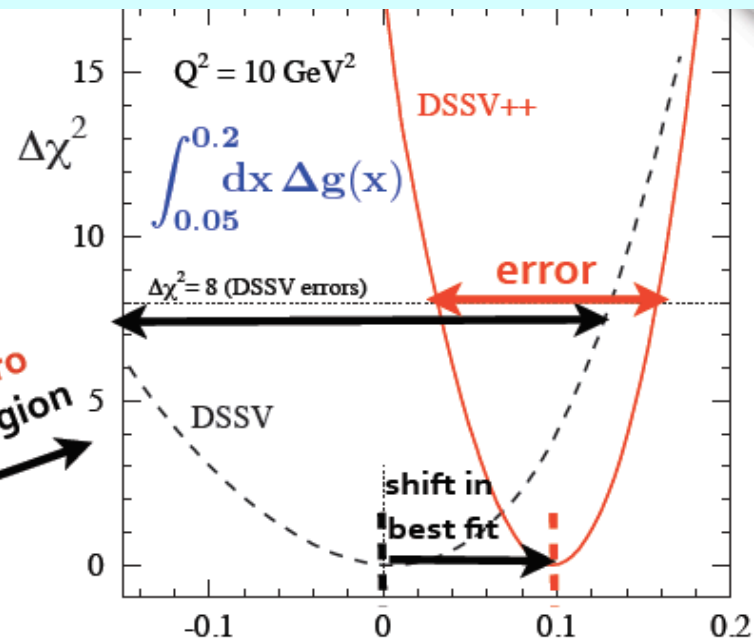
# Impact of RHIC measurements

new RHIC data included in **DSSV++**



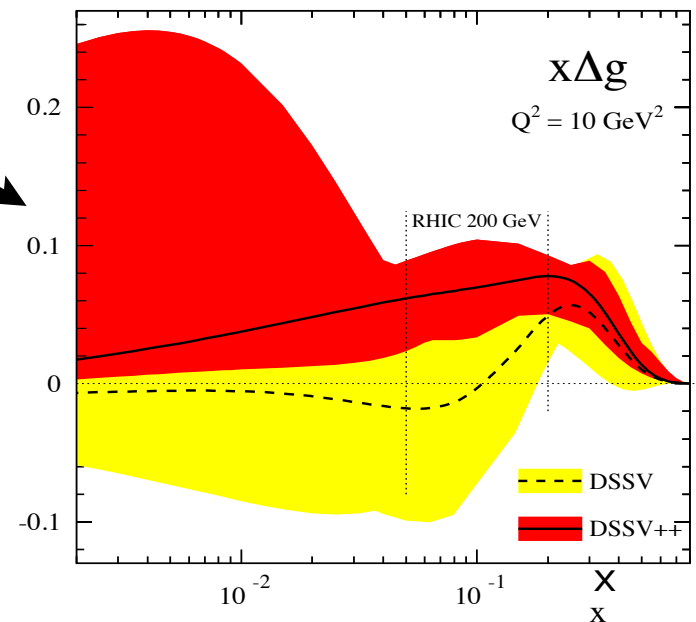
lead to **non-zero**  
 $\Delta g$  in RHIC x-region

**positive**  $\Delta g$   
in RHIC x-region



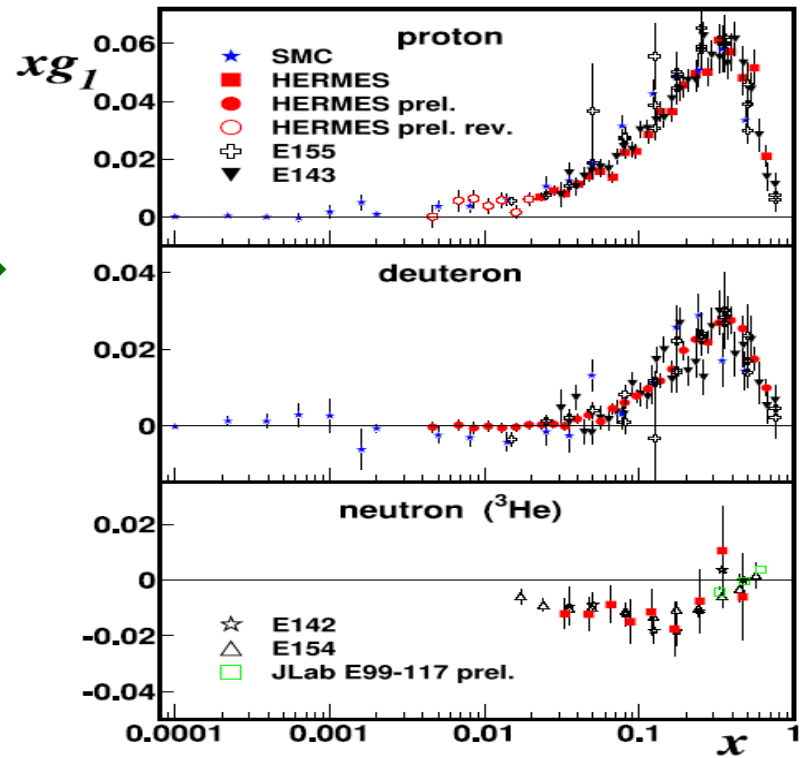
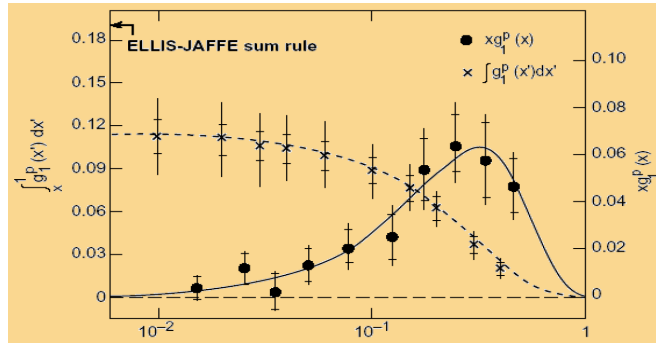
$$\int_{0.05}^{0.2} dx \Delta g(x, Q^2 = 10 \text{ GeV}^2) = 0.1^{+0.06}_{-0.07}$$

fully compatible with old DSSV error estimate



# Inclusive DIS data

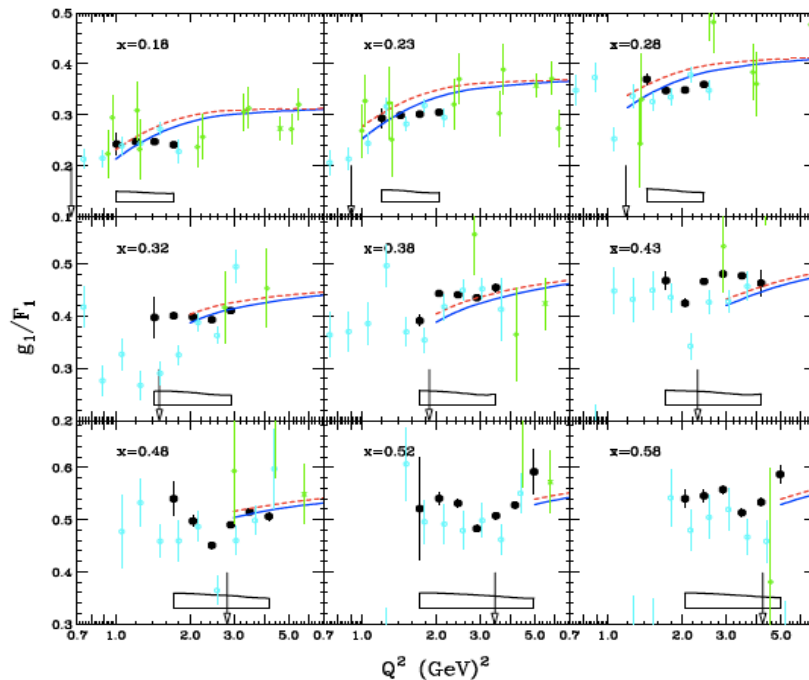
□ The “Plot” is greatly improved:



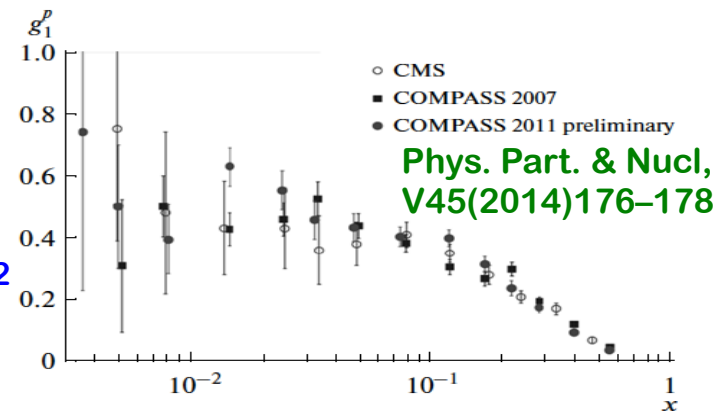
JLab/CLAS



arXiv:1404.6231

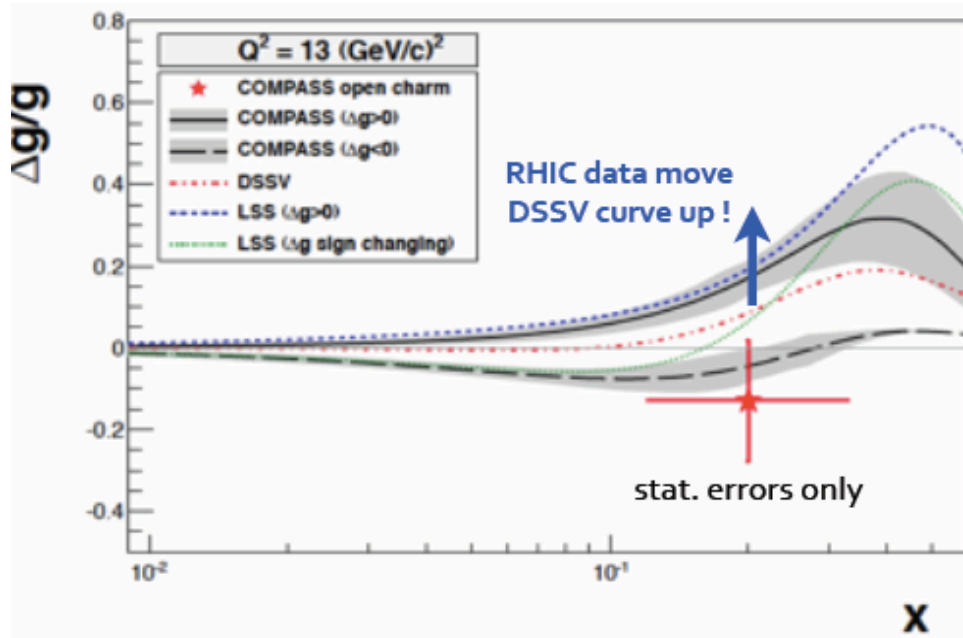
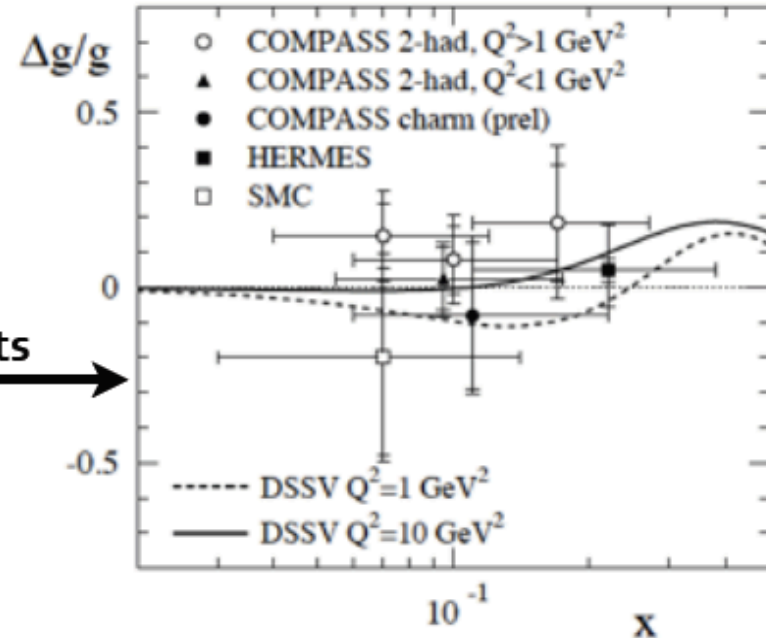
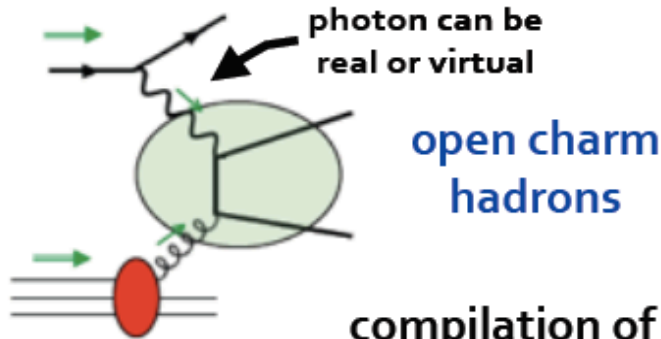


Lower  $Q^2$   
HT's



# Role of DIS measurements

idea: processes with (dominant) contributions from  $\gamma g$ -fusion



**new result**

**1211.6849**

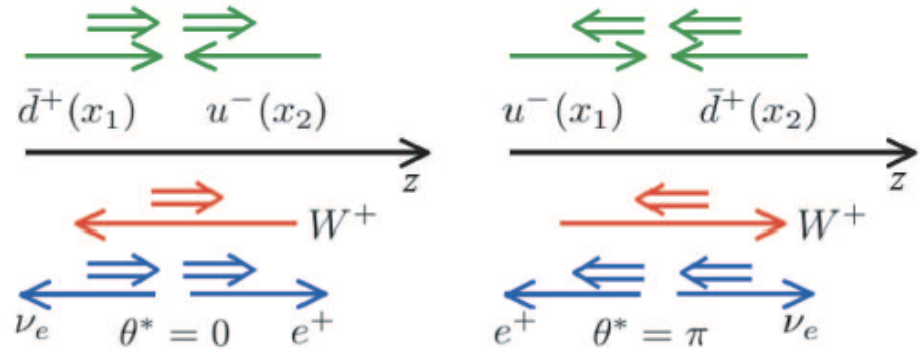
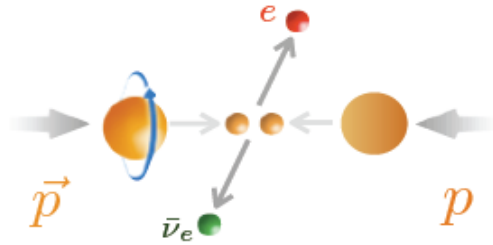
$$\left\langle \frac{\Delta g}{g} \right\rangle = -0.13 \pm 0.15 \pm 0.15$$

$$\langle x \rangle = 0.2 \quad \langle \mu^2 \rangle = 13 \text{ GeV}^2$$

from some "hybrid MC/NLO" extraction

# Determination of $\Delta q$ and $\Delta \bar{q}$

□ W's are left-handed:



□ Flavor separation:

Lowest order:

$$A_L^{W^+} = -\frac{\Delta u(x_1)\bar{d}(x_2) - \Delta\bar{d}(x_1)u(x_2)}{u(x_1)\bar{d}(x_2) + \bar{d}(x_1)u(x_2)}$$

$$x_1 = \frac{M_W}{\sqrt{s}} e^{y_W}, \quad x_2 = \frac{M_W}{\sqrt{s}} e^{-y_W}$$

Forward  $W^+$  (backward  $e^+$ ):

$$A_L^{W^+} \approx -\frac{\Delta u(x_1)}{u(x_1)} < 0$$

Backward  $W^+$  (forward  $e^+$ ):

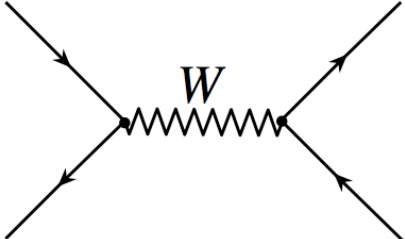
$$A_L^{W^+} \approx -\frac{\Delta\bar{d}(x_2)}{\bar{d}(x_2)} < 0$$

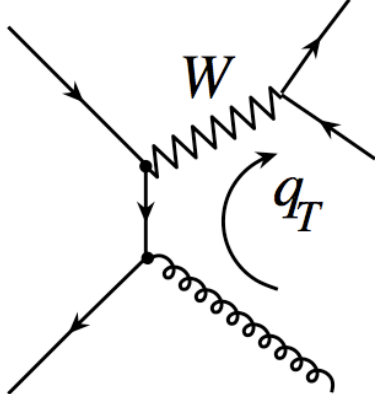
□ Complications:

High order, W's  $p_T$ -distribution at low  $p_T$

# High order effect

## □ Fixed order pQCD calculation:

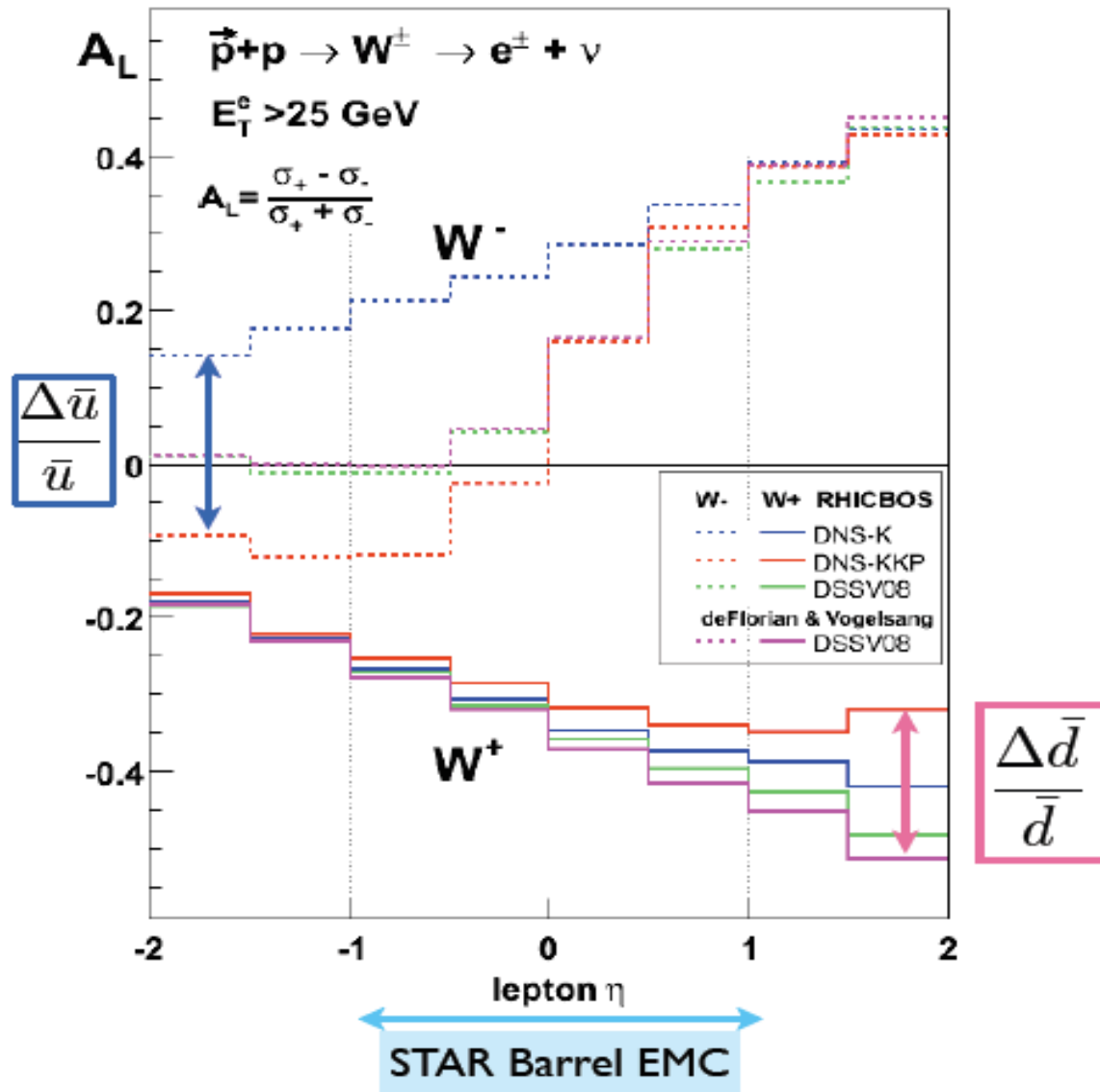
LO:   $\propto \delta^2(q_T)$

NLO:   $\propto \frac{1}{q_T^2} \Rightarrow \infty \text{ as } q_T^2 \rightarrow 0$

## □ All order resummation is needed at low $p_T$ :

CSS formalism – implemented in RHICBOS

# Predicted W asymmetry

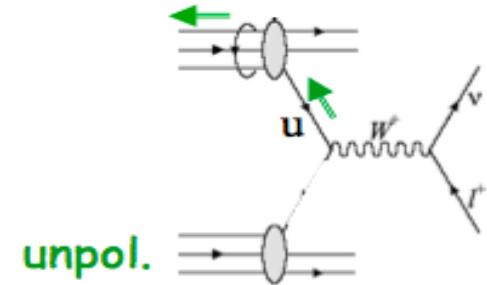


# Sea quark polarization – RHIC W program

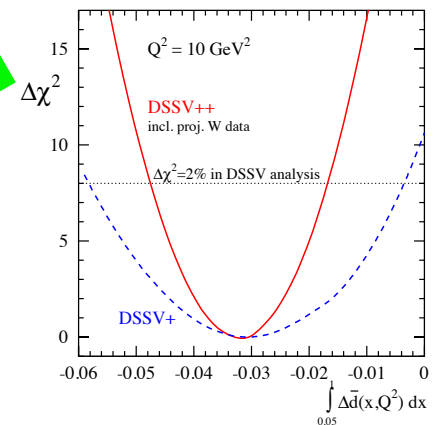
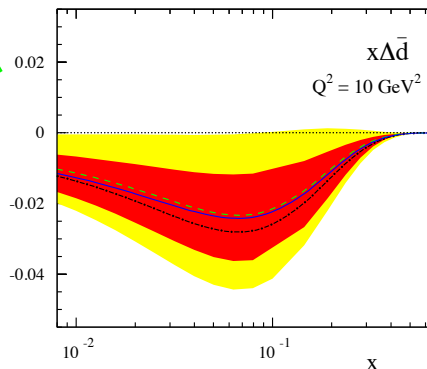
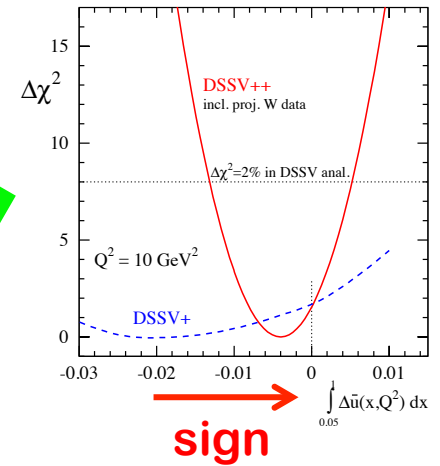
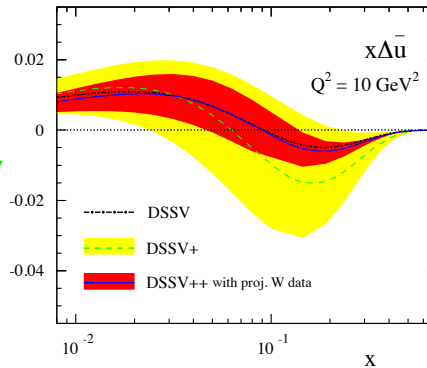
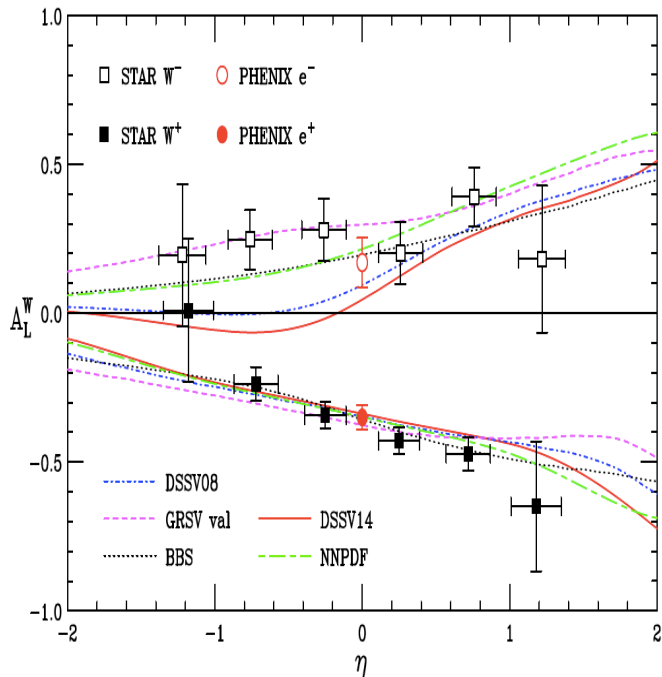
## □ Single longitudinal spin asymmetries:

$$A_L = \frac{[\sigma(+)-\sigma(-)]}{[\sigma(+)+\sigma(-)]} \quad \text{for } \sigma(s)$$

Parity violating weak interaction

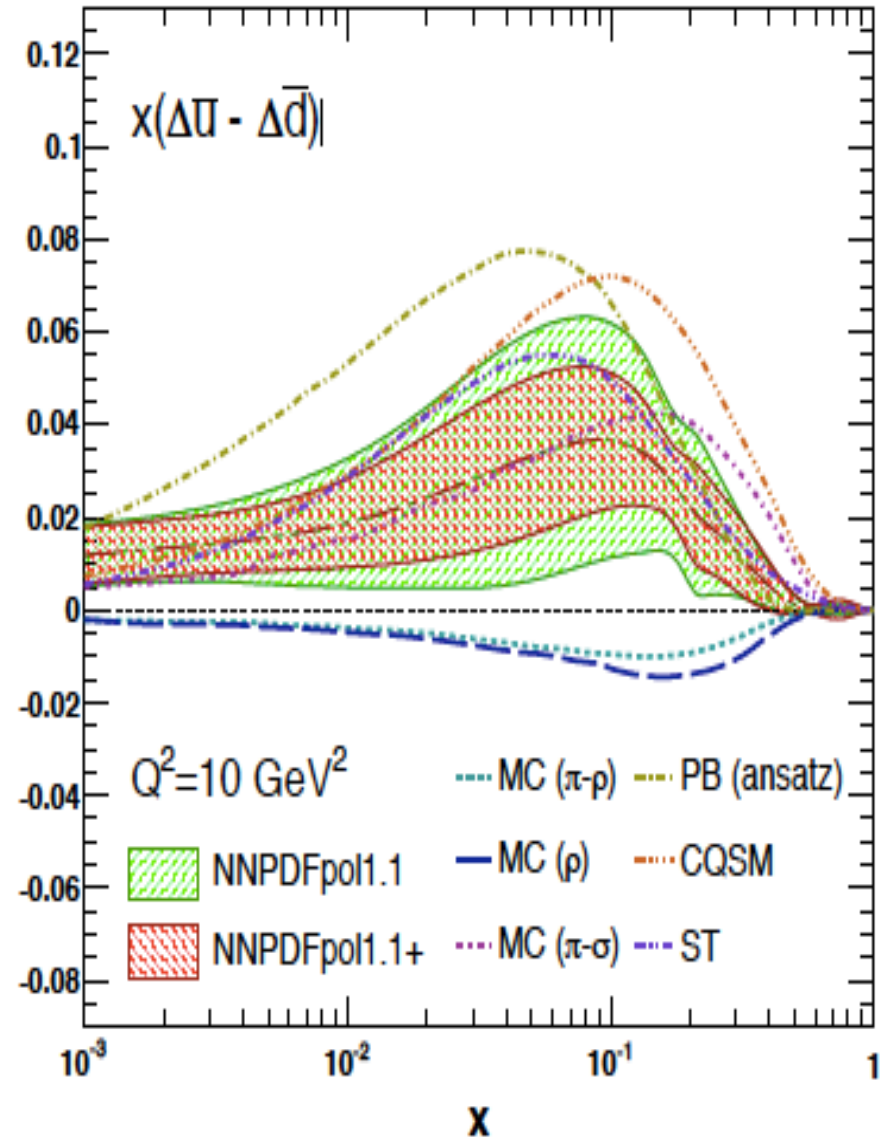
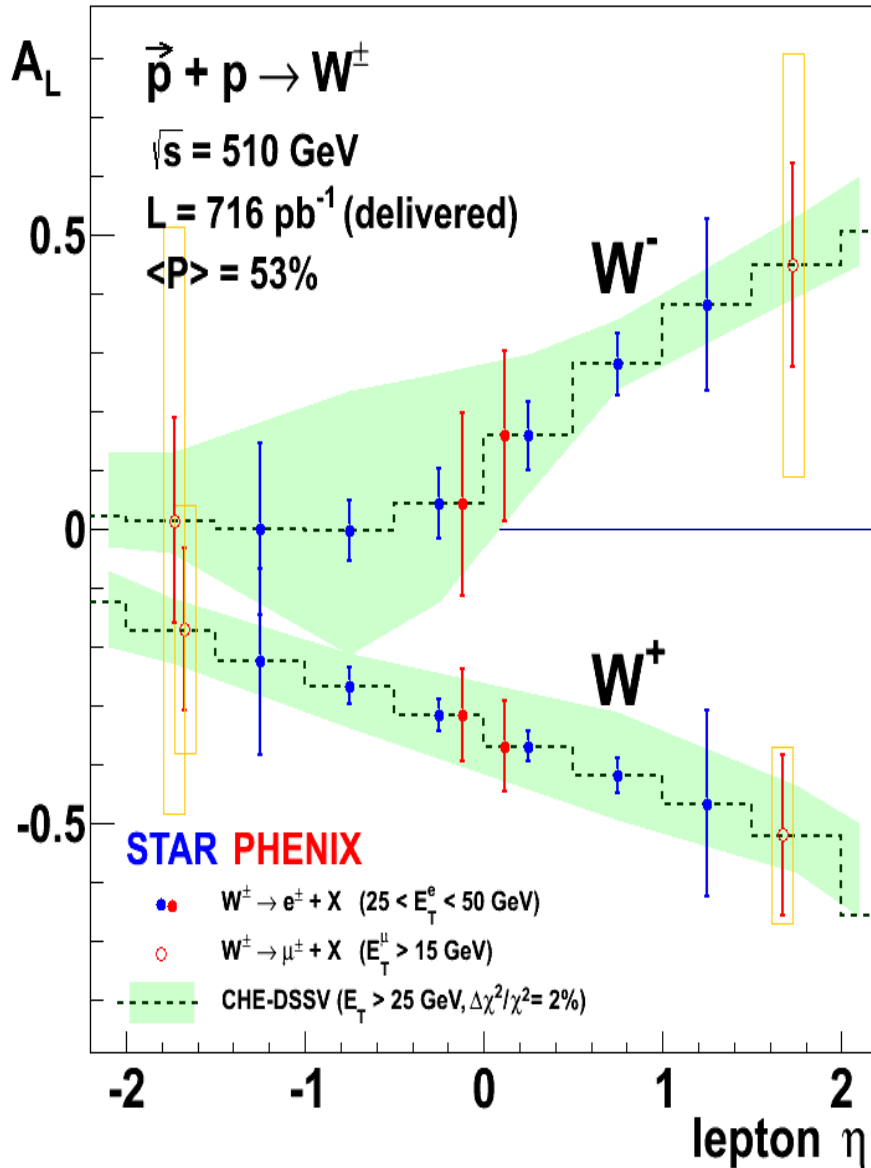


## □ From 2013 RHIC data:





# Projected future W asymmetries

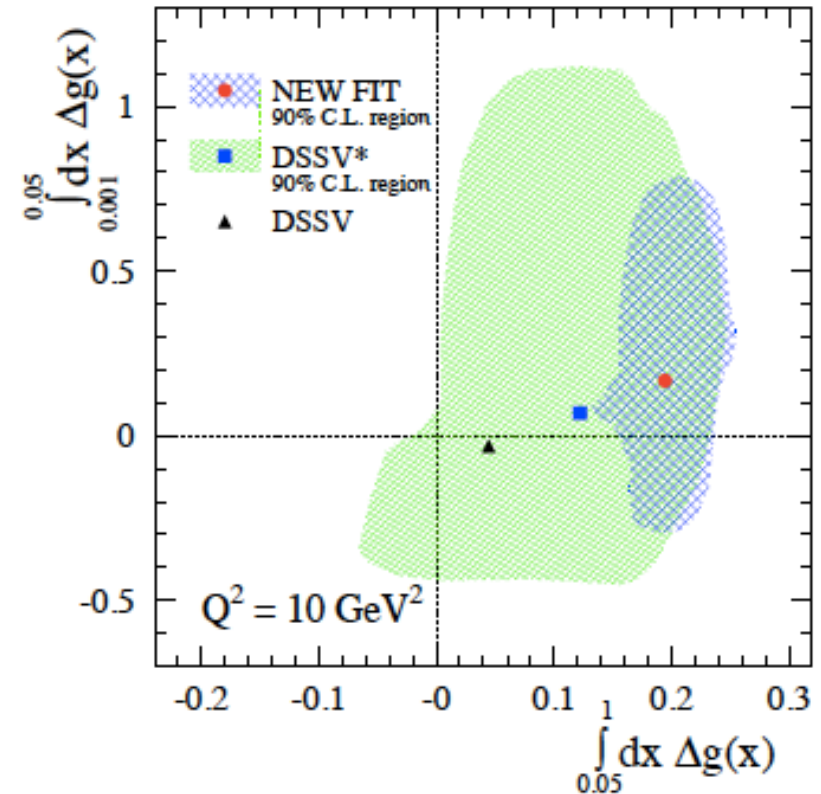
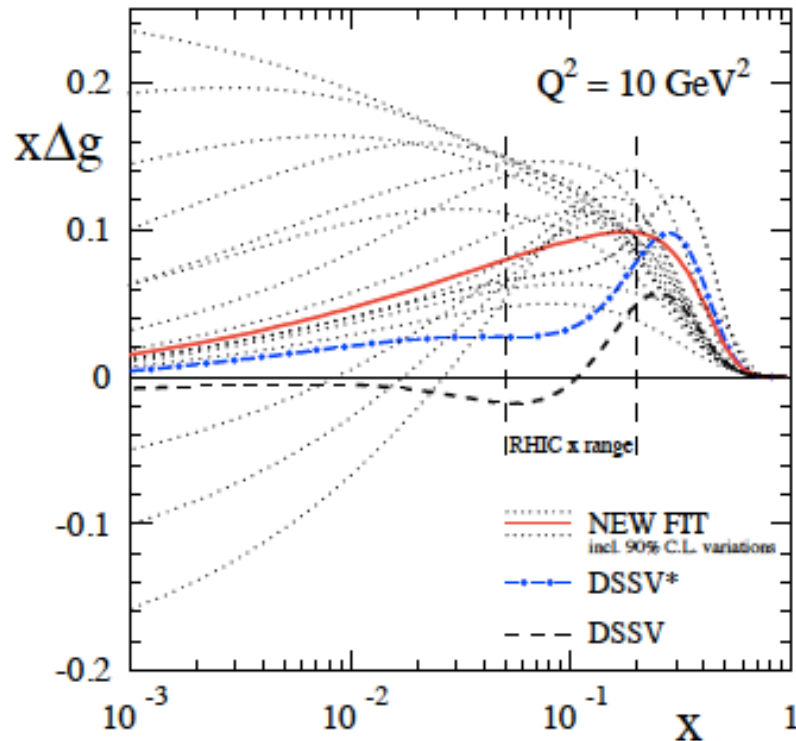


# Global QCD analysis of helicity PDFs

D. de Florian, R. Sassot, M. Stratmann, W. Vogelsang, PRL 113 (2014) 012001

results featured in Sci. Am., Phys. World, ...

## □ Impact on gluon helicity:



- ✧ Red line is the new fit
- ✧ Dotted lines = other fits with 90% C.L.

- ✧ 90% C.L. areas
- ✧ Leads  $\Delta G$  to a positive #

# Hadron structure at large $x$

□ Testing ground for hadron structure at  $x \rightarrow 1$ :

✧  $d/u \rightarrow 1/2$

SU(6) Spin-flavor symmetry

✧  $d/u \rightarrow 0$

Scalar diquark dominance

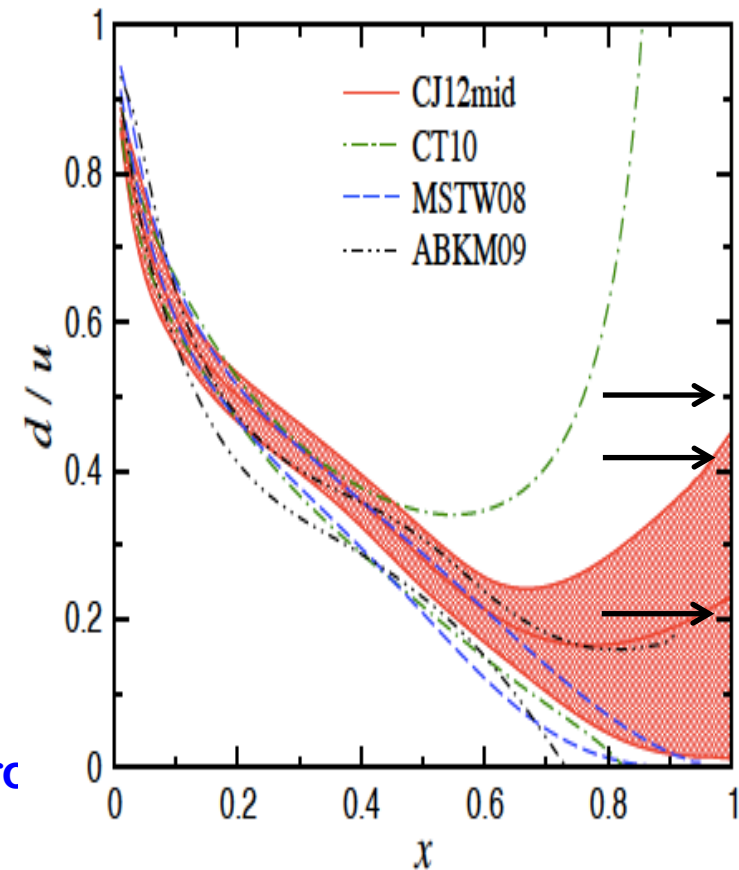
✧  $d/u \rightarrow 1/5$

pQCD power counting

✧  $d/u \rightarrow \frac{4\mu_n^2/\mu_p^2 - 1}{4 - \mu_n^2/\mu_p^2}$

Local quark-hadron duality

$\approx 0.42$



# Hadron structure at large $x$

## □ Testing ground for hadron structure at $x \rightarrow 1$ :

$$\diamond d/u \rightarrow 1/2$$

SU(6) Spin-flavor  
symmetry

$$\diamond \Delta u/u \rightarrow 2/3$$
$$\Delta d/d \rightarrow -1/3$$

$$\diamond d/u \rightarrow 0$$

Scalar diquark  
dominance

$$\diamond \Delta u/u \rightarrow 1$$
$$\Delta d/d \rightarrow -1/3$$

$$\diamond d/u \rightarrow 1/5$$

pQCD power  
counting

$$\diamond \Delta u/u \rightarrow 1$$
$$\Delta d/d \rightarrow 1$$

$$\diamond d/u \rightarrow \frac{4\mu_n^2/\mu_p^2 - 1}{4 - \mu_n^2/\mu_p^2}$$

Local quark-hadron  
duality

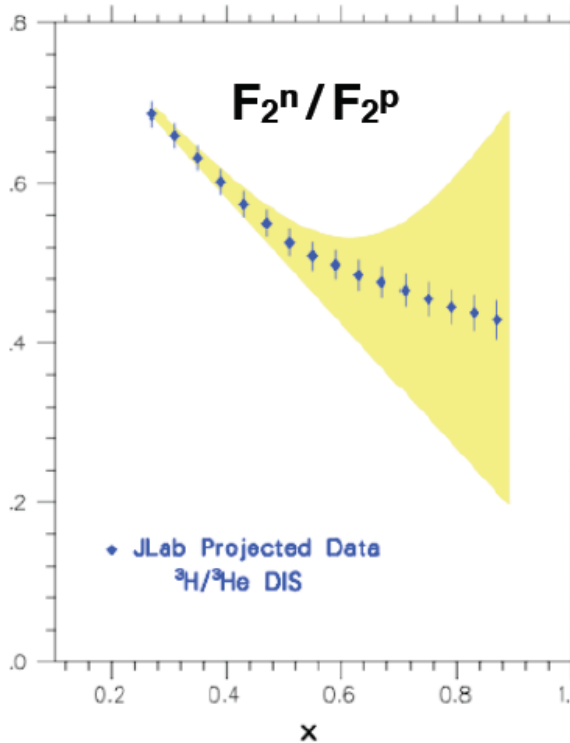
$$\diamond \Delta u/u \rightarrow 1$$
$$\Delta d/d \rightarrow 1$$

$$\approx 0.42$$

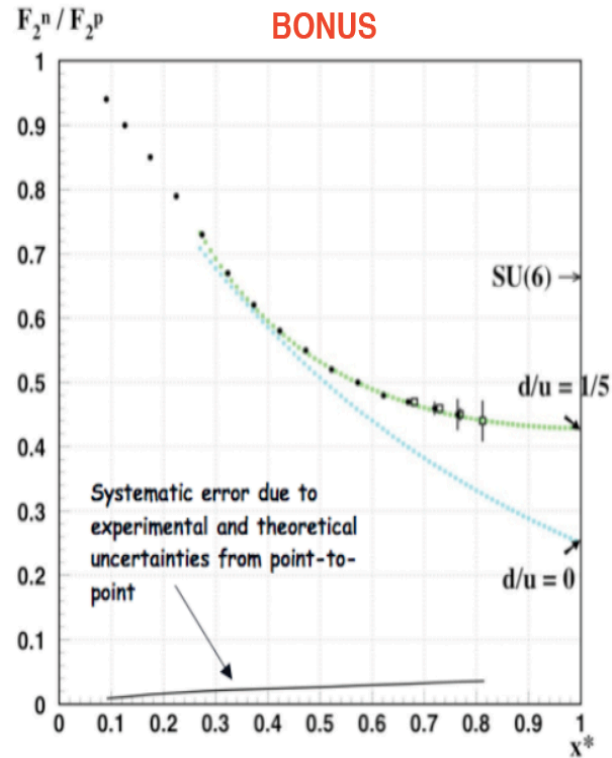
# Future large-x experiments – JLab12

## □ NSAC milestone HP14 (2018):

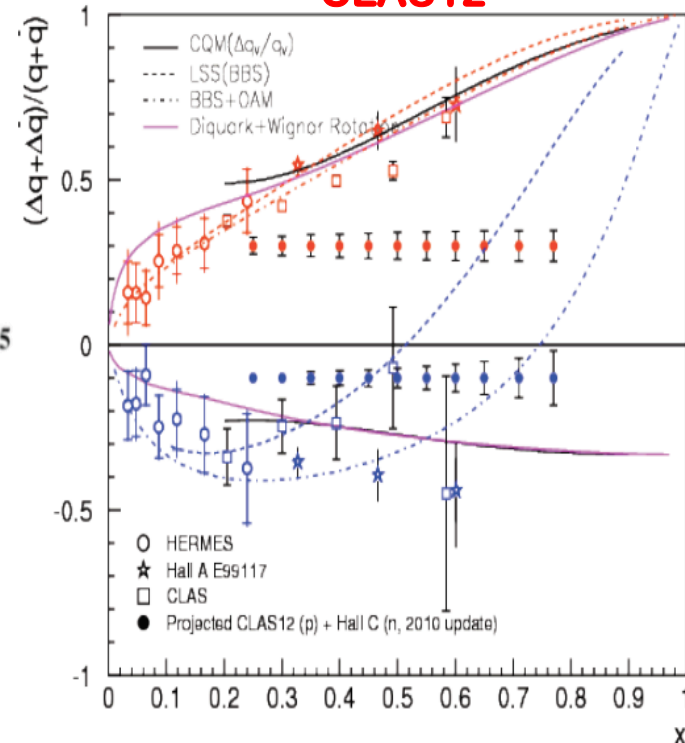
### MARATHON



### BONUS



### CLAS12



## Plus many more JLab experiments:

E12-06-110 (Hall C on  ${}^3\text{He}$ ), E12-06-122 (Hall A on  ${}^3\text{He}$ ),

E12-06-109 (CLAS on  $\text{NH}_3$ ,  $\text{ND}_3$ ), ...

and Fermilab E906, ...

# Future improvement to $\Delta G$

□ NNLO?      Probably not yet

□ Key: Extrapolation to low  $x$  and high  $x$

✧ Large  $x$ : total contribution might be small  
due to the steep falling phase space

✧ Small  $x$ : larger phase space for shower and smaller  $Q$   
for a fixed collision energy       $\Rightarrow$  Large  $\langle k_T^2 \rangle$ ,  $\ln(s/Q^2) \sim \ln(1/x)$

□ Collinear factorization does not work when  $Q \sim Q_s(x) \sim \langle k_T \rangle$

$$G(x) = G^+(x) + G^-(x) \propto \frac{1}{x^{1+\alpha}} \quad \text{at small } x$$

$$\Delta G(x) = G^+(x) - G^-(x) \quad \text{Could be proportional to } \frac{1}{x^\alpha}$$

Not positive definite!

□ Current understanding of  $\Delta G$  :

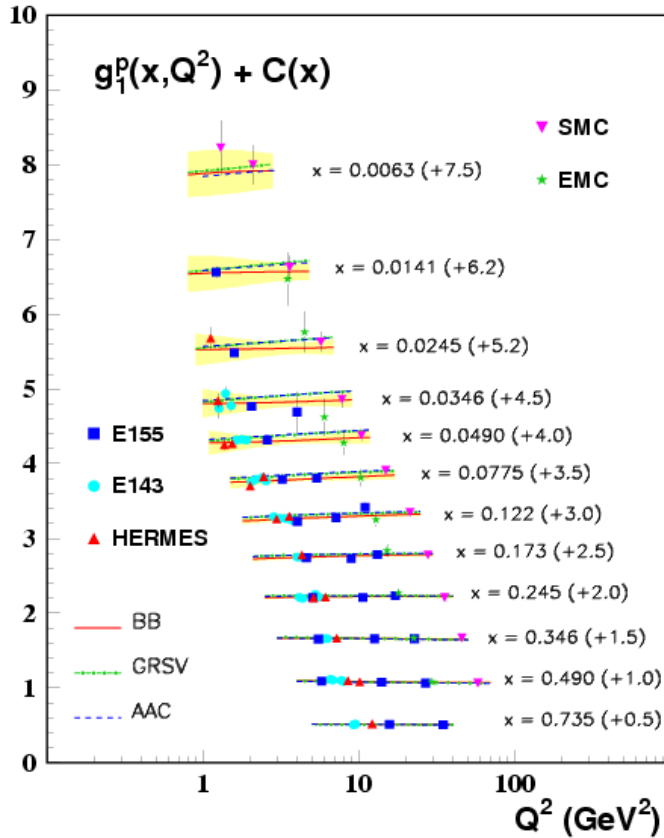
$\Delta G \sim 2$  is unlikely, but,  $\Delta G \sim 1/4$  or  $1/2$  ( $1/4$ ) is still possible

It is the  $G(x)$ , not  $\int dx G(x)$ , that is more sensitive to QCD dynamics!

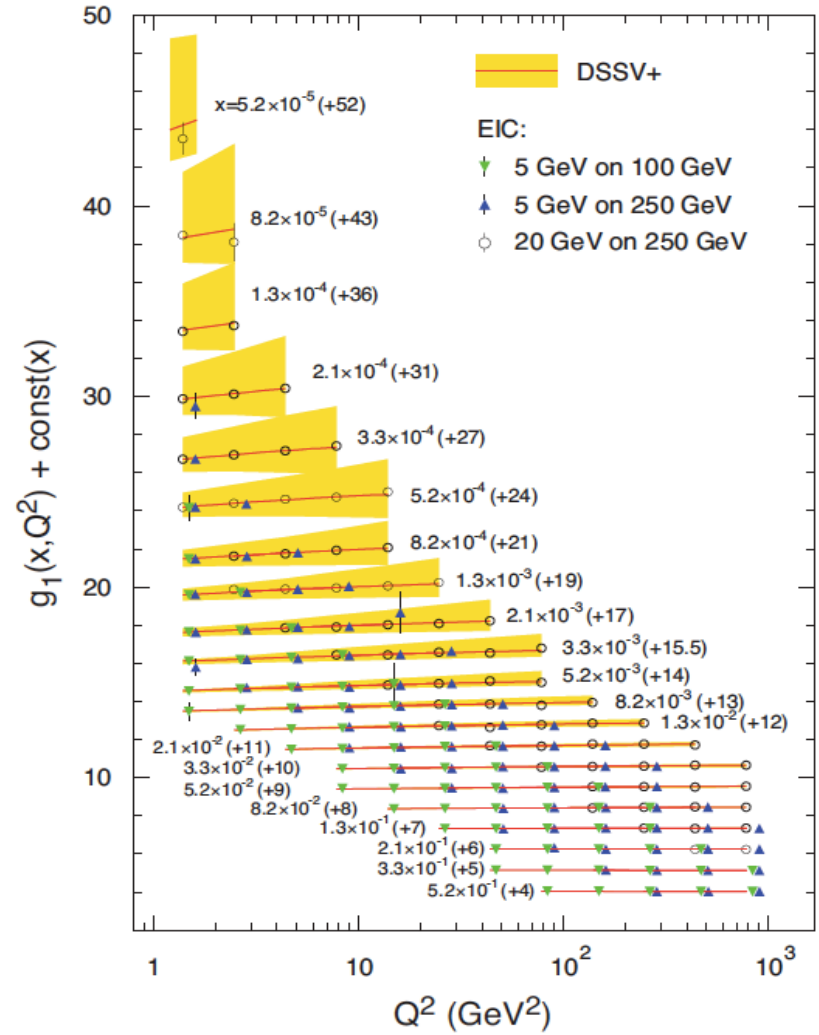
*Future EIC –  $Q^2$  evolution*

# The Future: Challenges & opportunities

## □ The power & precision of EIC:



at EIC



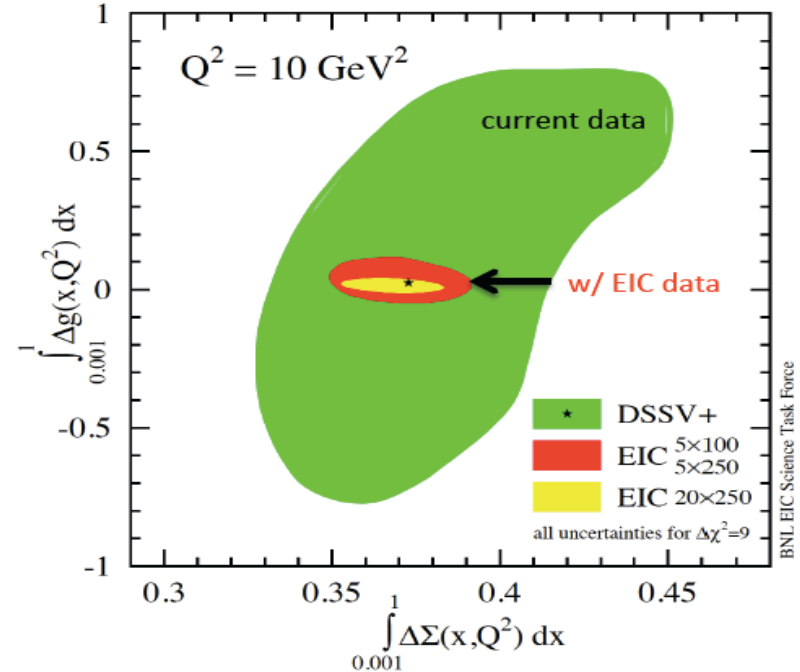
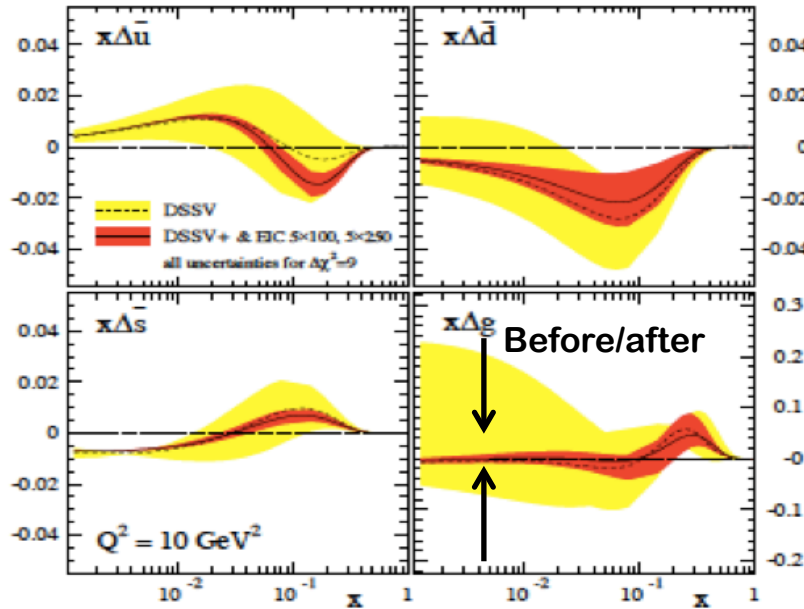
## □ Reach out the glue:

$$\frac{dg_1(x, Q^2)}{d \ln Q^2} = \frac{\alpha_s}{2\pi} P_{qg} \otimes \Delta g(x, Q^2) + \dots$$

# The Future: Challenges & opportunities

## One-year of running at EIC:

Wider  $Q^2$  and  $x$  range including low  $x$  at EIC!



No other machine in the world can achieve this!

## Ultimate solution to the proton spin puzzle:

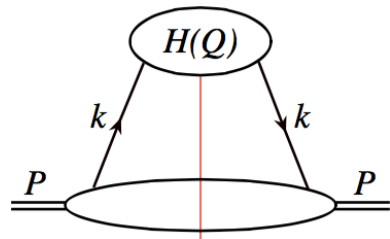
- ✧ Precision measurement of  $\Delta g(x)$  – extend to smaller  $x$  regime
- ✧ Orbital angular momentum contribution – measurement of GPDs!



# Recall: the other leading power distribution

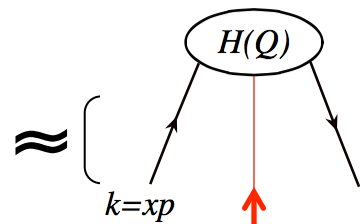
## Collinear approximation:

– quark:



Spin:  $I, \gamma_5, \gamma^\mu, \gamma^\mu \gamma_5, \sigma^{\mu\nu} (i\gamma_5)$

$S, P, V, A, T$



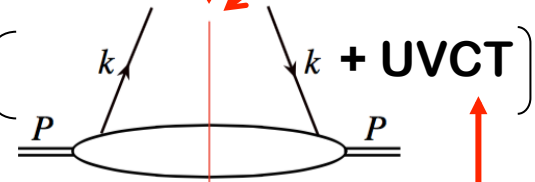
$+ O\left(\frac{k_T^2}{Q^2}\right)$

$\int \frac{dx}{x}$

$S, P, V, A, T$

$I, \gamma_5, \gamma_\mu, \gamma_5 \gamma_\mu, \sigma_{\mu\nu} (i\gamma_5)$

$\delta\left(x - \frac{k \cdot n}{P \cdot n}\right) \frac{d^4 k}{(2\pi)^4}$



Scheme dependence

## Leading power hard parts in $p$ :

$$\frac{1}{2} \gamma \cdot p (V), \quad \frac{1}{2} \gamma_5 \gamma \cdot p (A), \quad \frac{1}{2} \gamma \cdot p \gamma_\perp^\alpha \gamma_5 (T) \longleftrightarrow \text{4 – spin states of the “quark-pair”}$$

Non-flip, longitudinally flip, transversely flip

## Leading power distributions:

$$\frac{\gamma \cdot n}{2p \cdot n} (V), \quad \frac{\gamma_5 \gamma \cdot n}{2p \cdot n} (A), \quad \frac{\gamma \cdot n \gamma_\perp^\alpha \gamma_5}{2p \cdot n} (T) \longleftrightarrow q(x, Q), \quad \Delta q(x, Q), \quad h_1(x, Q)$$

Unpolarized PDF, Helicity/Polarized PDF, Transversity distribution

# Transversity Distributions

## □ Transversity:

Jaffe and Ji, 1991

$$h_1(x) = \frac{1}{\sqrt{2p^+}} \int \frac{d\lambda}{2\pi} e^{i\lambda x} \langle PS_{\perp} | \psi_{+}^{\dagger}(0) \gamma_{\perp} \gamma_5 \psi_{+}(\lambda n) | PS_{\perp} \rangle + \text{UVCT}$$

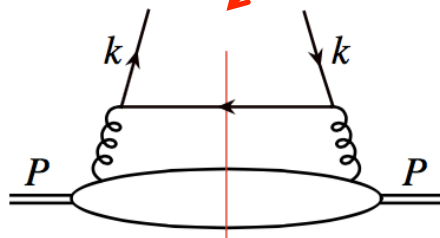
with  $\psi_{\pm} = P_{\pm} \psi$  and  $P_{\pm} = \frac{1}{2} \gamma^{\mp} \gamma^{\pm}$

## □ Unique for the quarks:

No mixing with gluons!

$$\gamma \cdot n \gamma_{\perp} \gamma_5$$

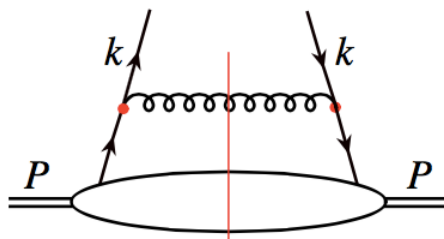
Even # of  $\gamma$ 's



= 0

No mixing with PDFs,  
helicity distributions

## □ Perturbatively UV and CO divergent:



+ wave function renormalization

$$\Delta_T P_{qq}^{(0)}(x) = C_F \left[ \frac{2x}{(1-x)_+} + \frac{3}{2} \delta(1-x) \right]$$

→ “DGLAP” evolution kernels

NLO - Vogelsang, 1998

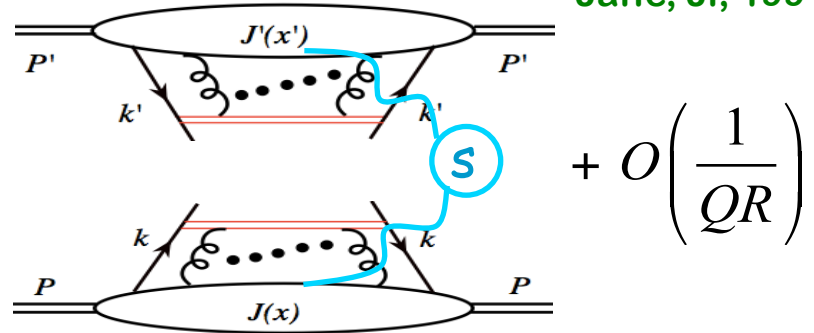
# Connection to physical observables

□ Need two-chiral odd distributions – two hadrons:

– Drell-Yan:

$$\sigma_{\text{tot}}^{\text{DY}} \sim \text{[Diagram: Drell-Yan annihilation]} \otimes \text{[Diagram: Parton distribution]} \otimes \text{[Diagram: Parton distribution]}$$

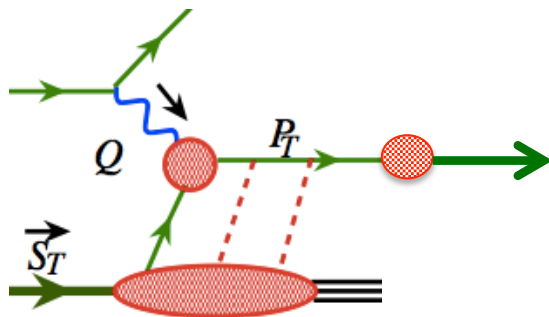
$$\sim h_1(x) \otimes h_1(x')$$



Soper, Ralston, 1978  
Jaffe, Ji, 1991, 1992

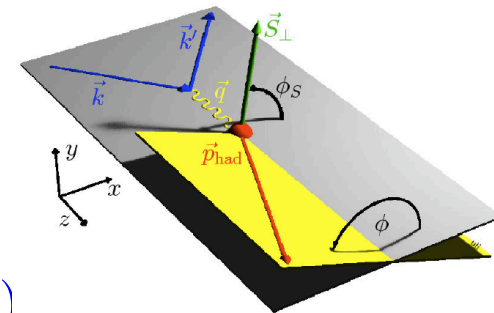
**Predictive power: Universal Transversity**

– SIDIS:



$$\sim h_1(x) \otimes D_{\text{Collins}}(z)$$

$$\sim A_T^{\sin(\phi + \phi_s)}$$



□ Caution:

Transversity extracted depends on the “scheme” or UVCT

Cross section is always positive!

Like PDFs (helicity distributions), transversity does not have to be positive

# Soffer's inequality

## □ Relation between quark distributions:

$$h_1(x) \leq \frac{1}{2} [q(x) + \Delta q(x)] = q^+(x)$$

Derived by using the positivity constraint of  
quark + nucleon  $\rightarrow$  quark + nucleon  
forward scattering helicity amplitudes

## Cautions:

- ✧ Quark field of the Transversity distribution is NOT on-shell
- ✧ Quark + nucleon  $\rightarrow$  quark + nucleon  
forward scattering amplitude is perturbatively divergent

## □ Testing vs using as a constraint:

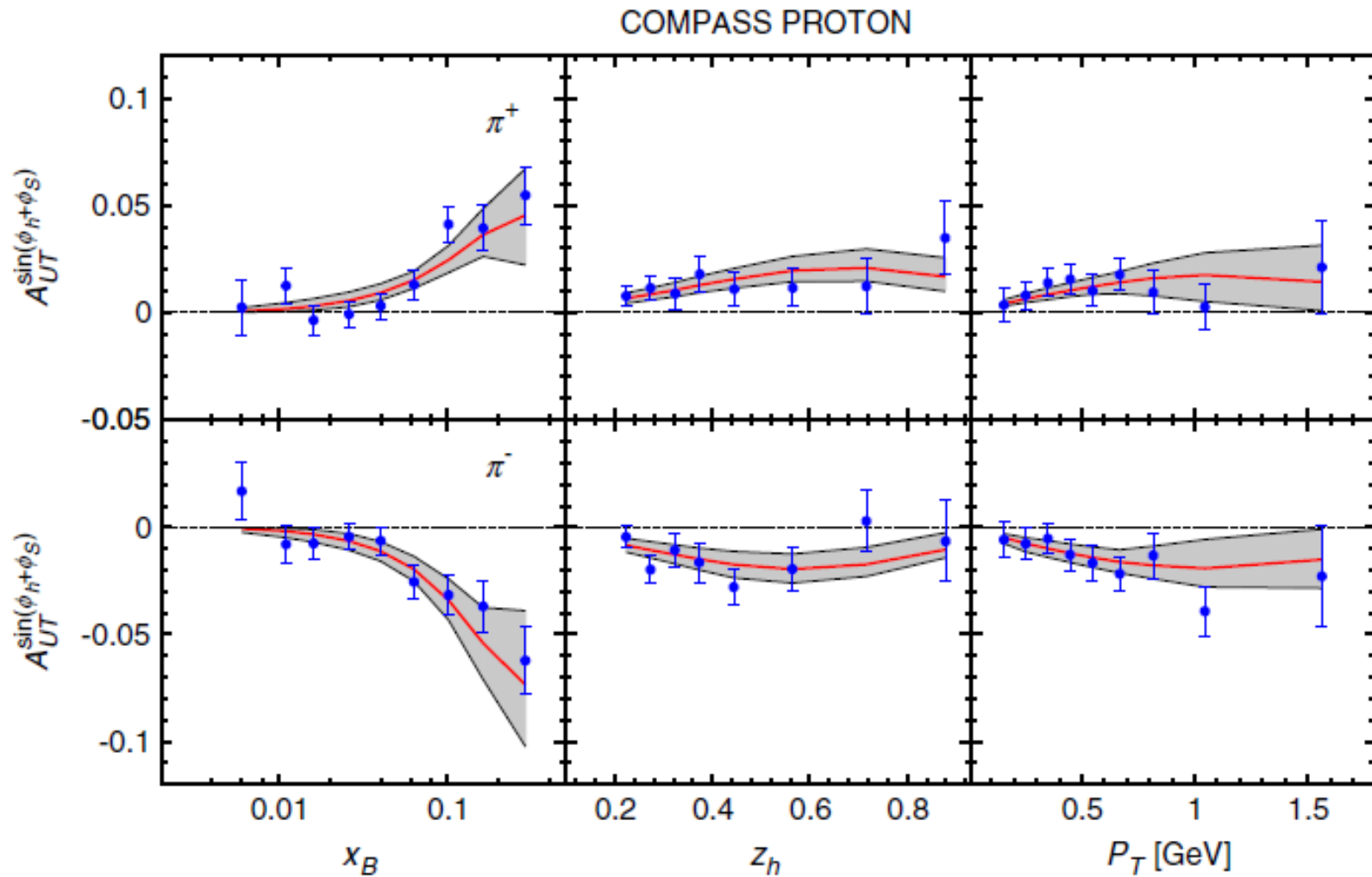
It is important to test this inequality, rather than using it  
as a constraint for fitting the transversity

Perturbatively calculated evolution kernels seem to be consistent  
with the inequality – the scale dependence

# Extraction of Transversity

□ SIDIS – mixed with Collins function:

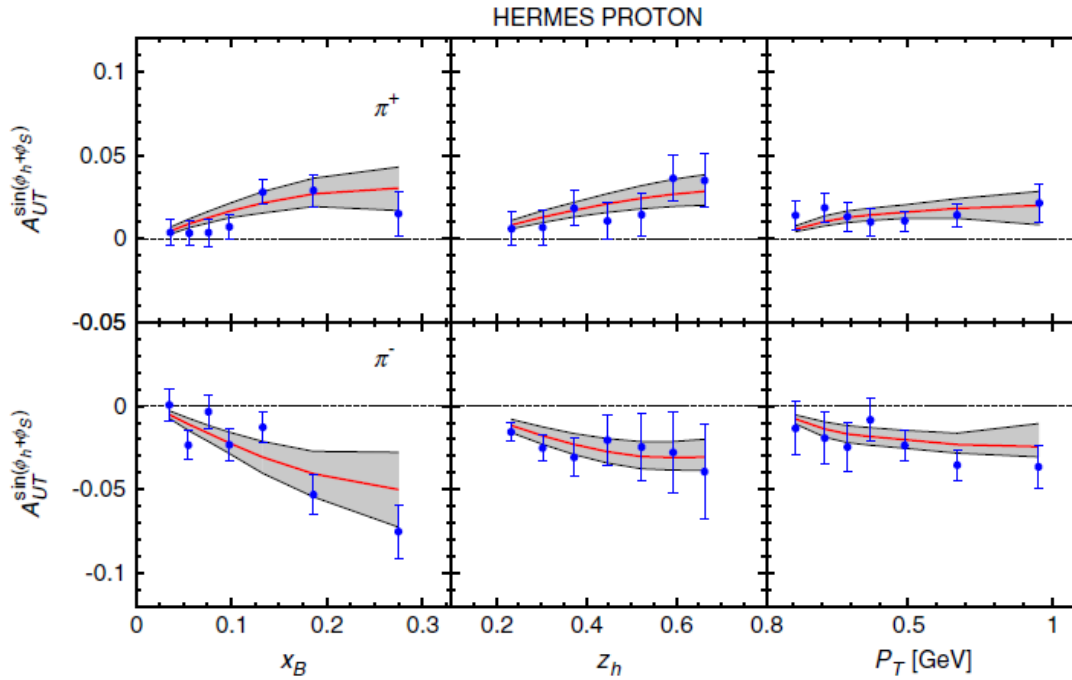
Anselmino et al.,  
PRD 87, 094019 (2013)



# Extraction of Transversity

□ SIDIS – mixed with Collins function:

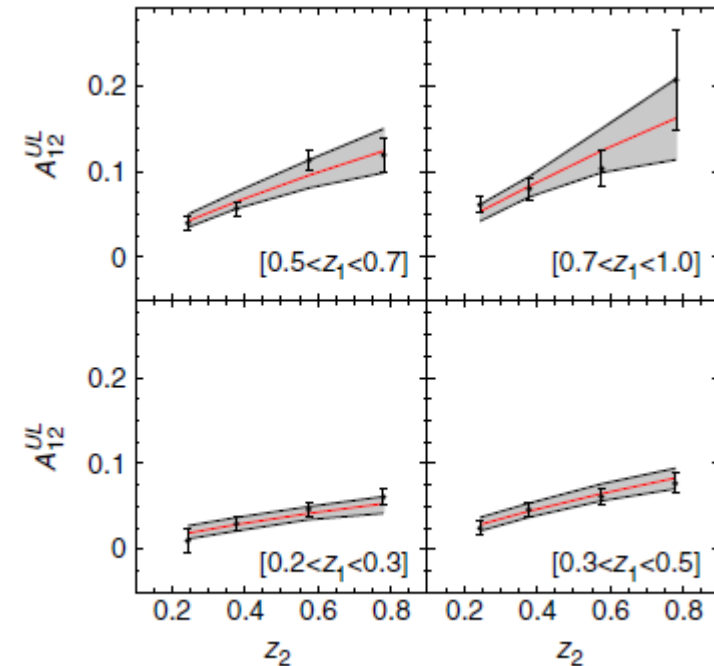
Anselmino et al.,  
PRD 87, 094019 (2013)



← HERMES (eP)

□ e+e- – Collins functions:

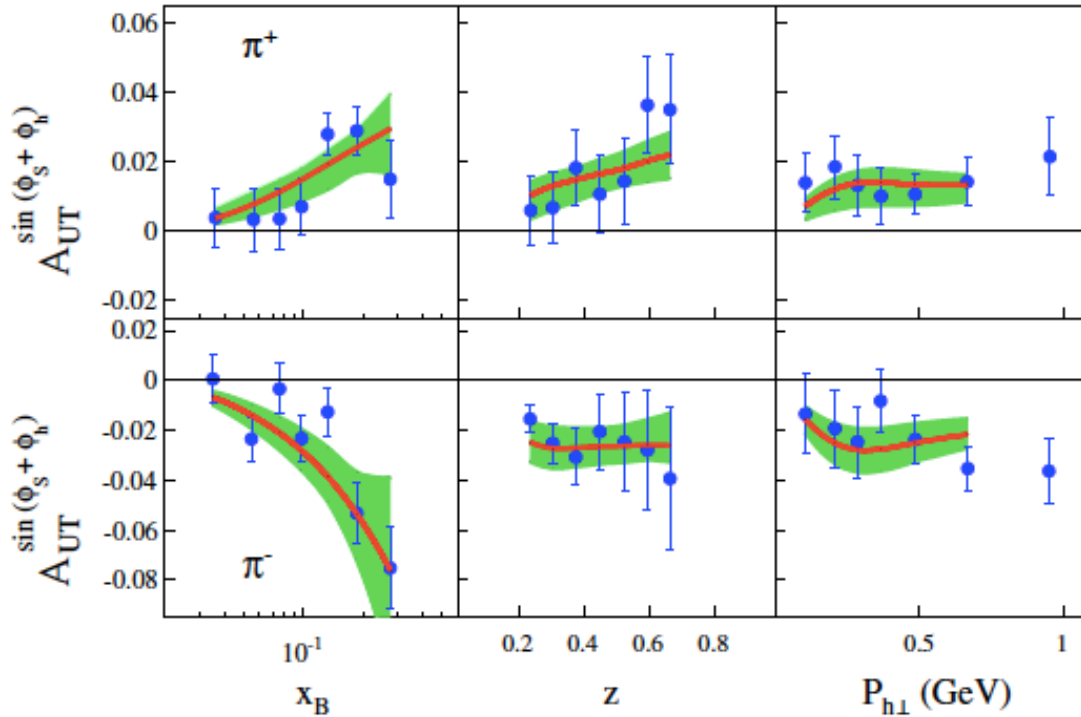
Belle (e+e-) →



# Extraction of Transversity

Kang et al, PRD, 2016

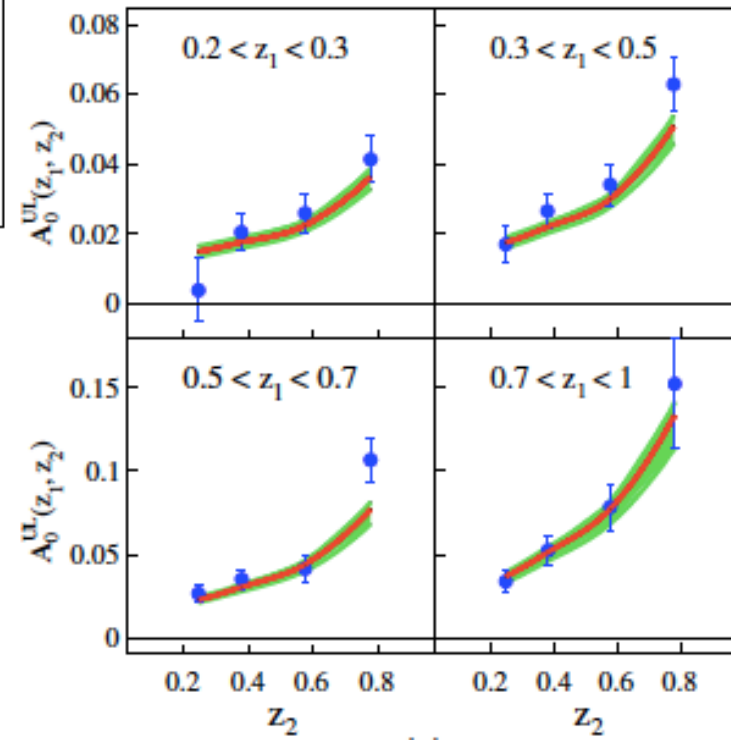
□ SIDIS – mixed with Collins function:



← HERMES (eP)

□ e+e- – Collins functions:

Belle (e+e-) →

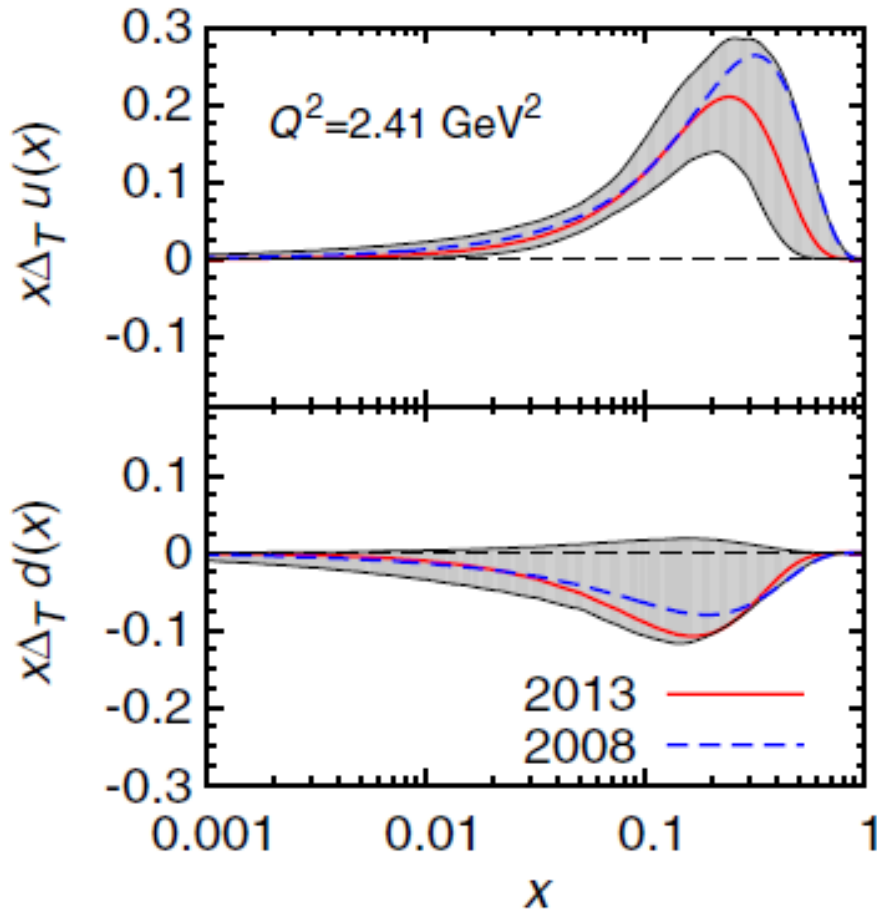


# Extraction of Transversity

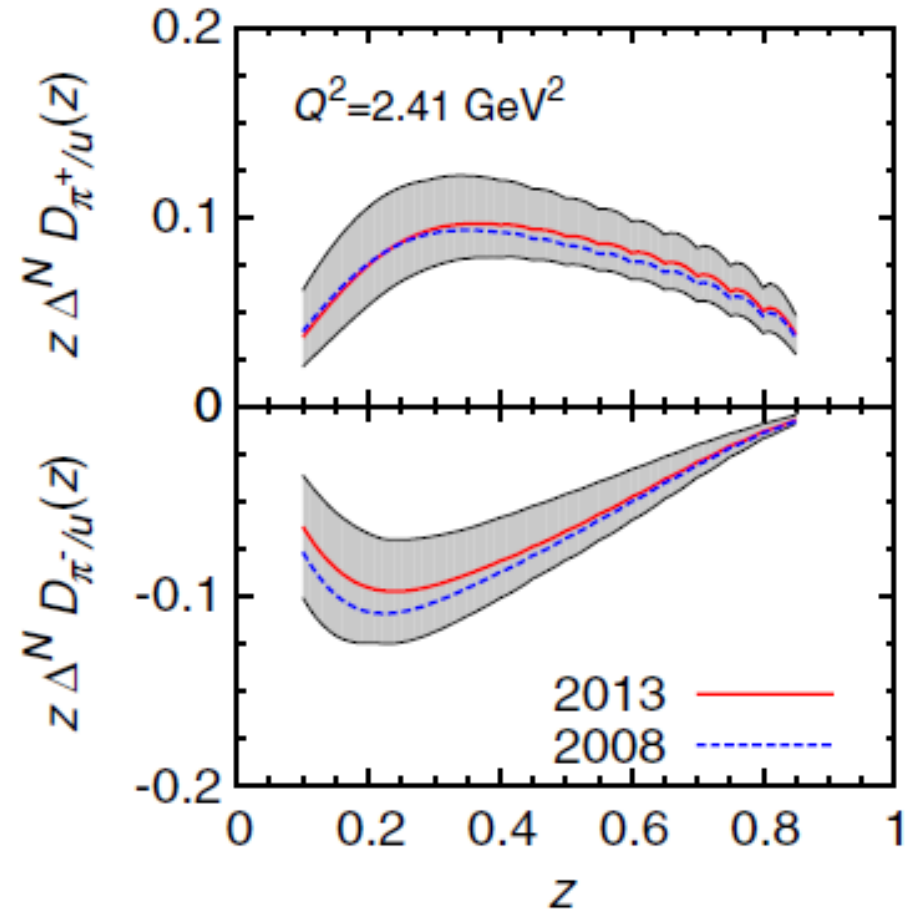
Anselmino et al.,  
PRD 87, 094019 (2013)

## □ Transversity and Collins function:

### Transversity



### Collins function





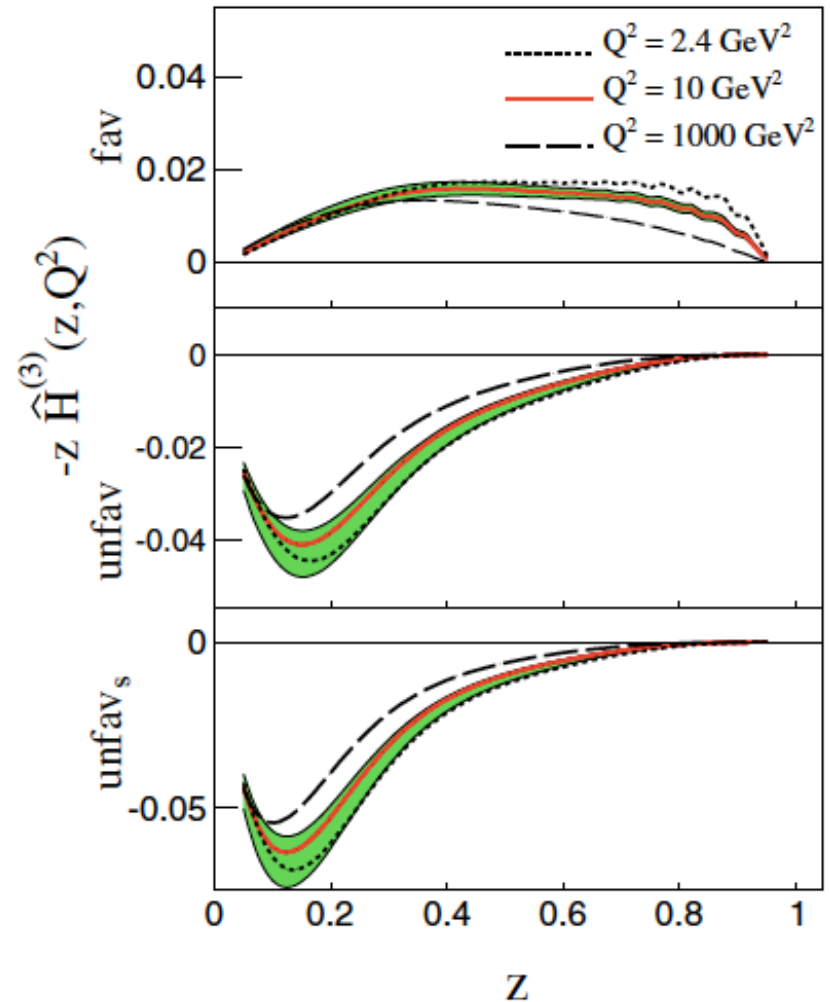
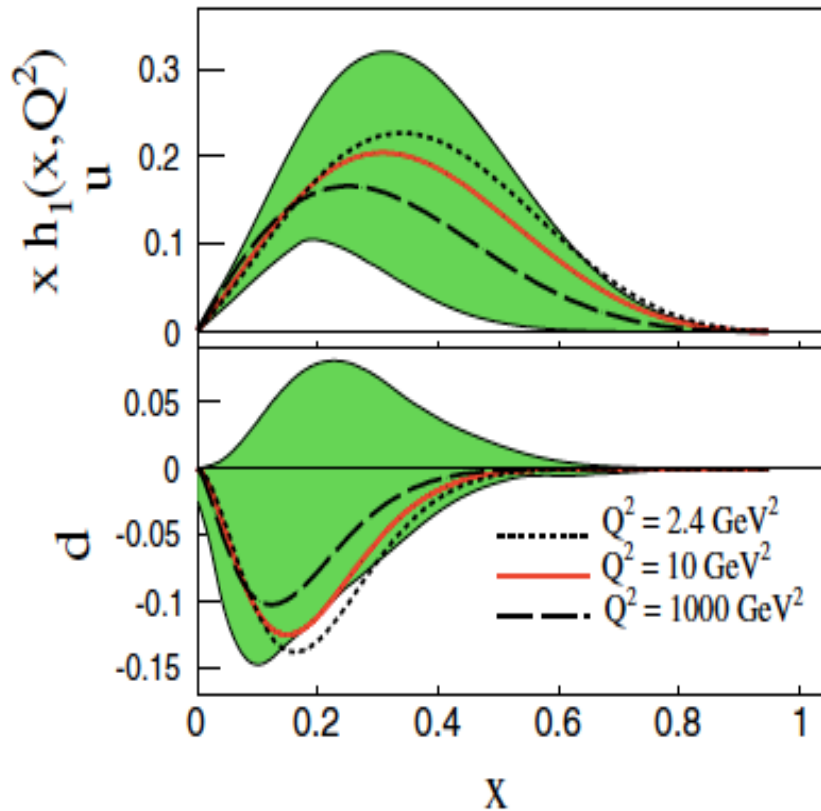
# Extraction of Transversity

Kang et al, PRD, 2016

□ Transversity and Collins function:

Collins function

Transversity

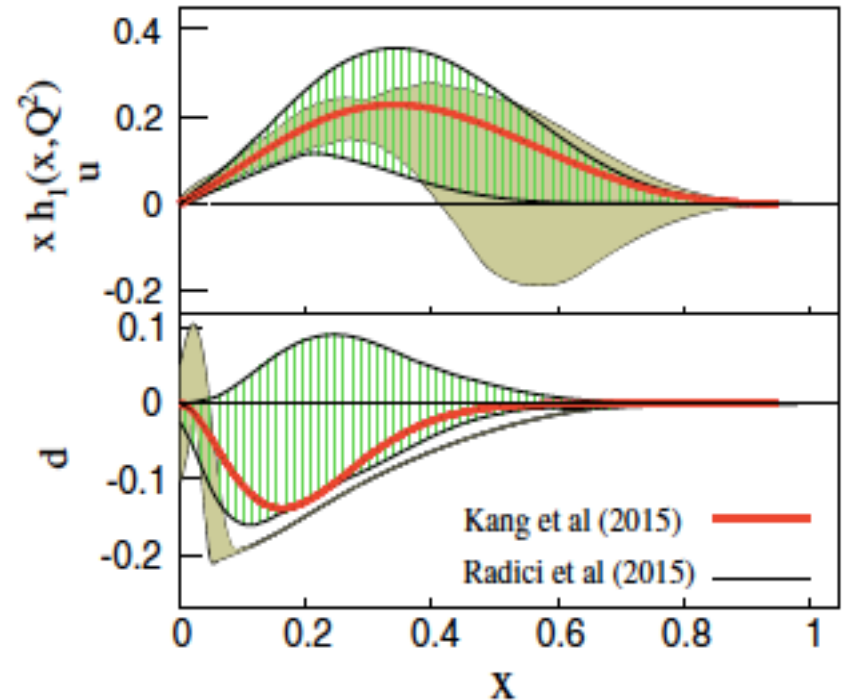
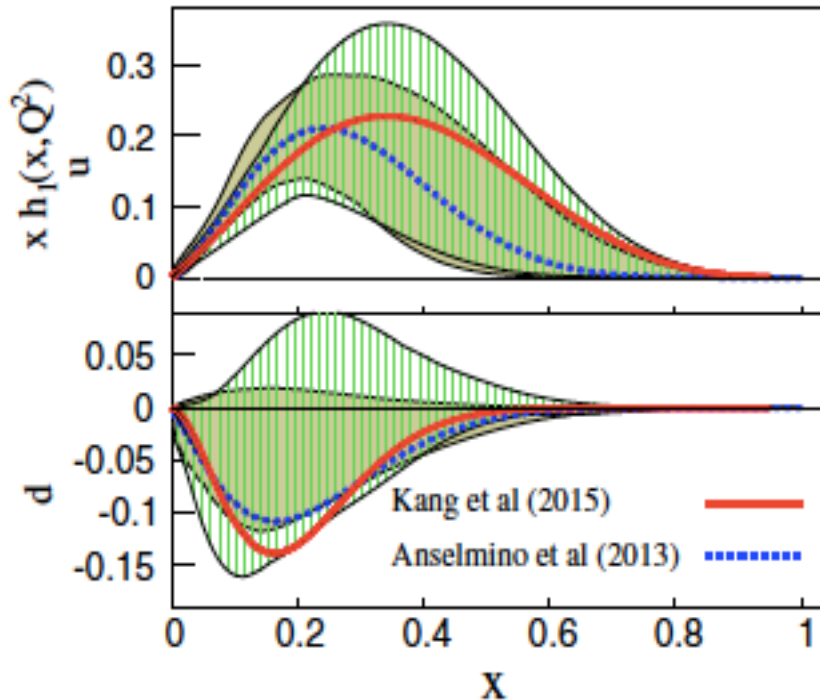


# Extraction of Transversity

## □ Transversity comparison:

Anselmino et al.,  
PRD 87, 094019 (2013)

Kang et al, PRD, 2016



✧ Consistent in overall shape and sign, but, different in details

✧ Large uncertainties!

## □ Future:

JLab12, Compass, EIC; Transverse polarized Drell-Yan?

# Tensor charge

## □ Definition:

$$\delta q = \int_0^1 [h_1^q(x) - h_1^{\bar{q}}(x)] dx$$

Moment – matrix elements of local operators

– fundamental QCD quantity – calculable on lattice or using models

## □ Extraction:

Anselmino et al.,  
PRD 87, 094019 (2013)

●  $\delta u = 0.39^{+0.18}_{-0.12}$

●  $\delta d = -0.25^{+0.30}_{-0.10}$

▲  $\delta u = 0.31^{+0.16}_{-0.12}$

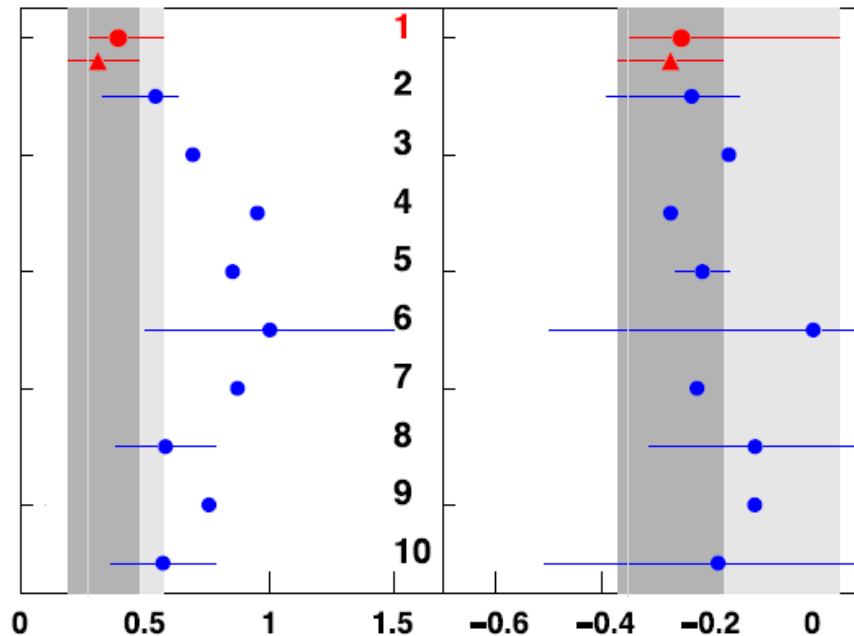
▲  $\delta d = -0.27^{+0.10}_{-0.10}$

✧ Extracted from global fits

by using two different  
parameterizations for  
Collins FF)

✧ Predictions from various  
models (including LQCD)

✧ Tensor charges are  
expected to be smaller  
than axial charge



$\Delta u = 0.787$     $\Delta d = -0.319$

# Tensor charge

## □ Definition:

$$\delta q = \int_0^1 [h_1^q(x) - h_1^{\bar{q}}(x)] dx$$

Moment – matrix elements of local operators

– fundamental QCD quantity – calculable on lattice or using models

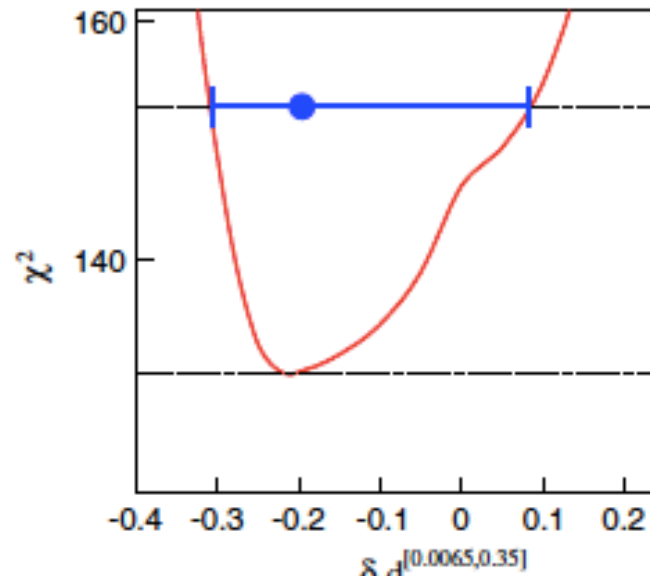
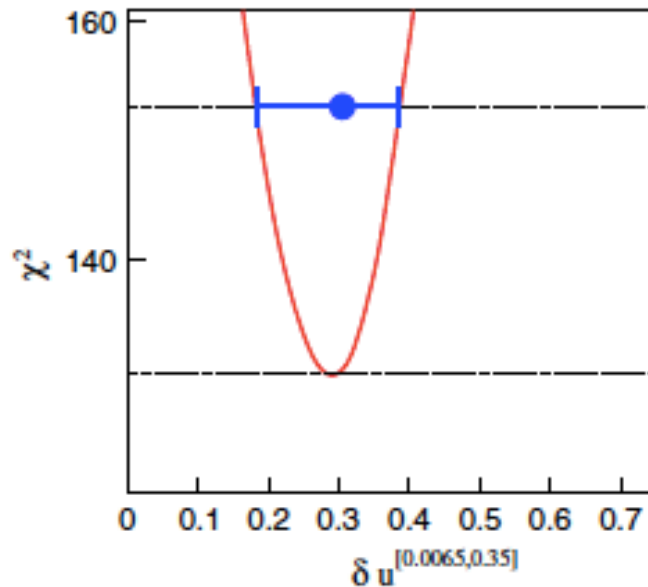
## □ Extraction from global fits :

$$\delta q^{[x_{\min}, x_{\max}]}(Q^2) \equiv \int_{x_{\min}}^{x_{\max}} dx h_1^q(x, Q^2)$$

$$\delta u^{[0.0065, 0.35]} = +0.30_{-0.12}^{+0.08}$$

$$\delta d^{[0.0065, 0.35]} = -0.20_{-0.11}^{+0.28}$$

Kang et al, PRD, 2016



$Q^2 = 10 \text{ GeV}^2$

90% C.L.

$$\Delta u = 0.787 \quad \Delta d = -0.319$$

# Summary of lecture six

- ❑ With the existing data from lepton-hadron and hadron-hadron collisions with polarized beams, we have a good idea on the quark/gluon helicity contribution to proton's spin
- ❑ Transversity and tensor charge are fundamental QCD quantities!
- ❑ But, EIC is a ultimate QCD machine, and absolutely needed:
  - 1) **to discover and explore** the quark/gluon structure and properties of hadrons and nuclei,
  - 2) **to search for** hints and clues of color confinement, and
  - 3) **to measure** the color fluctuation and color neutralization

*In particular, EIC can determine the helicity contribution to proton's spin, and to answer the question if there is a need for orbital contribution*

**Thanks!**

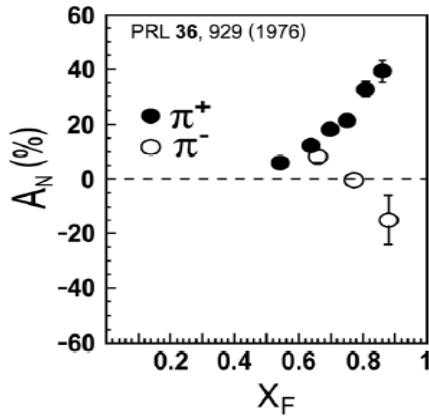
**Backup slides**

# QCD and hadrons

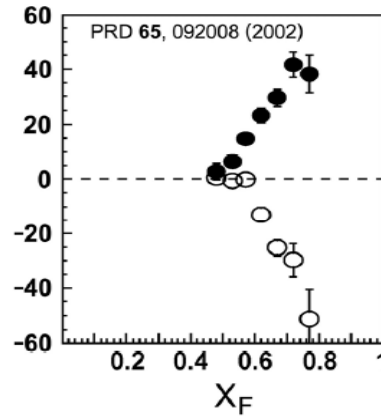
# Single transverse-spin asymmetry

□  $A_N$  - consistently observed for over 35 years (~ 0 in parton model)!

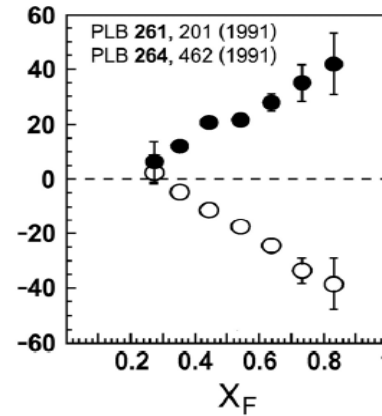
ANL – 4.9 GeV



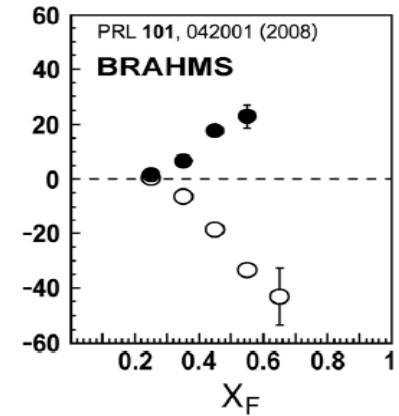
BNL – 6.6 GeV



FNAL – 20 GeV

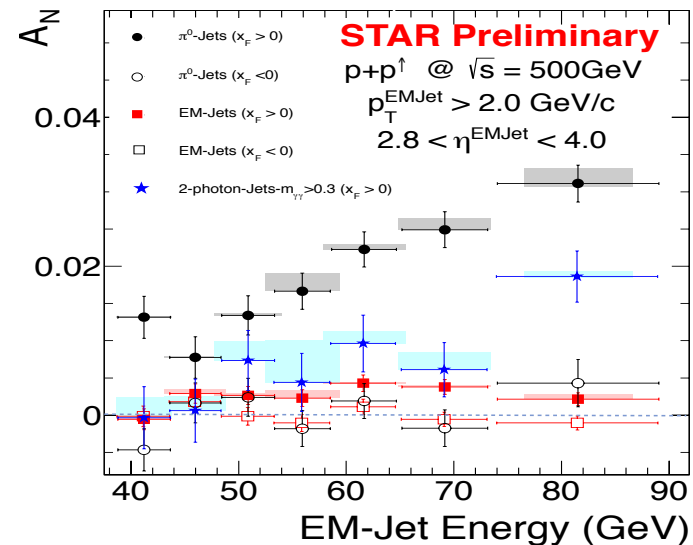
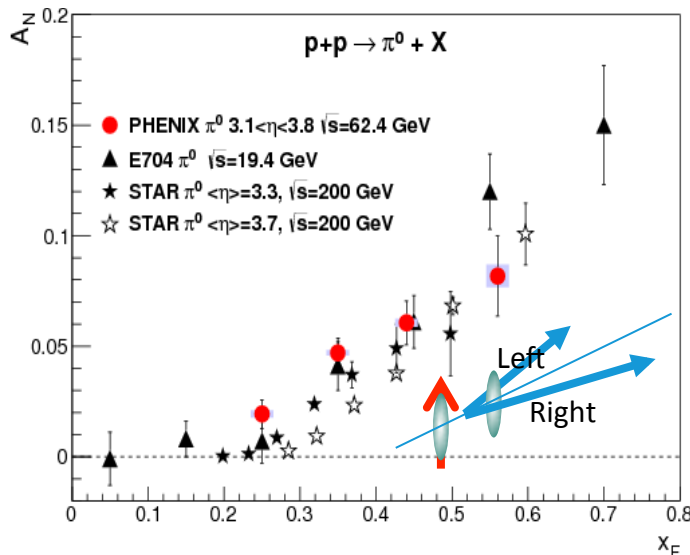


BNL – 62.4 GeV



□ Survived the highest RHIC energy:

$$A_N \equiv \frac{\Delta\sigma(l, \vec{s})}{\sigma(l)} = \frac{\sigma(l, \vec{s}) - \sigma(l, -\vec{s})}{\sigma(l, \vec{s}) + \sigma(l, -\vec{s})}$$



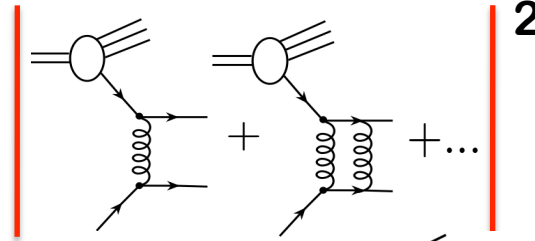


# Do we understand it?

Kane, Pumplin, Repko, PRL, 1978

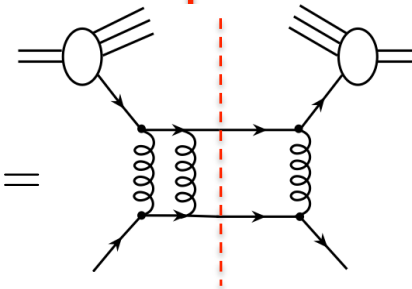
## □ Early attempt:

Cross section:  $\sigma_{AB}(p_T, \vec{s}) \propto$



Asymmetry:

$$\sigma_{AB}(p_T, \vec{s}) - \sigma_{AB}(p_T, -\vec{s}) =$$



$$\propto \alpha_s \frac{m_q}{p_T}$$

Too small to explain available data!

## □ What do we need?

$$A_N \propto i\vec{s}_p \cdot (\vec{p}_h \times \vec{p}_T) \Rightarrow i\epsilon^{\mu\nu\alpha\beta} p_{h\mu} s_\nu p_\alpha p'_{h\beta}$$

Need a phase, a spin flip, enough vectors

## □ Vanish without parton's transverse motion:

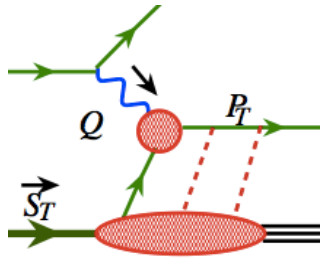


A direct probe for parton's transverse motion,

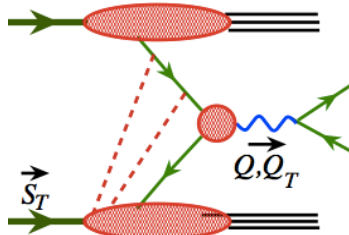
Spin-orbital correlation, QCD quantum interference

# Current understanding of SSAs

□ Two scales observables –  $Q_1 \gg Q_2 \sim \Lambda_{\text{QCD}}$ :



**SIDIS:  $Q \gg P_T$**



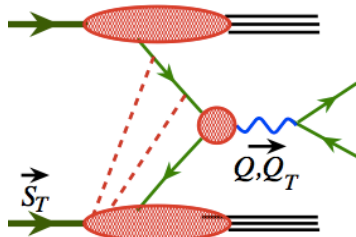
**DY:  $Q \gg Q_T$**



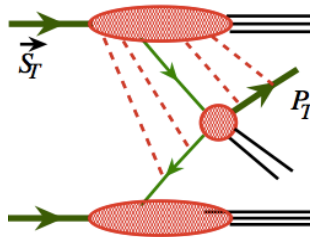
**TMD factorization**  
**TMD distributions**

*Direct information on  
parton  $k_T$*

□ One scale observables –  $Q \gg \Lambda_{\text{QCD}}$ :



**DY:  $Q \sim Q_T$**



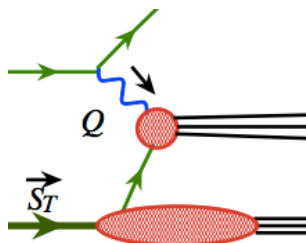
**Jet, Particle:  $P_T$**



**Collinear factorization**  
**Twist-3 distributions**

*Information on  
moments of parton  $k_T$*

□ Symmetry plays important role:



**Inclusive DIS**  
**Single scale**  
**Q**

**Parity**  
**Time-reversal**



**$A_N = 0$**